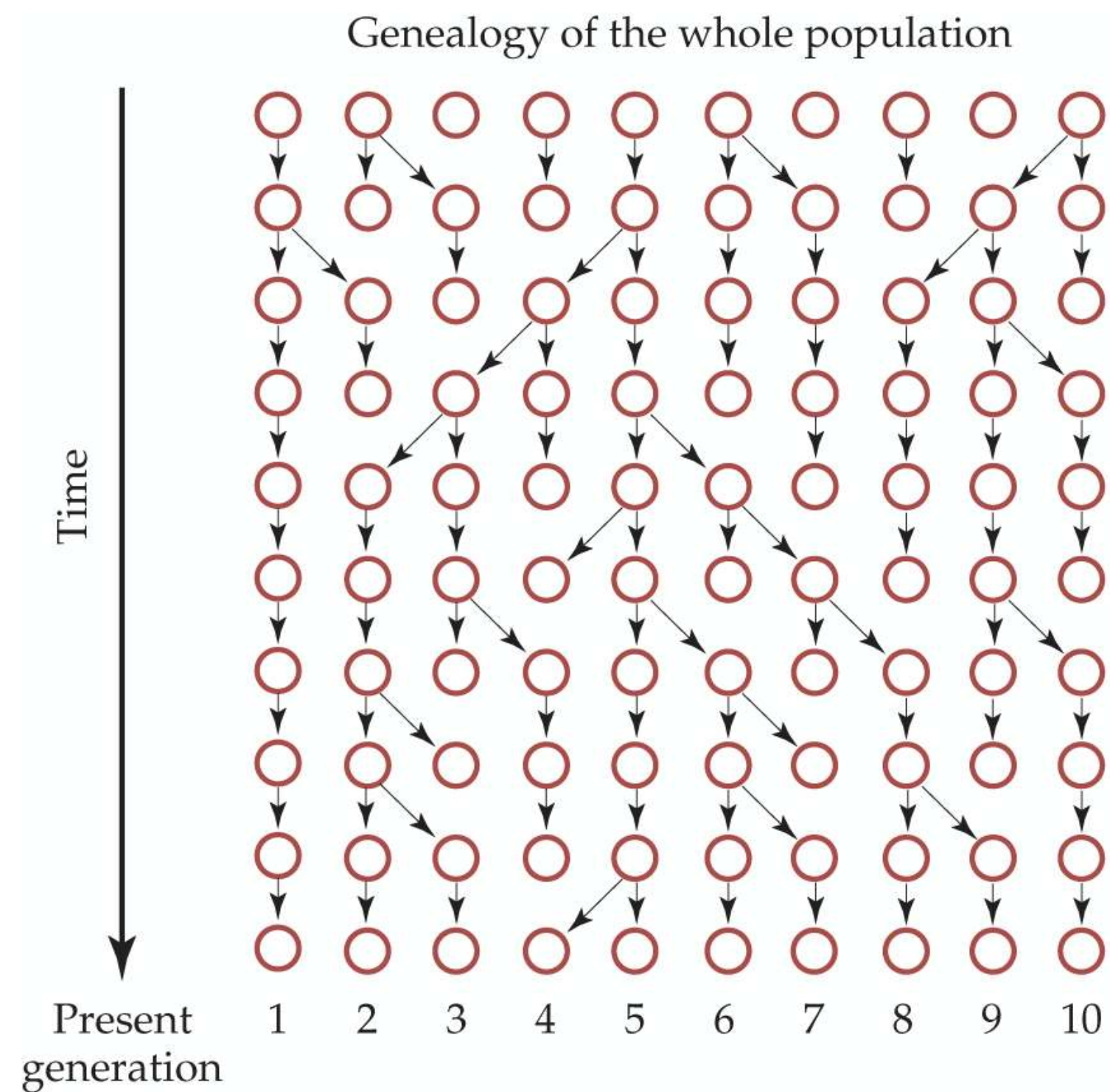


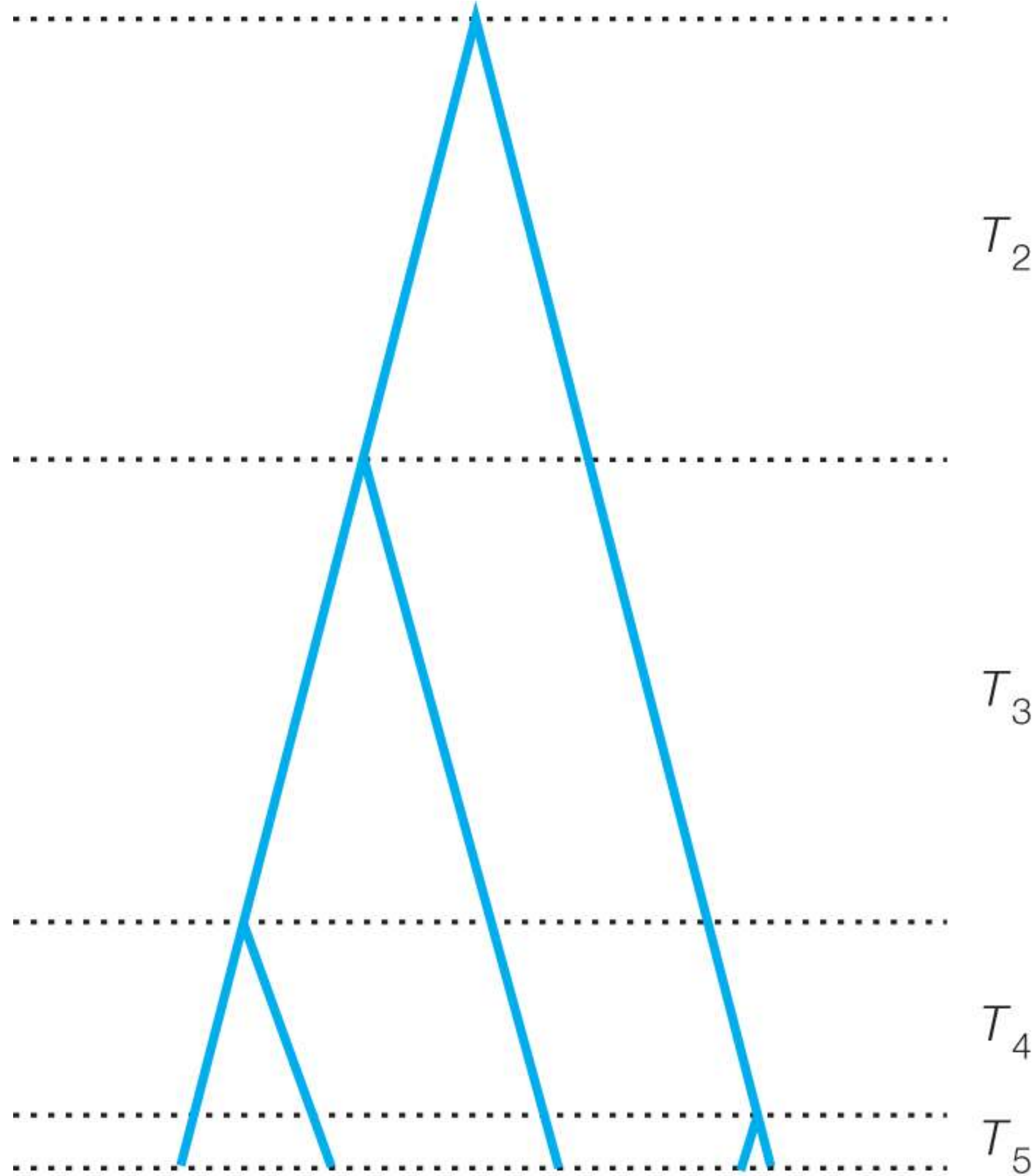
Outline for today

1. Coalescent
2. Multispecies coalescent

Matthew Hahn
mwh@iu.edu
@3rdreviewer

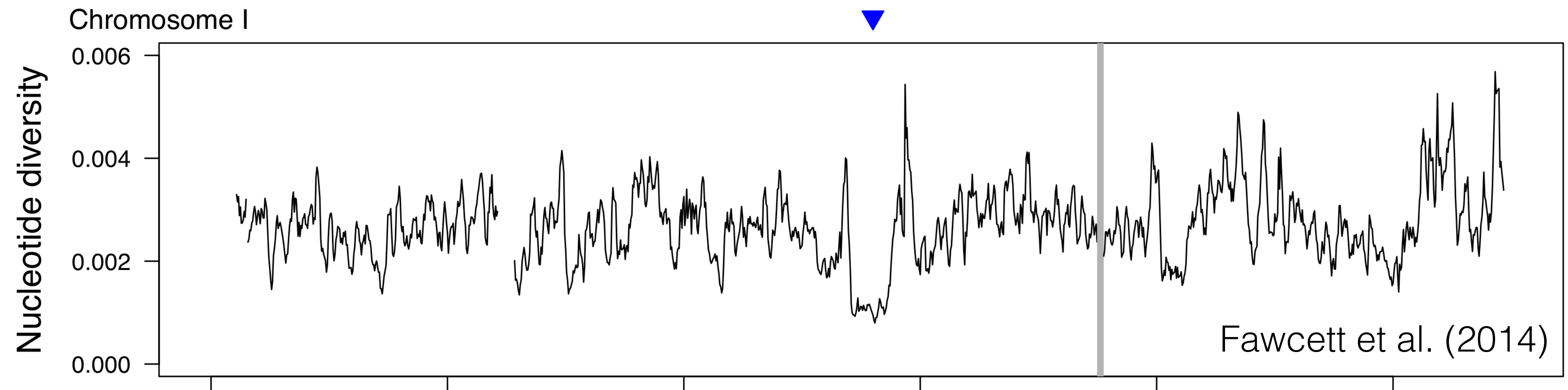
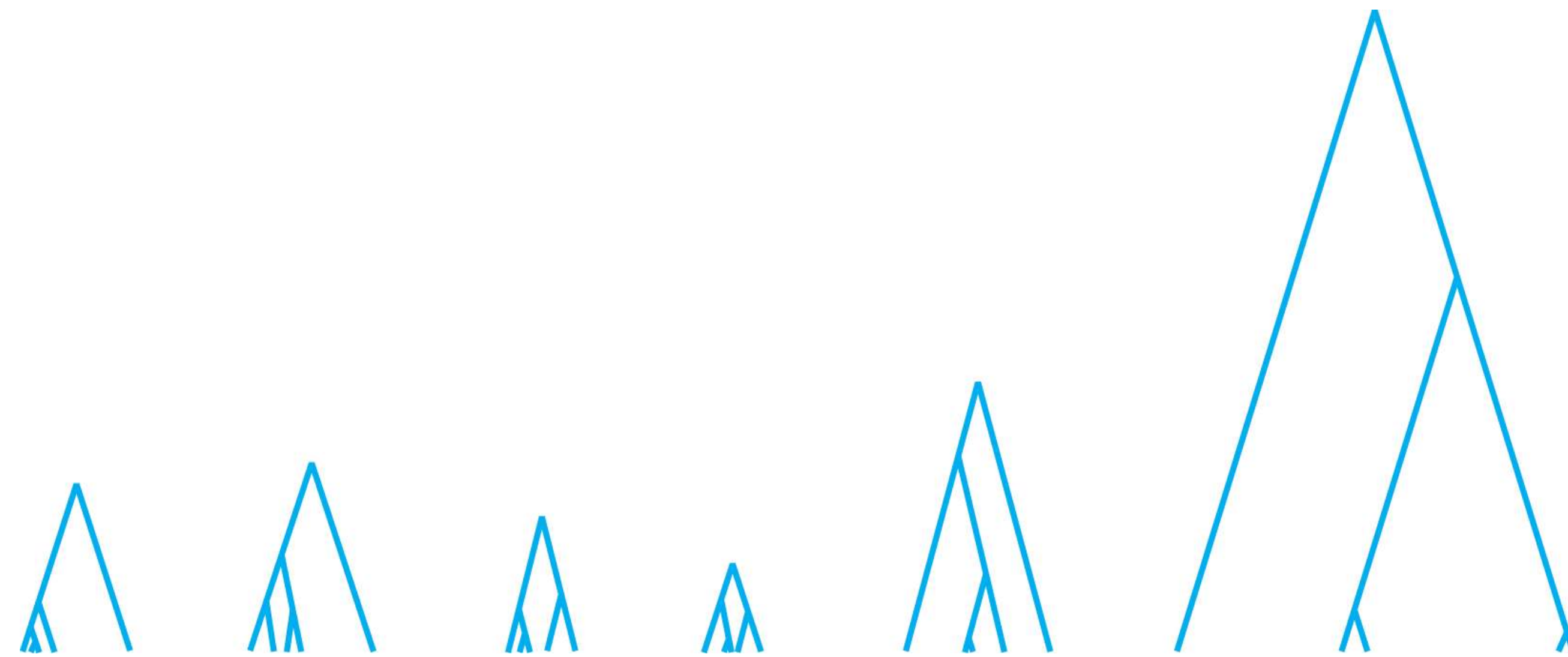
Why do we need the coalescent model?





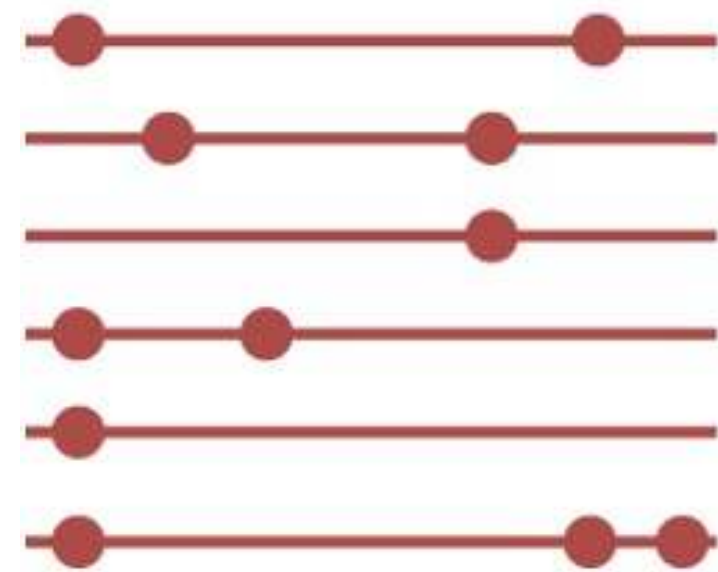
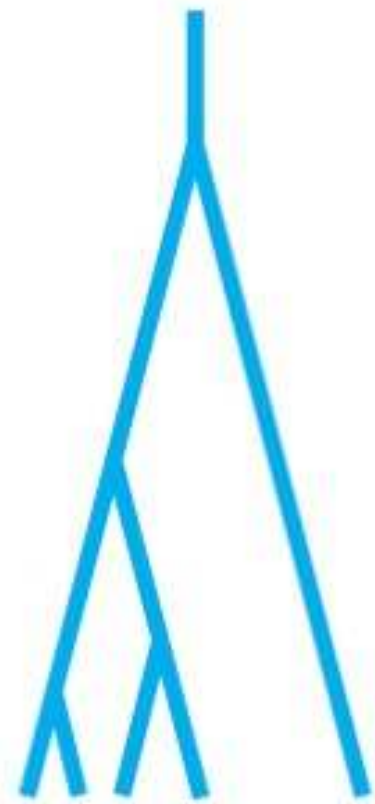
Algorithm for generating a coalescent tree

1. Start with $i=n$ chromosomes
2. Choose a time until first coalescence from an exponential distribution with parameter $\lambda = i(i-1)/2$
3. Choose two chromosomes at random to coalesce
4. Merge the two lineages chosen, and have $i \rightarrow i-1$
5. If $i > 1$ go to 2; if not stop

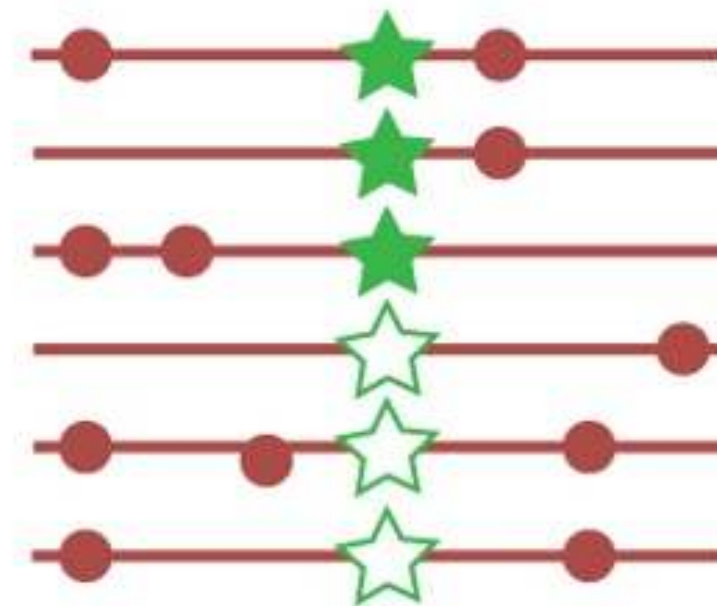
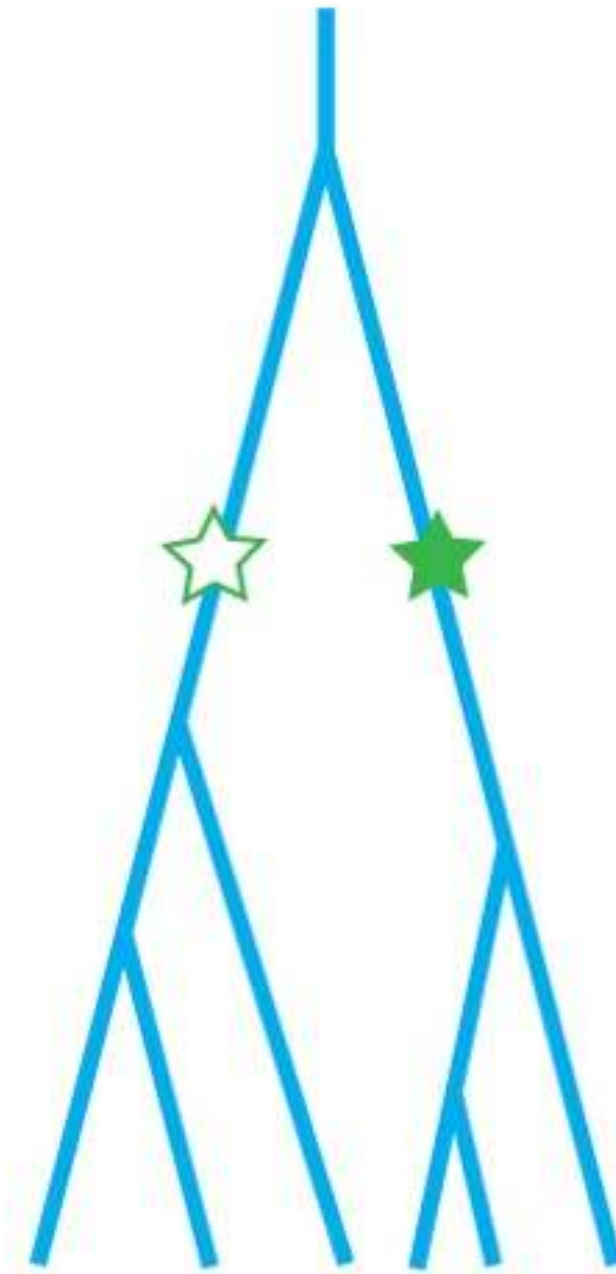


<https://bedford.io/projects/coaltrace/>

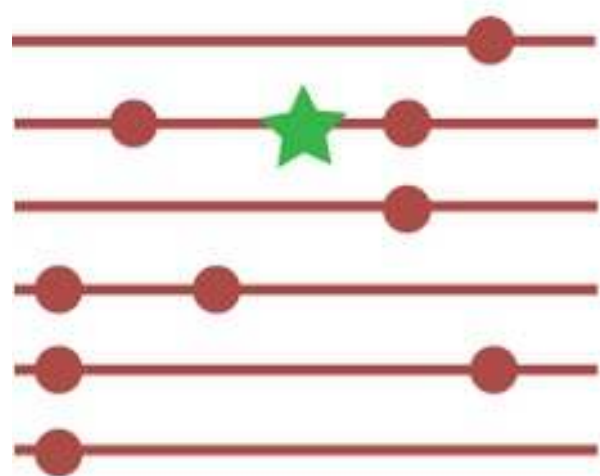
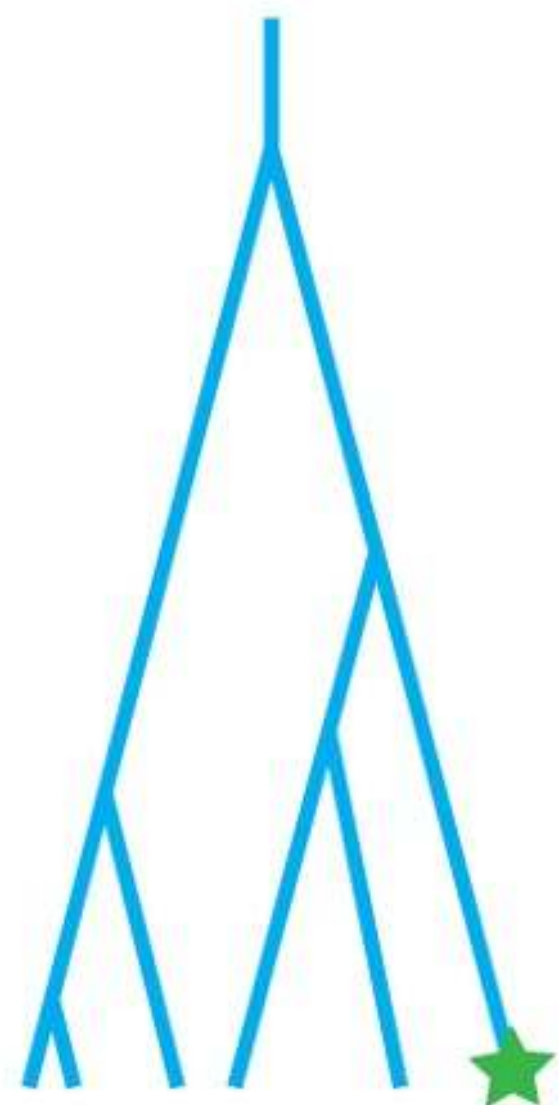
(A)



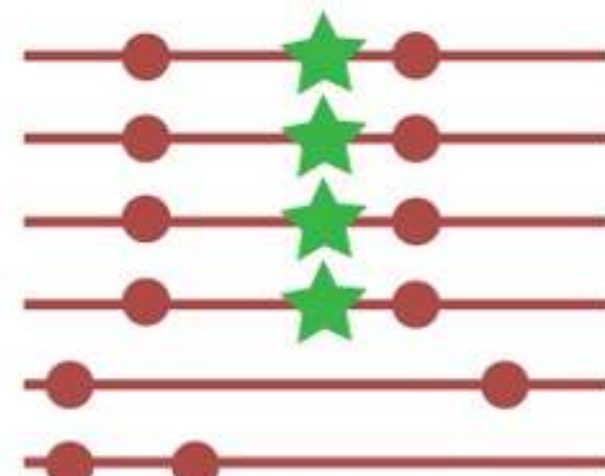
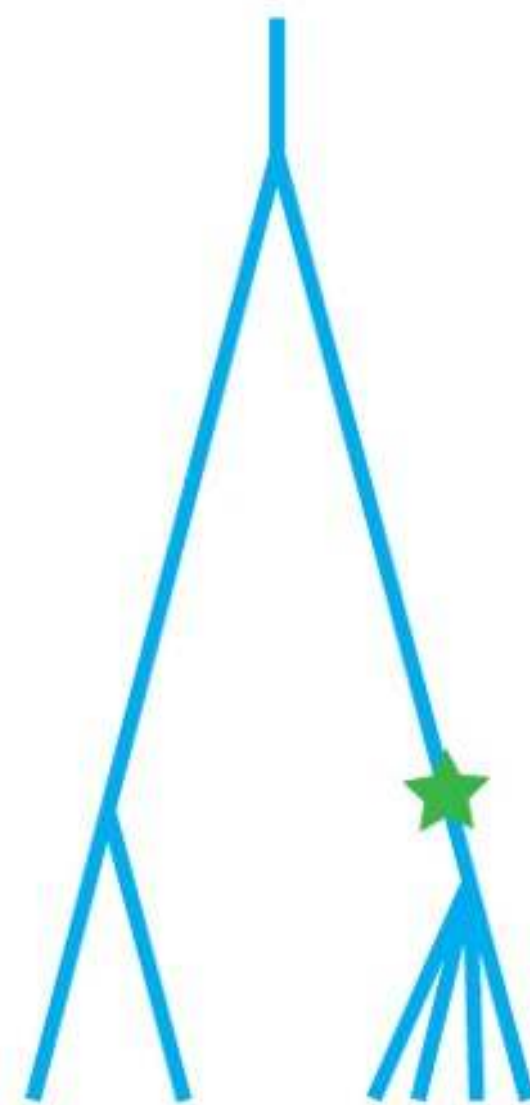
(B)

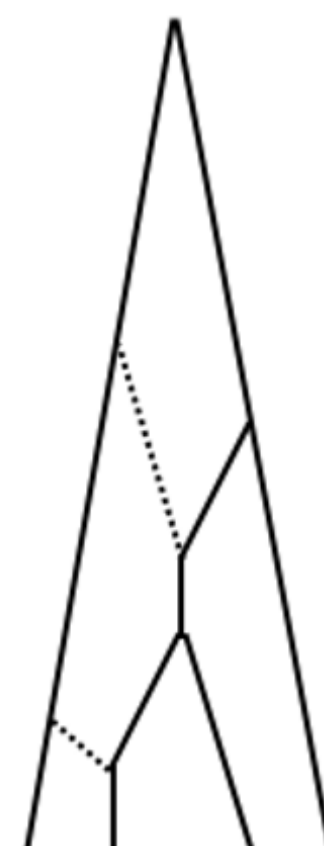
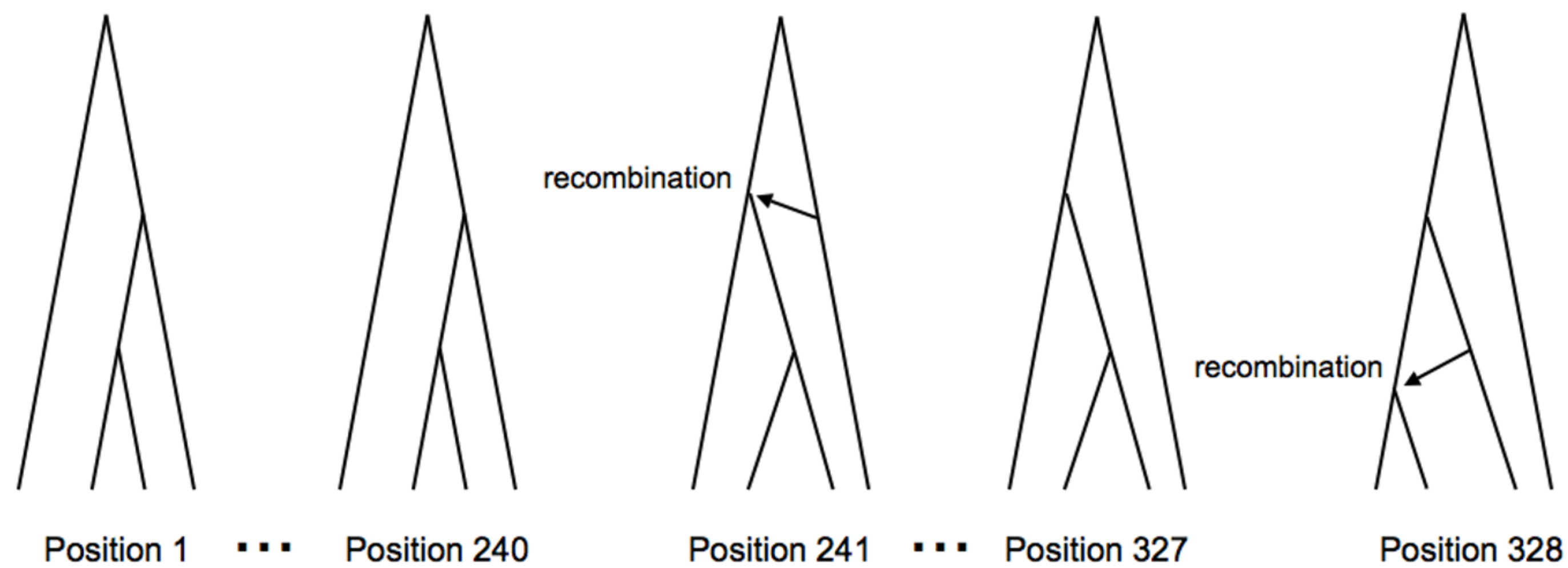


(A)



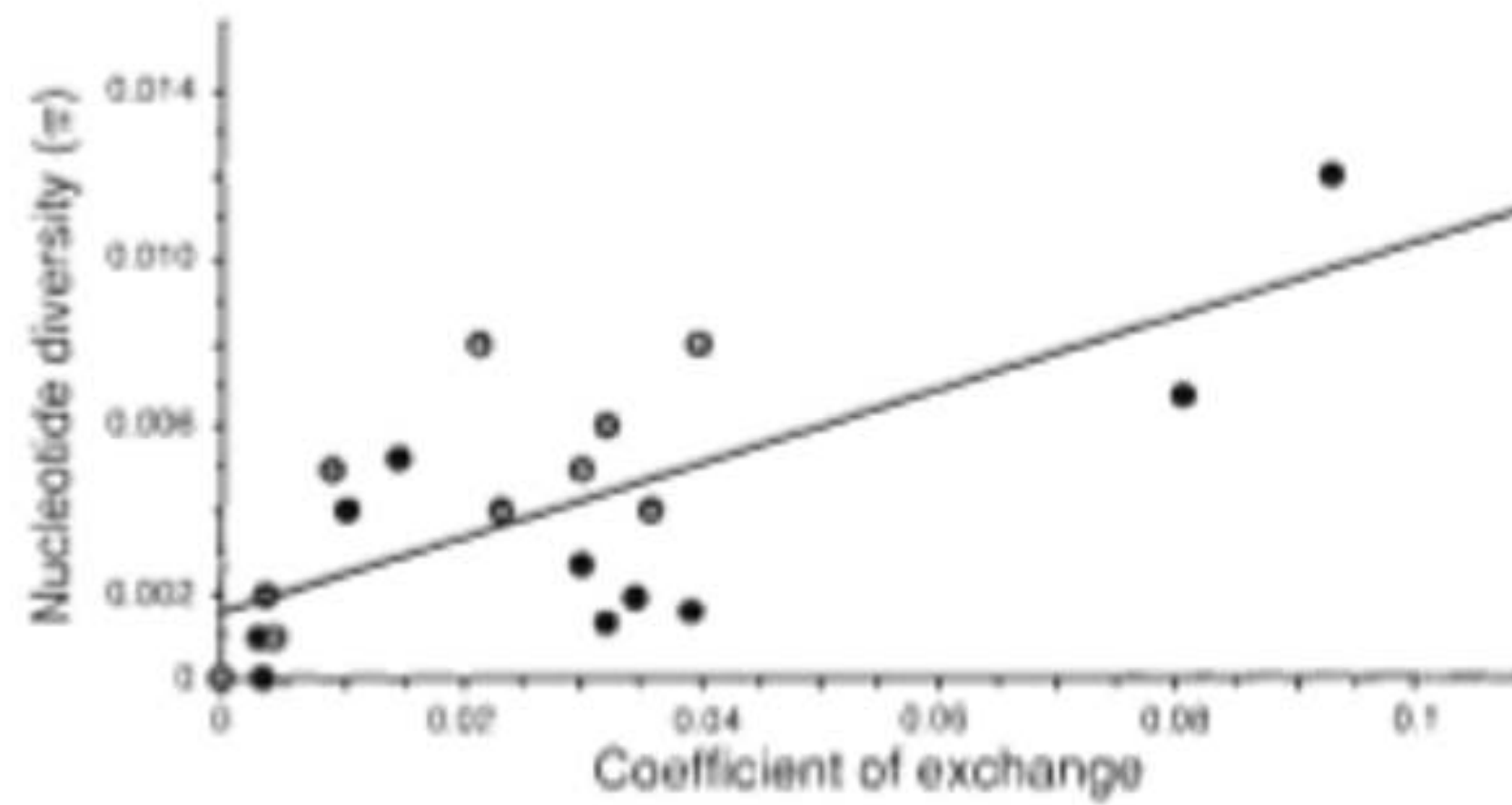
(B)



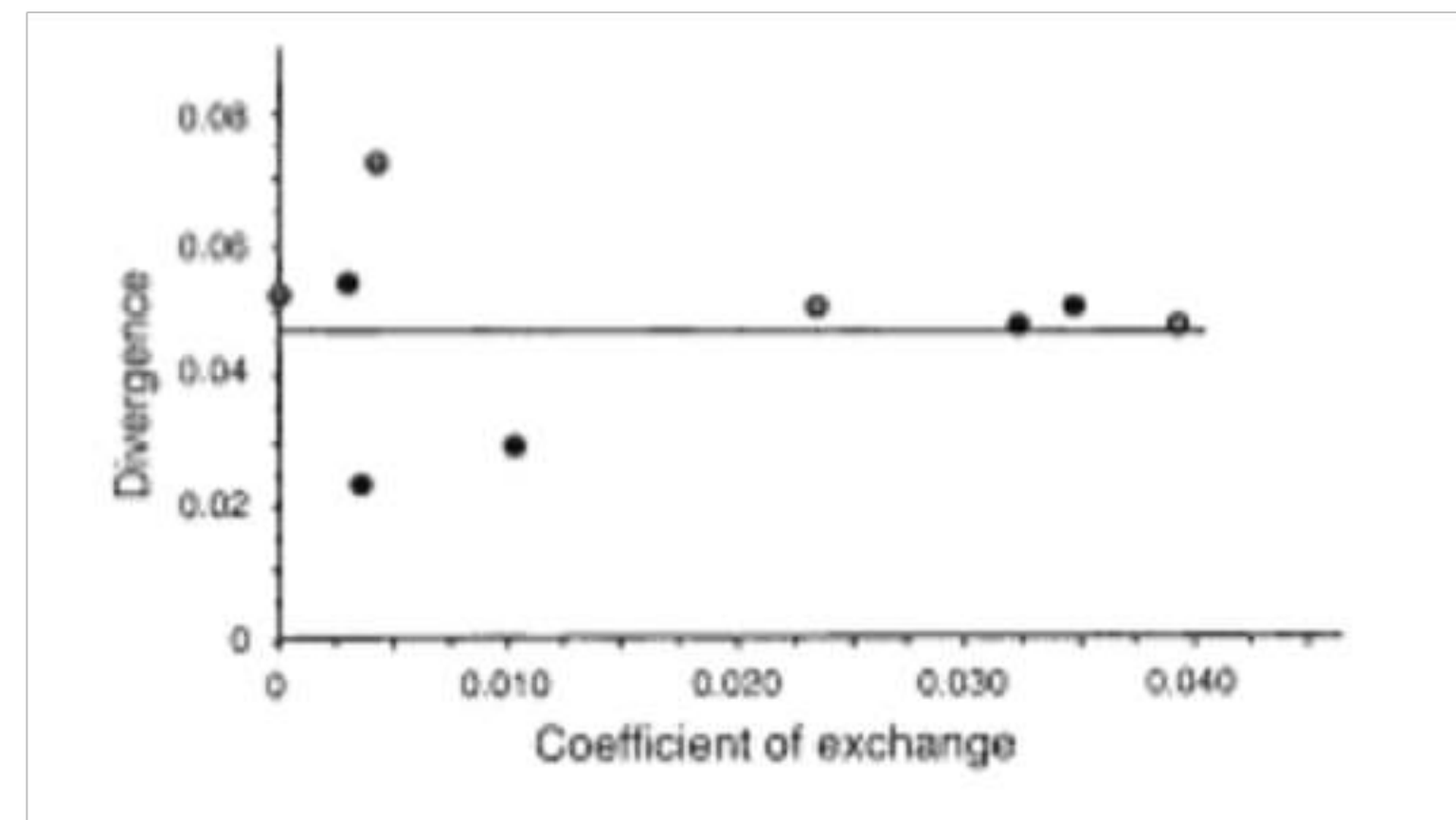


Ancestral recombination graph

Polymorphism vs. recombination



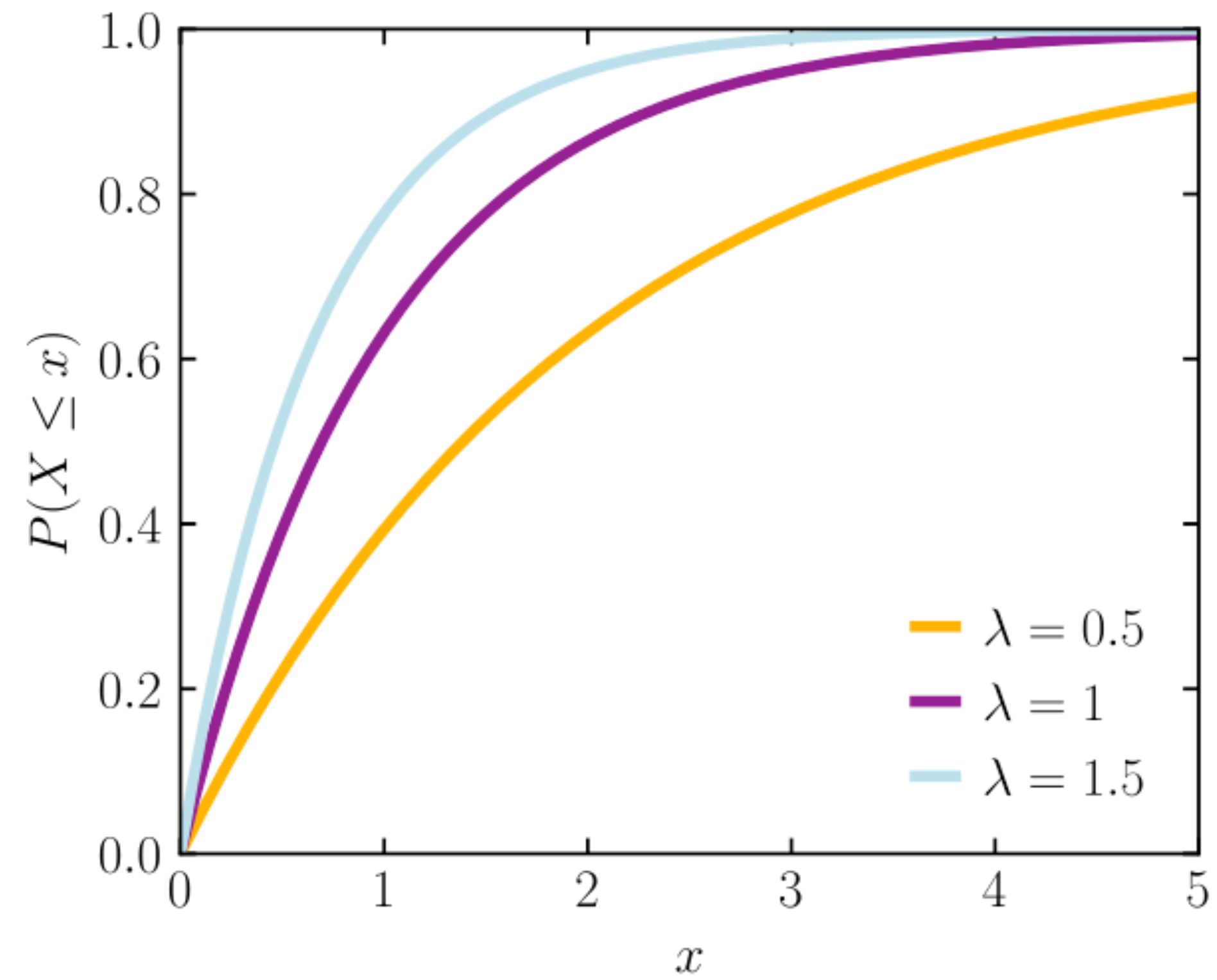
Divergence vs. recombination



Begun and Aquadro (1992)

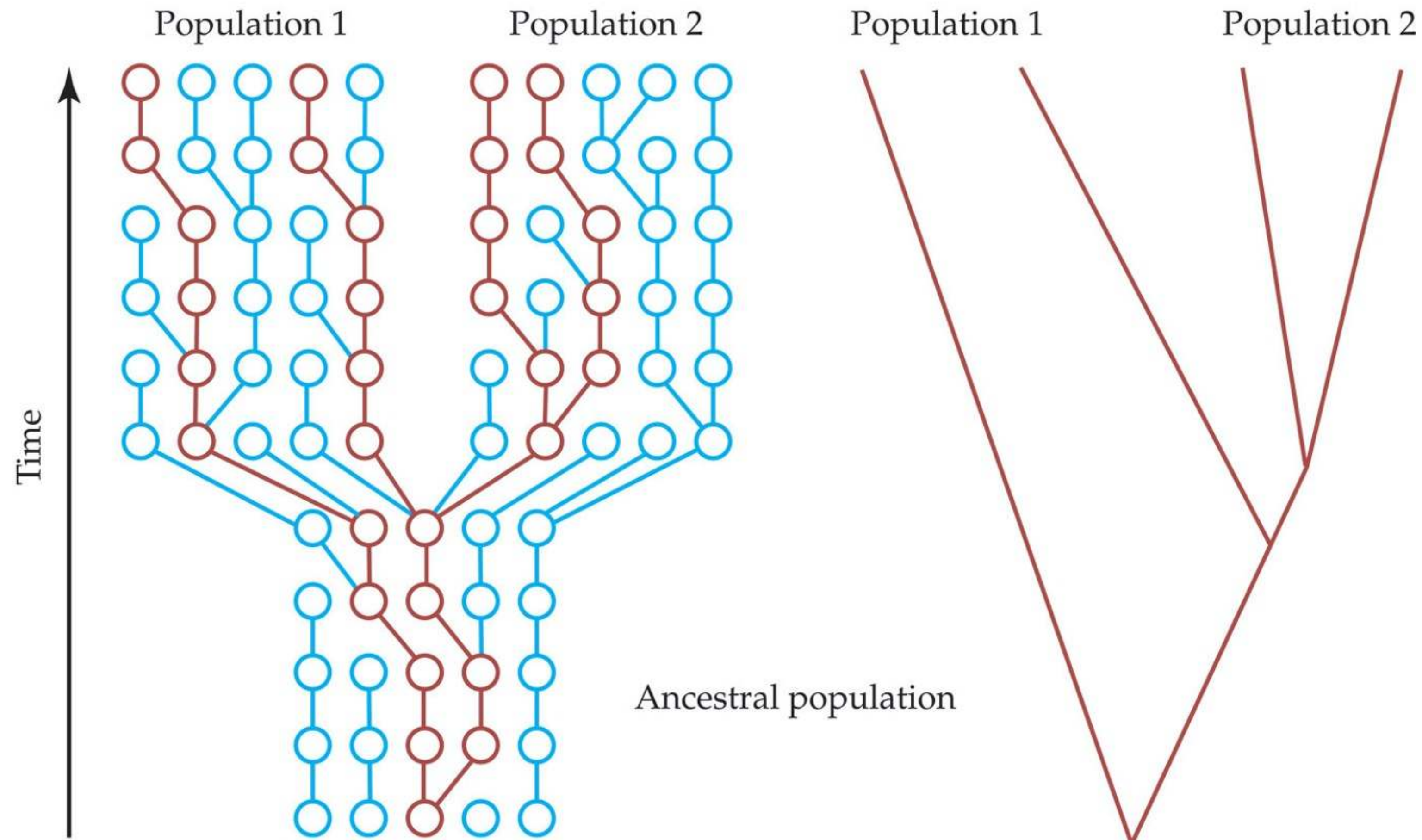
Cumulative distribution function of exponential: $1 - e^{-\lambda x}$

(For two lineages, $\lambda = 1$)



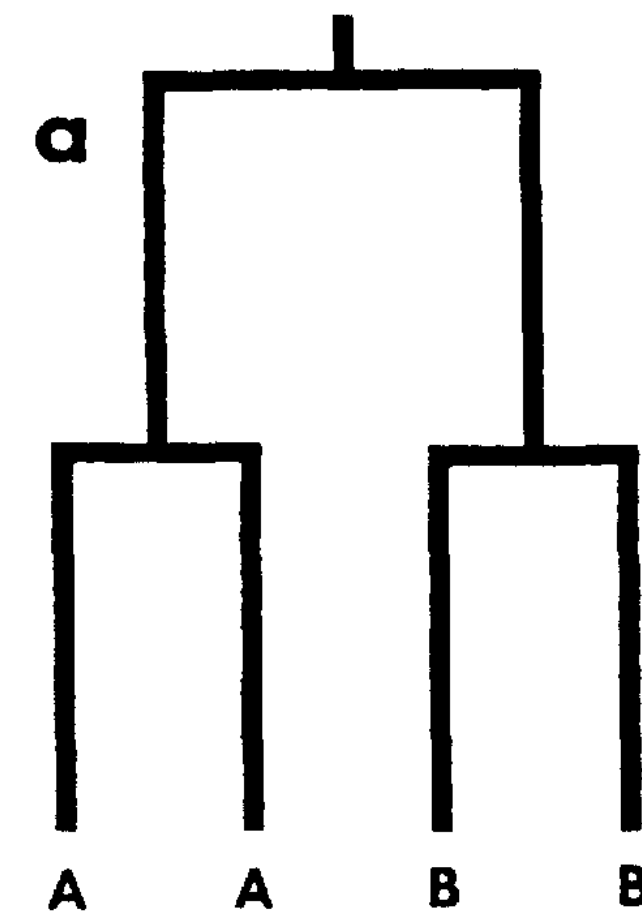
(B)

Incomplete lineage sorting

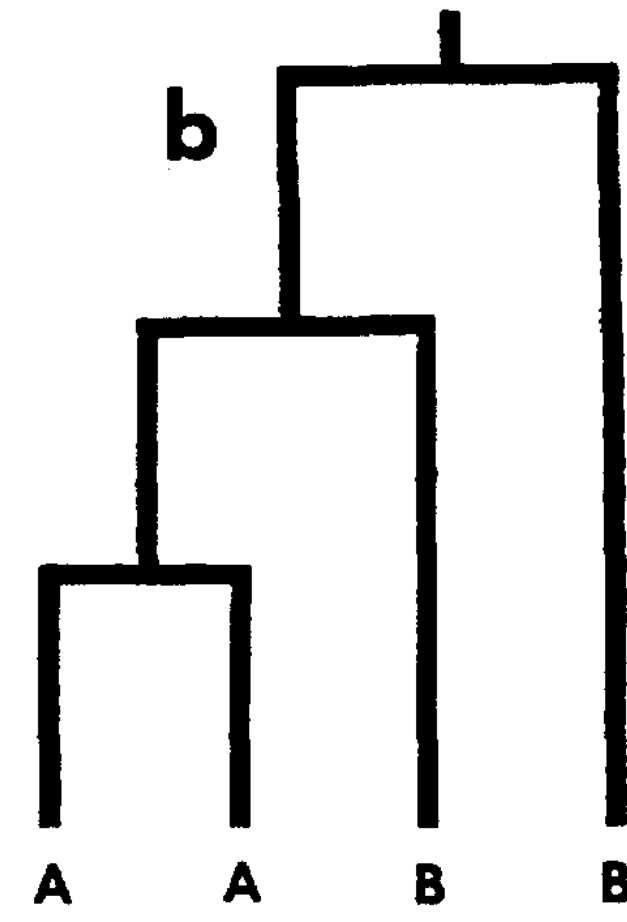


INTRODUCTION TO POPULATION GENETICS, Figure 5.5 (Part 2)
© 2013 Sinauer Associates, Inc.

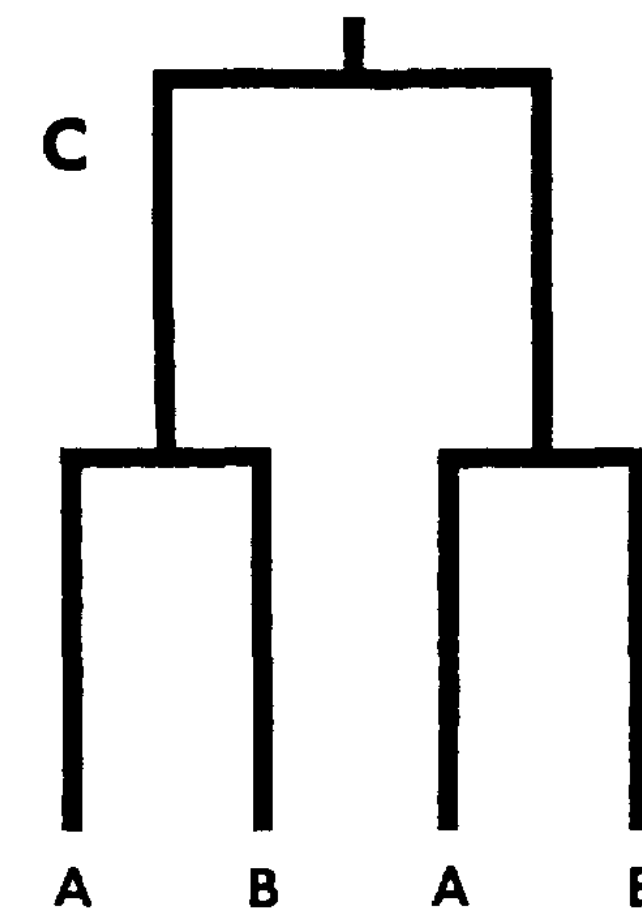
Nielsen and Slatkin (2013)



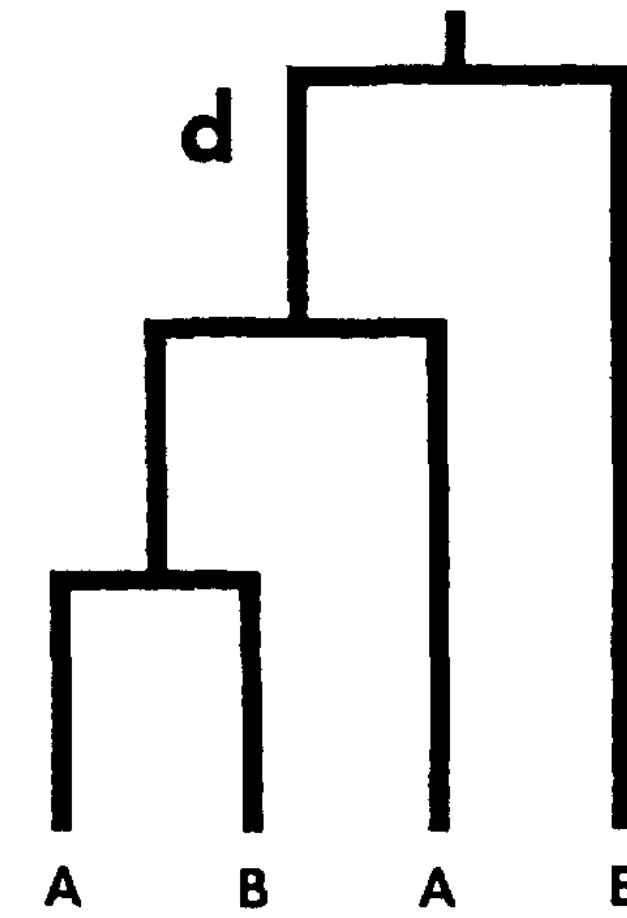
$$P = \left(1 - \frac{2}{3} e^{-\frac{t}{2N}}\right)^2$$



$$P = \frac{4}{3} e^{-\frac{t}{2N}} \left(1 - \frac{5}{6} e^{-\frac{t}{2N}}\right)$$

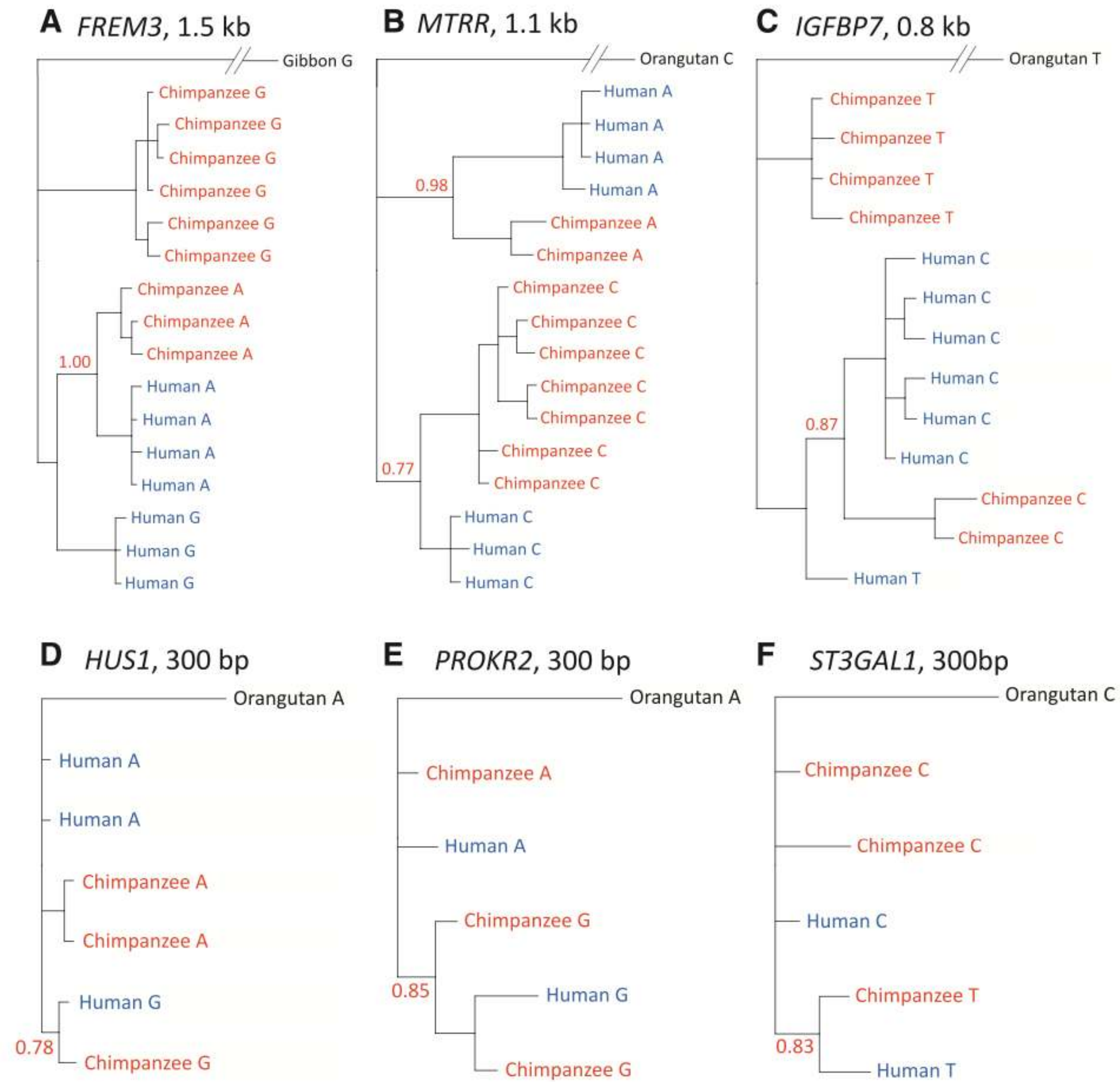


$$P = \frac{2}{9} e^{-\frac{t}{N}}$$

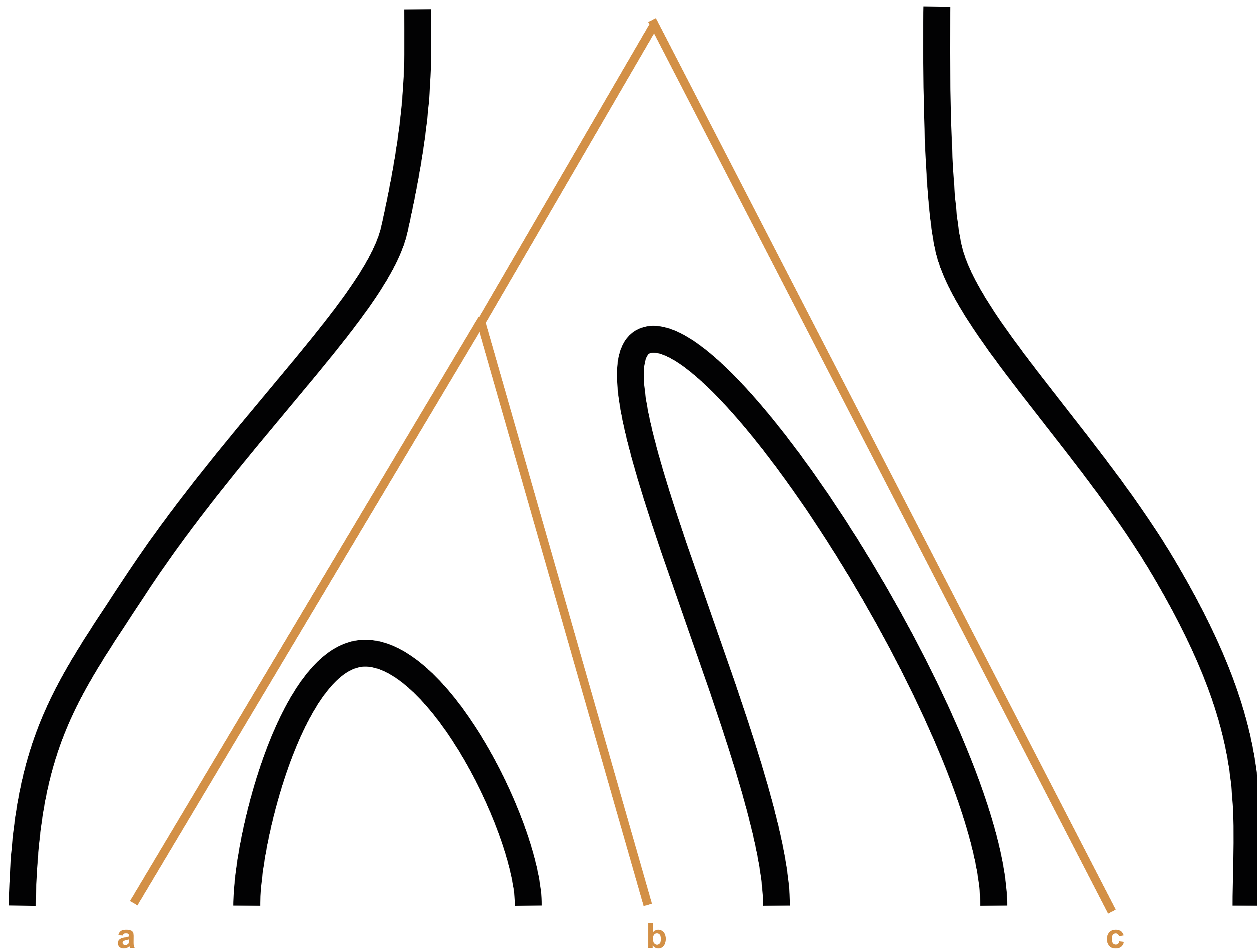


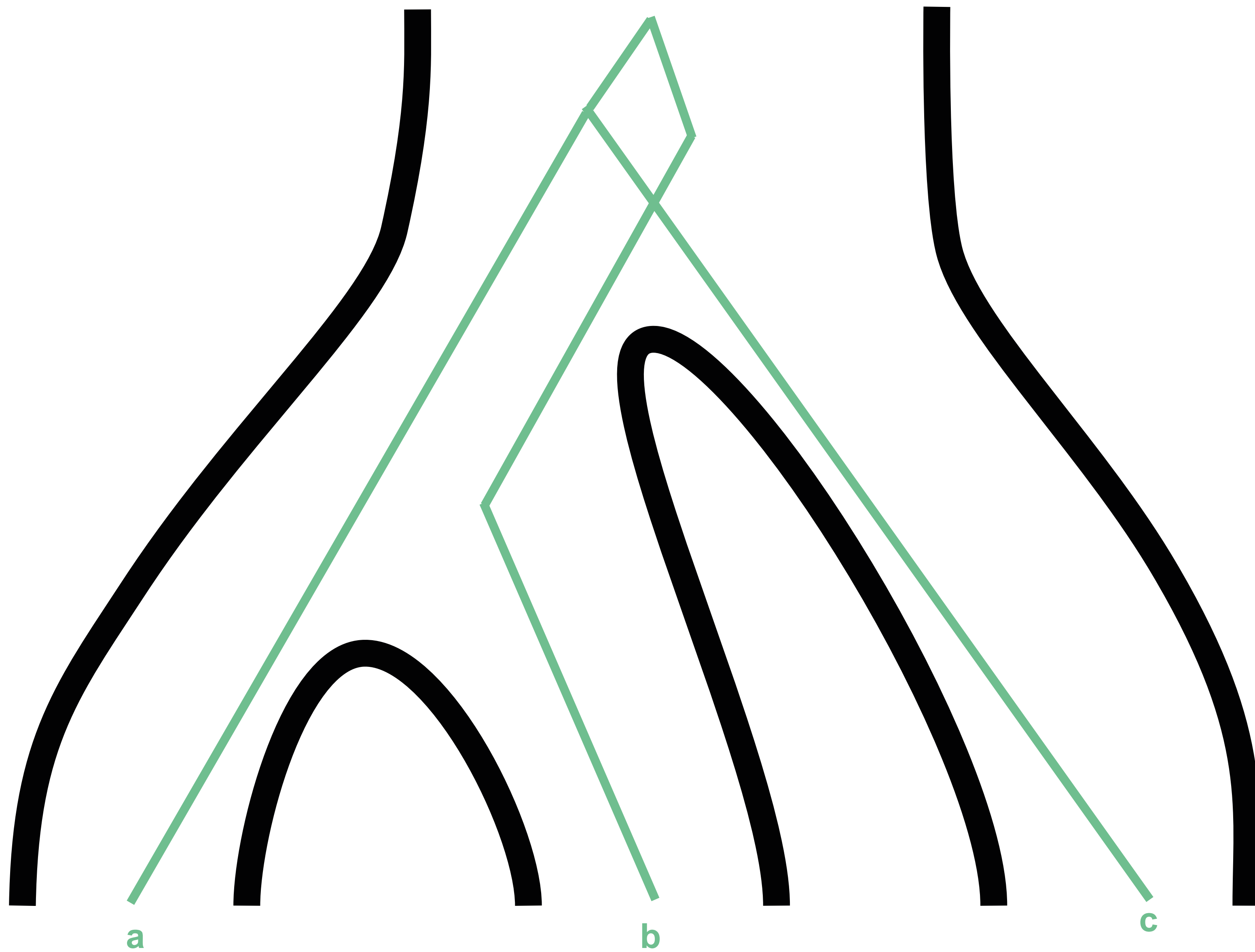
$$P = \frac{4}{9} e^{-\frac{t}{N}}$$

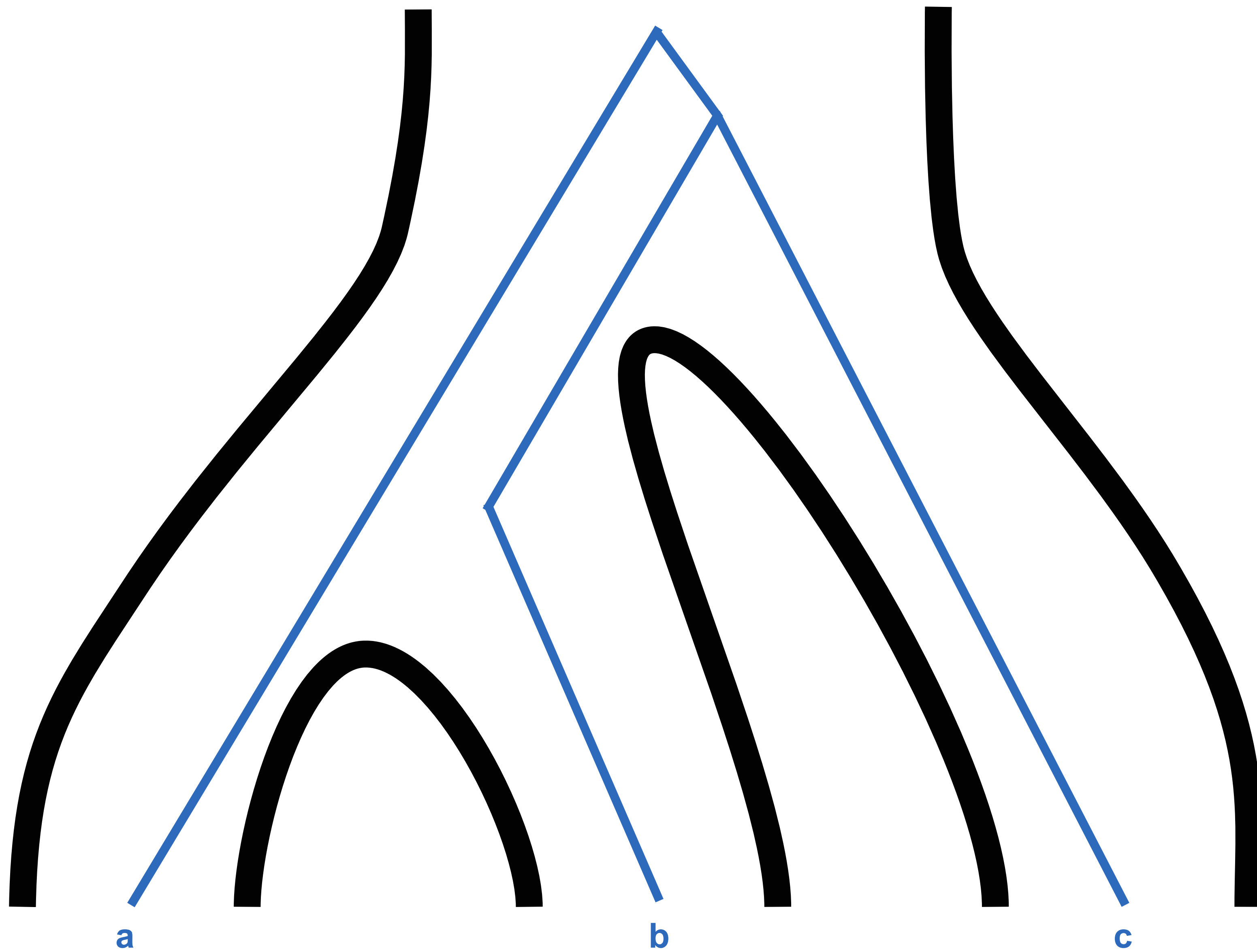
Tajima (1983)



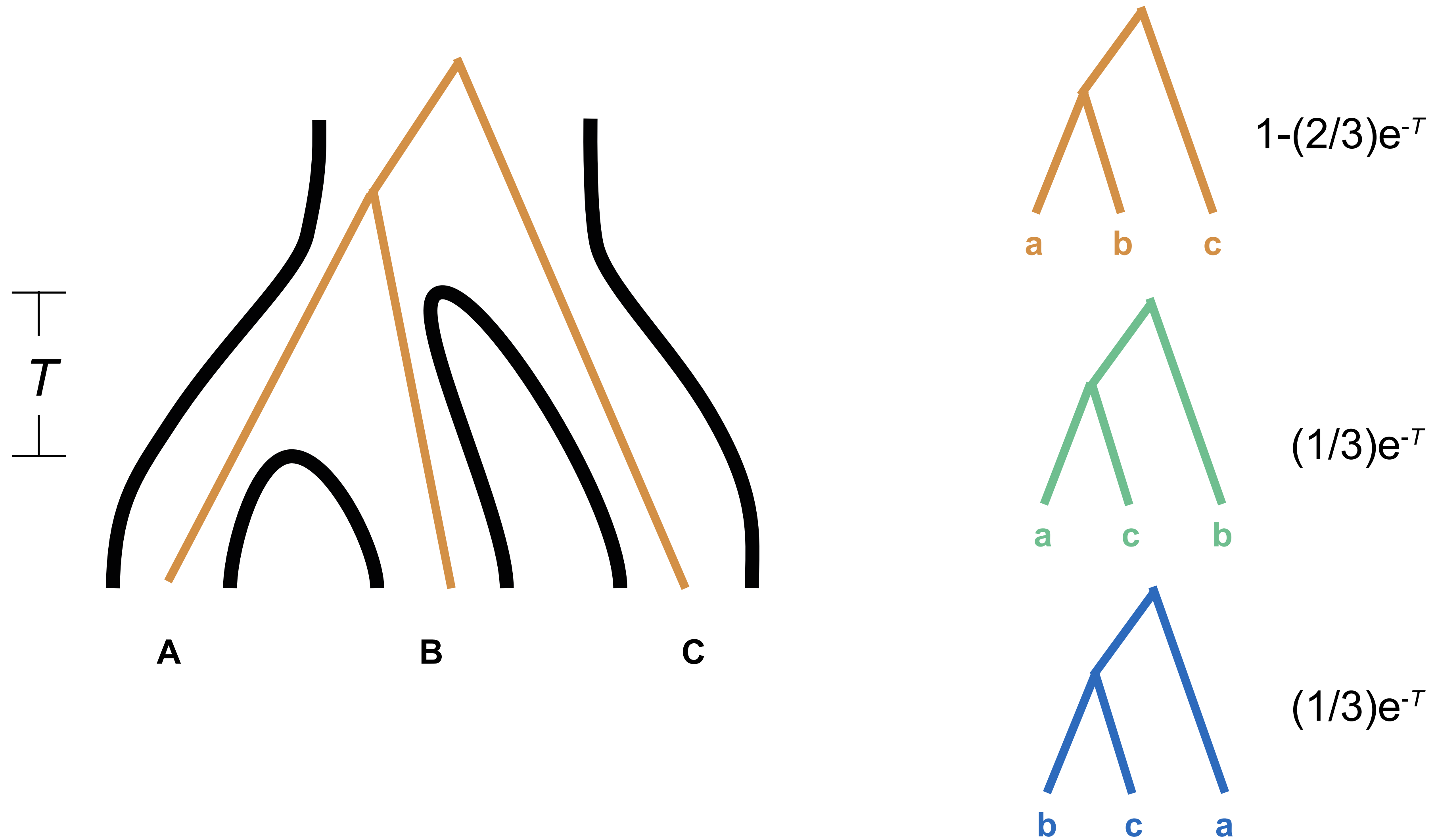
Leffler et al. (2013)

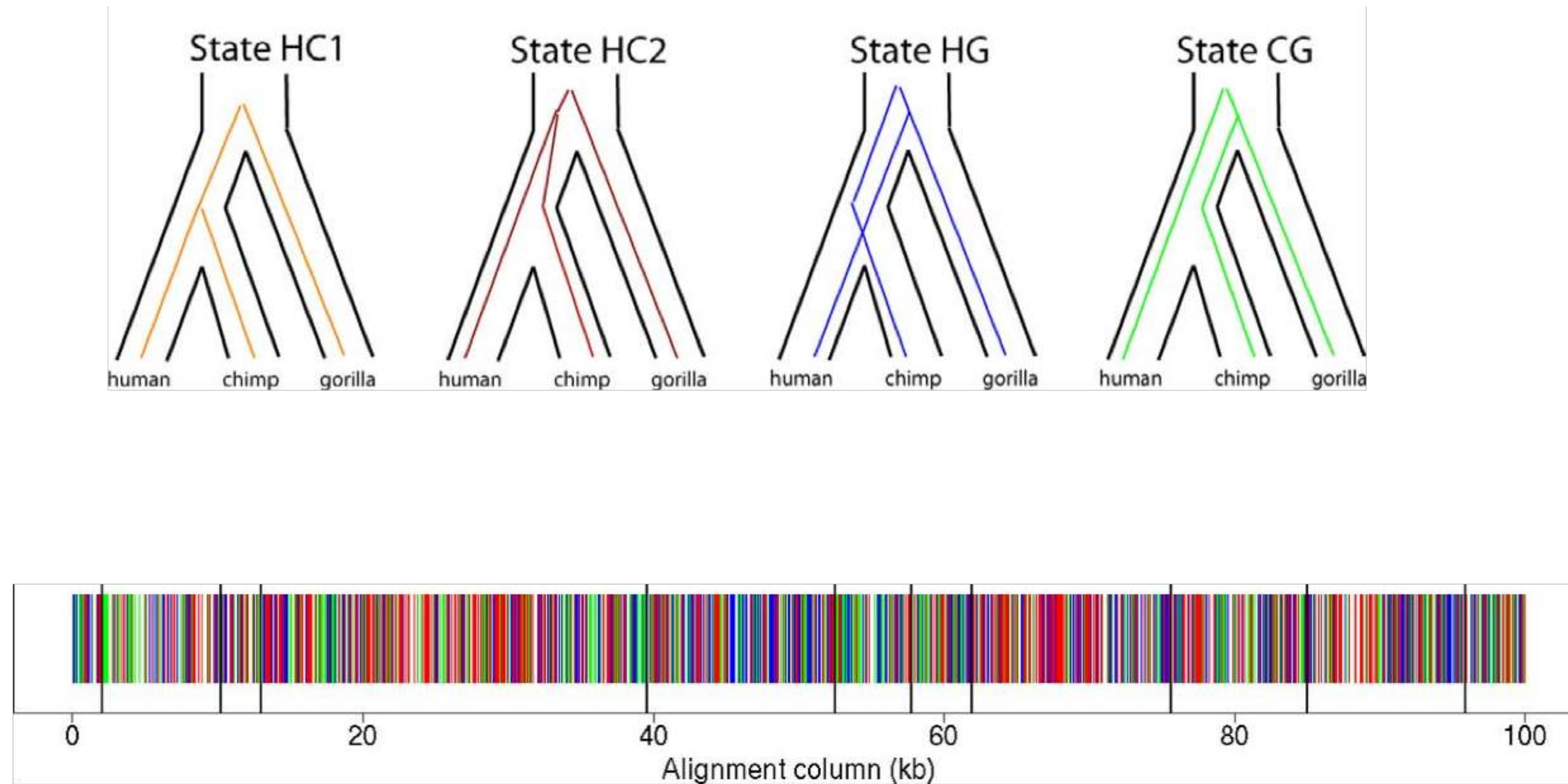




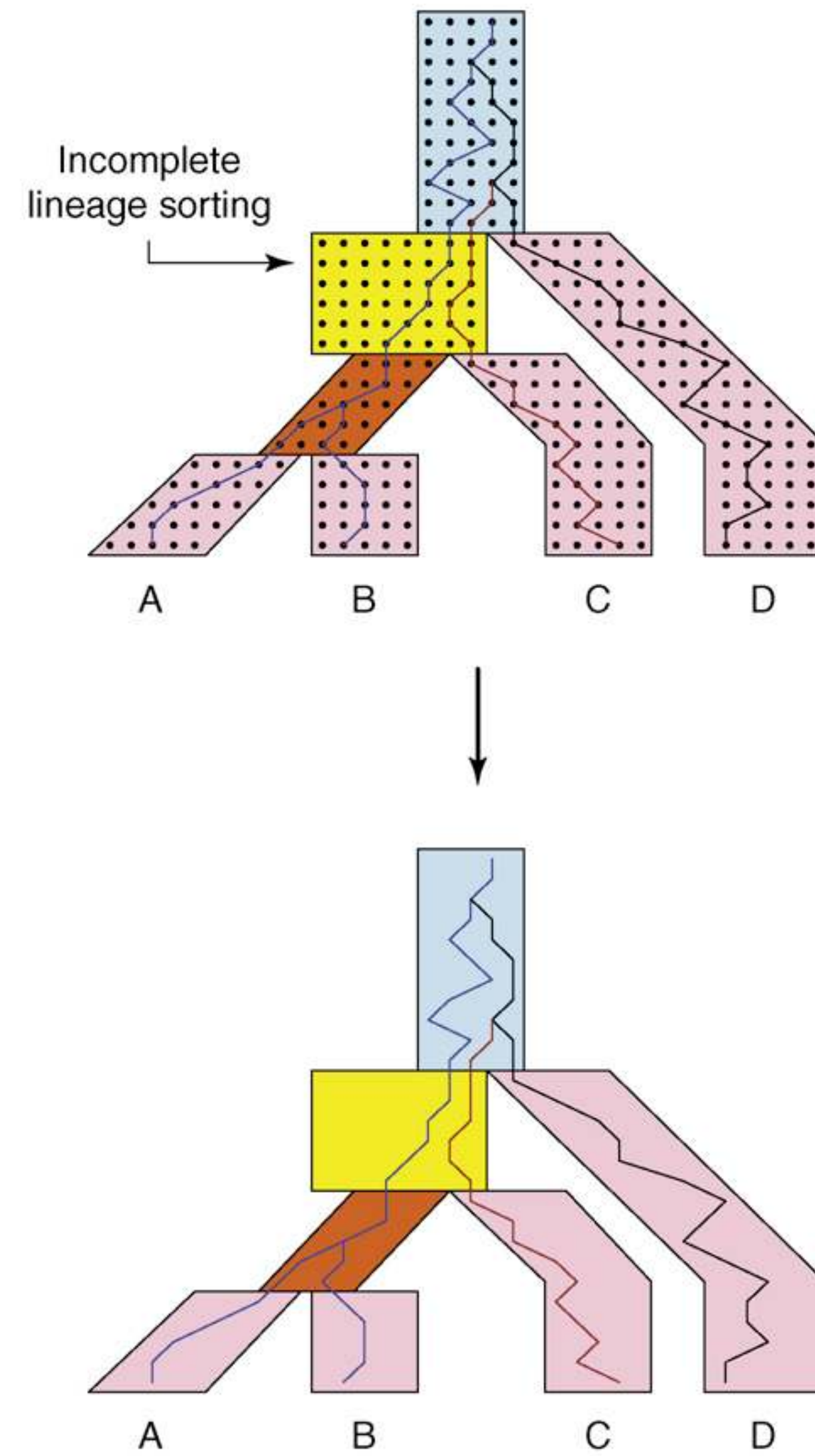


The multispecies coalescent model

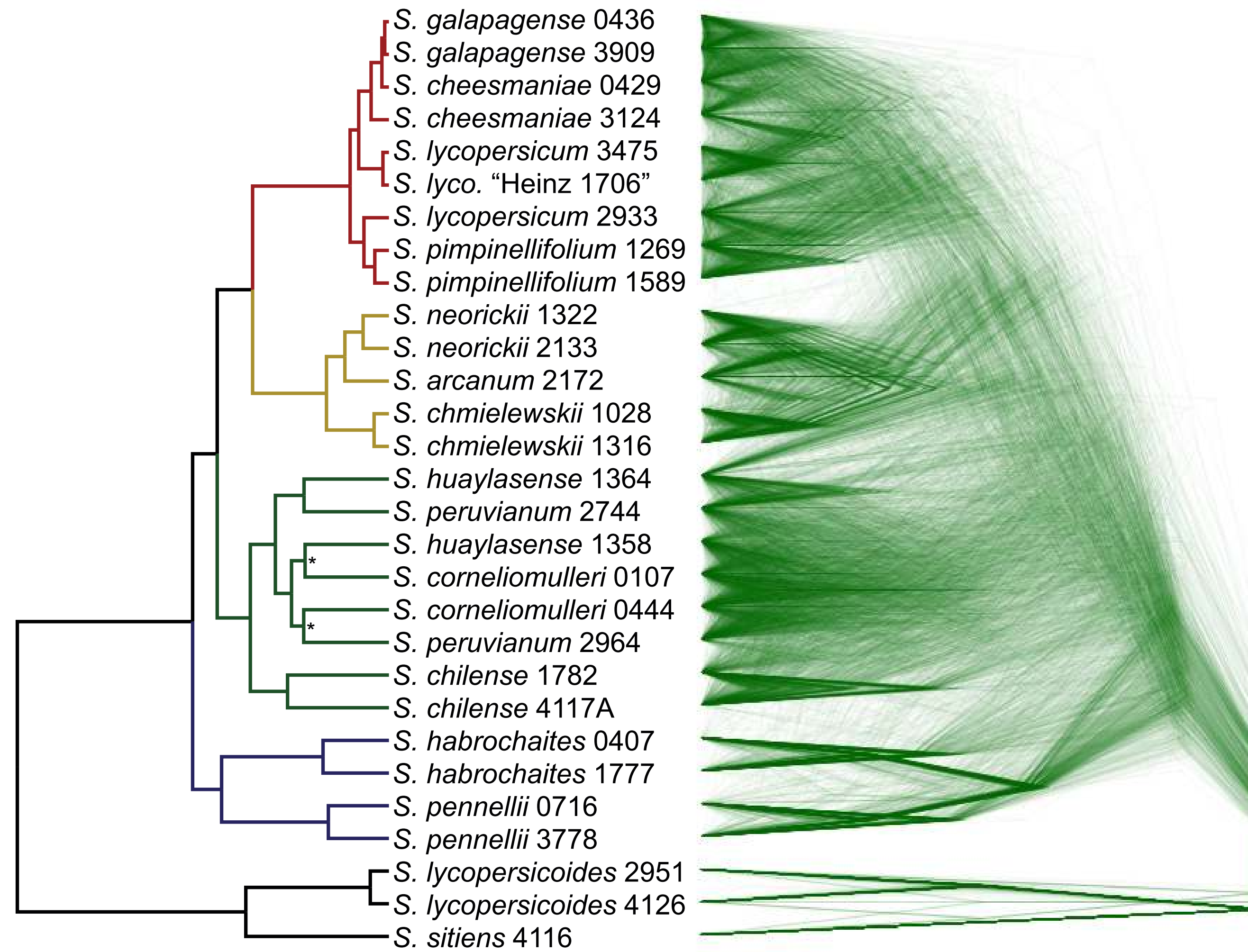




Hobolth et al. (2007)

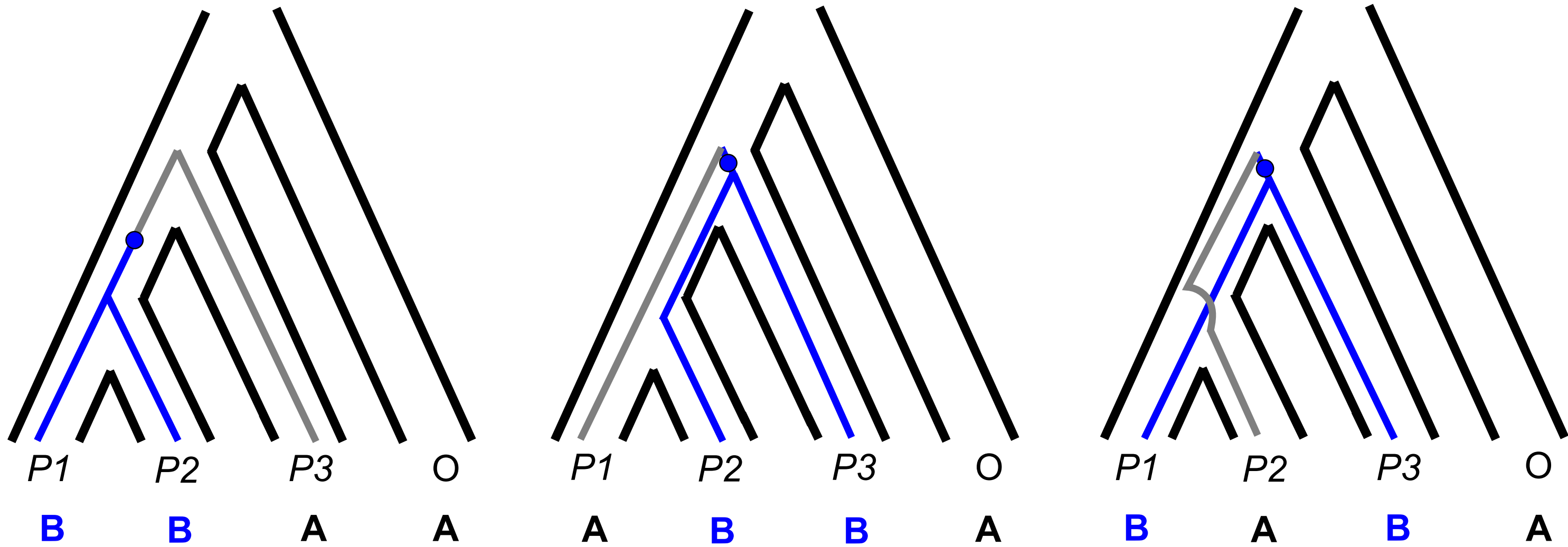


Degnan and Rosenberg (2009)



Pease et al. (2016)

ILS only:



ILS + introgression:

