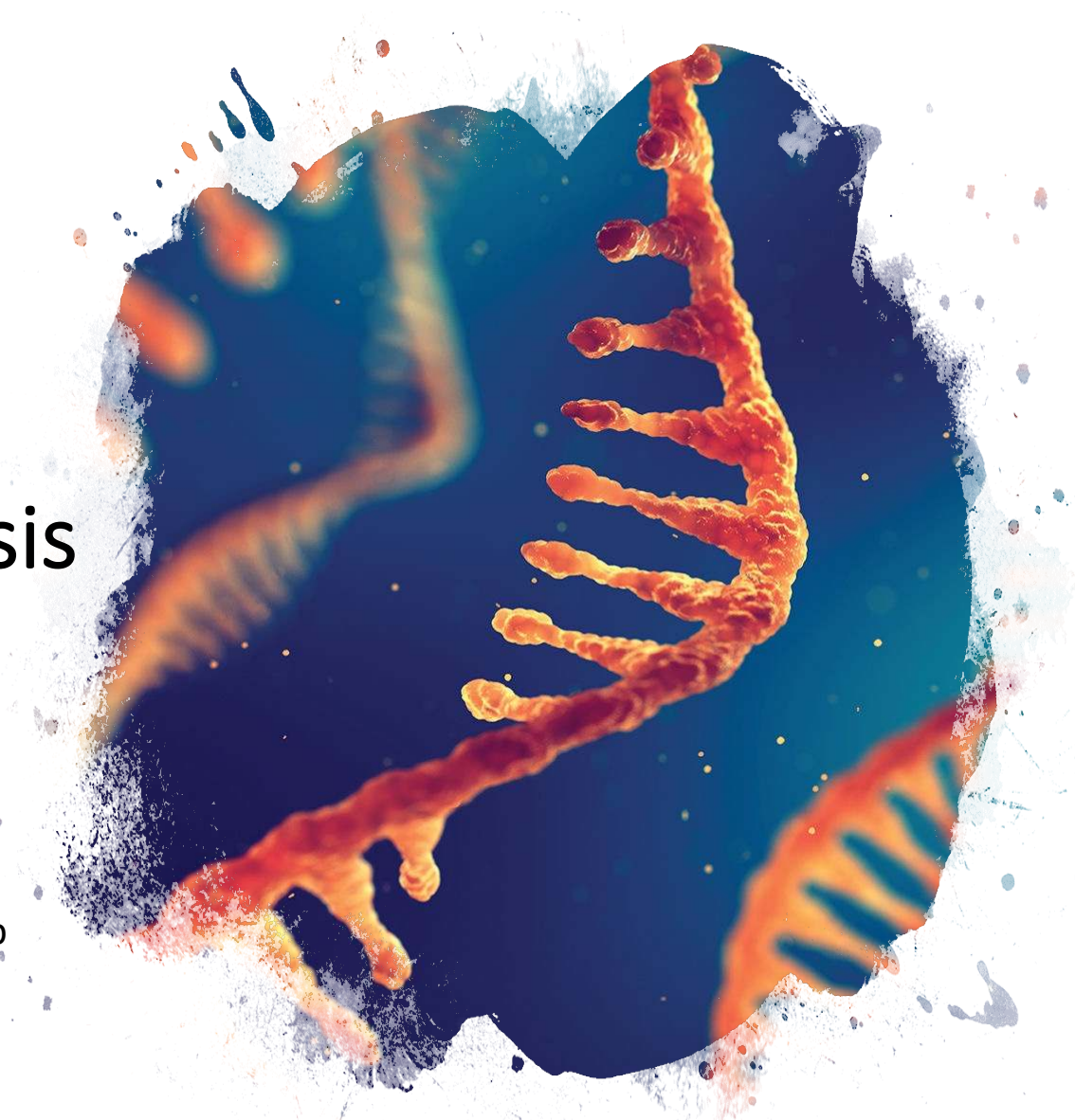


# Differential gene expression analysis

2023 Workshop on Genomics,  
Česky Krumlov

Rachel Steward  
Postdoctoral researcher, Runemark Lab  
Lund University



# Today's activity

7:00 - 7:30 : Differential expression background

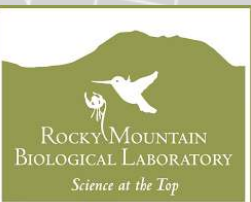
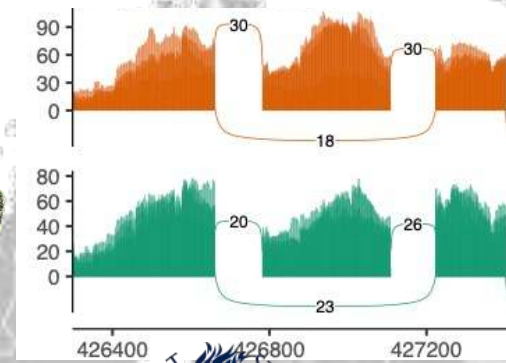
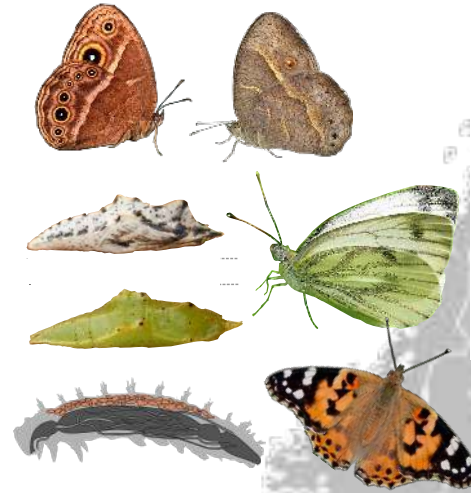
7:30 – 8:30 : Free work time  
(take a break when you need/want it)

8:30 – 8:45 : Check-in, walk through some preliminary results

8:45 – 9:30 : Free work time  
(take a break when you need/want it)

9:30 – 10 : Wrap-up and discussion

# About me



# Lecture outline

## 1. Ref-based differential expression overview

✓ [Basic Statistics](#)

✗ [Per base sequence quality](#)

! [Per tile sequence quality](#)

## 2. Trimming, mapping, counting

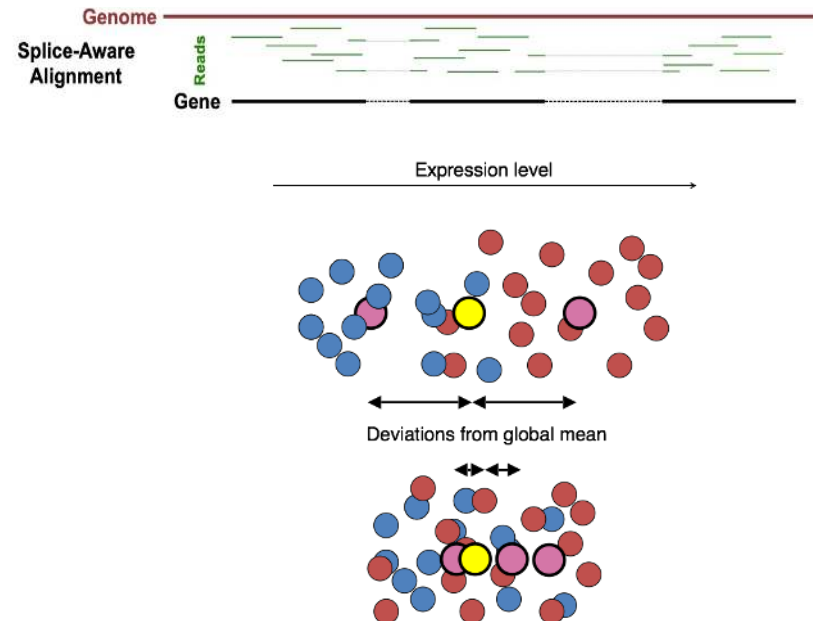
## 3. Differential expression analysis

a. Normalization

b. Dispersion estimates

c. Model fitting

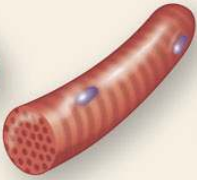
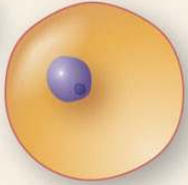
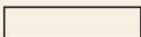
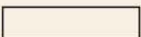
d. Hypothesis testing & output



# Gene expression

The selective activity of certain genes is a highly regulated process called gene expression.

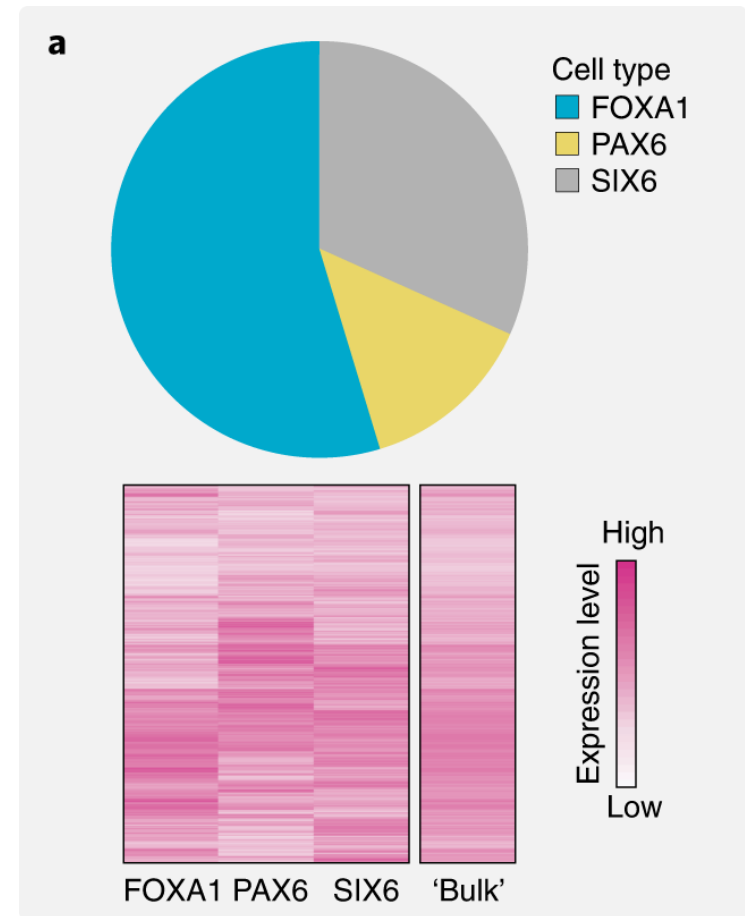
Gene expression is a characteristic of space (e.g., cell type, tissue, etc.) and time (e.g., developmental stage, time after event)

| Cell type    | Red blood                                                                           | Muscle                                                                              | Pancreatic                                                                          |
|--------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|
|              |  |  |  |
| Gene type    |                                                                                     |                                                                                     |                                                                                     |
| Housekeeping |  |  |  |
| Hemoglobin   |  |  |  |
| Insulin      |  |  |  |
| Myosin       |  |  |  |

# Gene expression

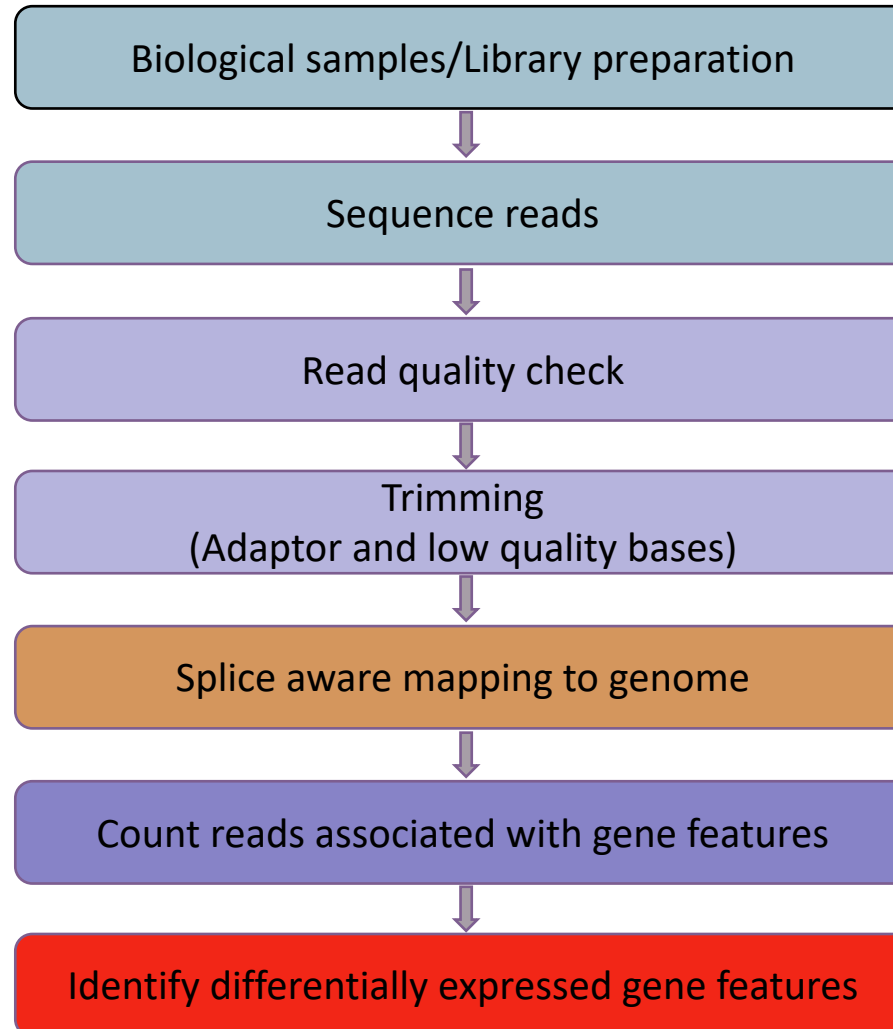
The selective activity of certain genes is a highly regulated process called gene expression.

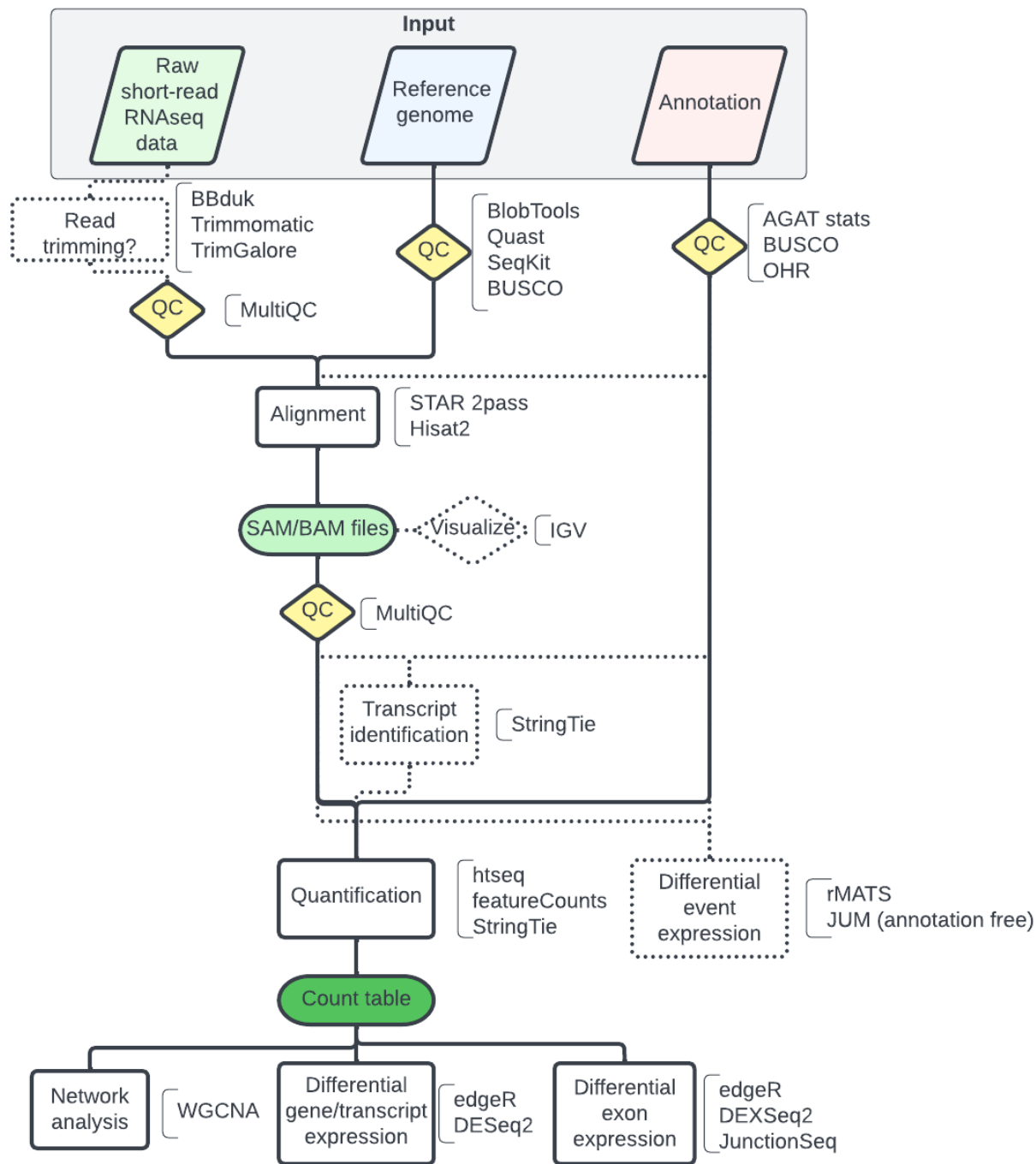
**Gene expression is a characteristic of space (e.g., cell type, tissue, etc.) and time (e.g., developmental stage, time after event)**

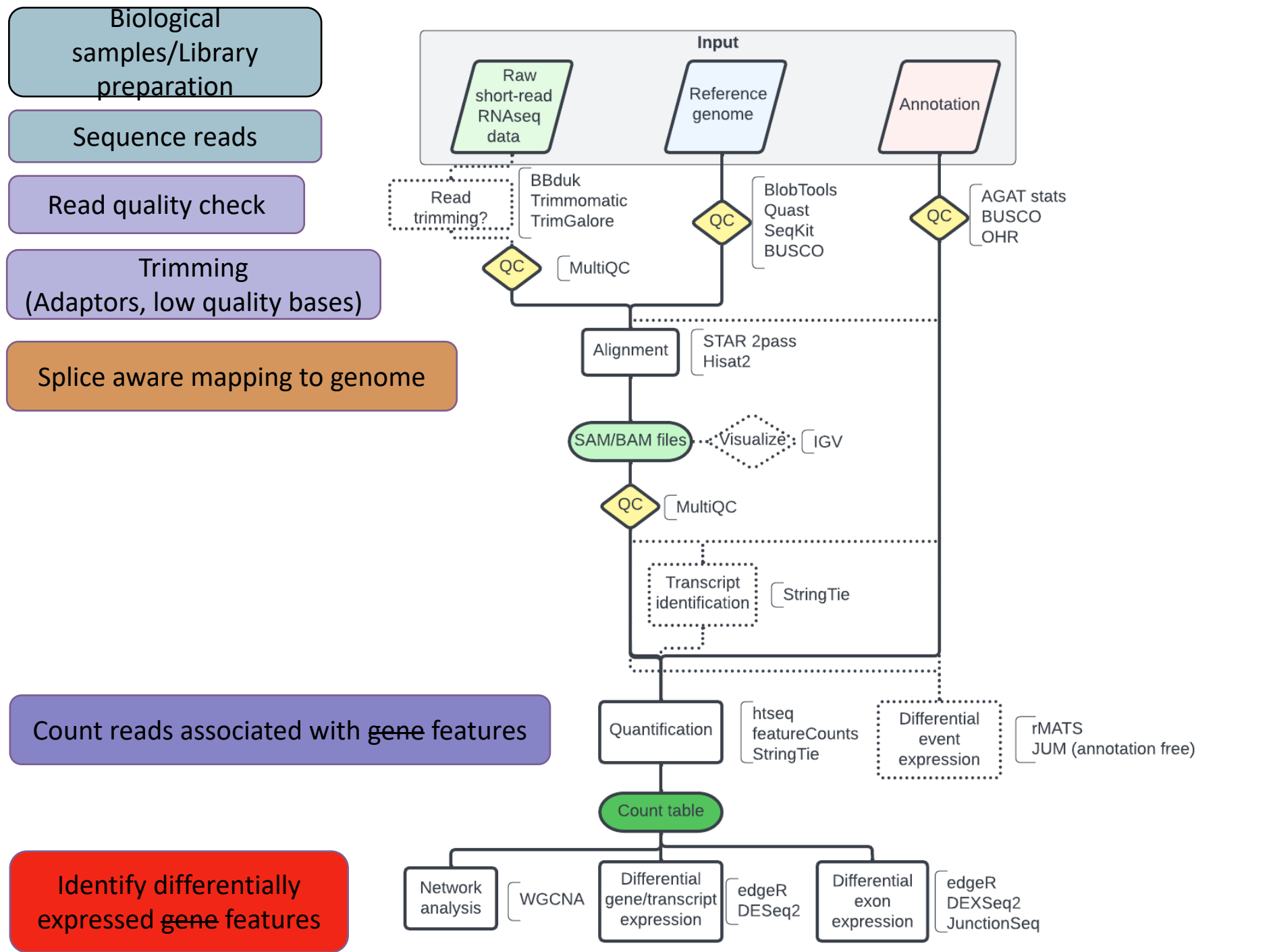


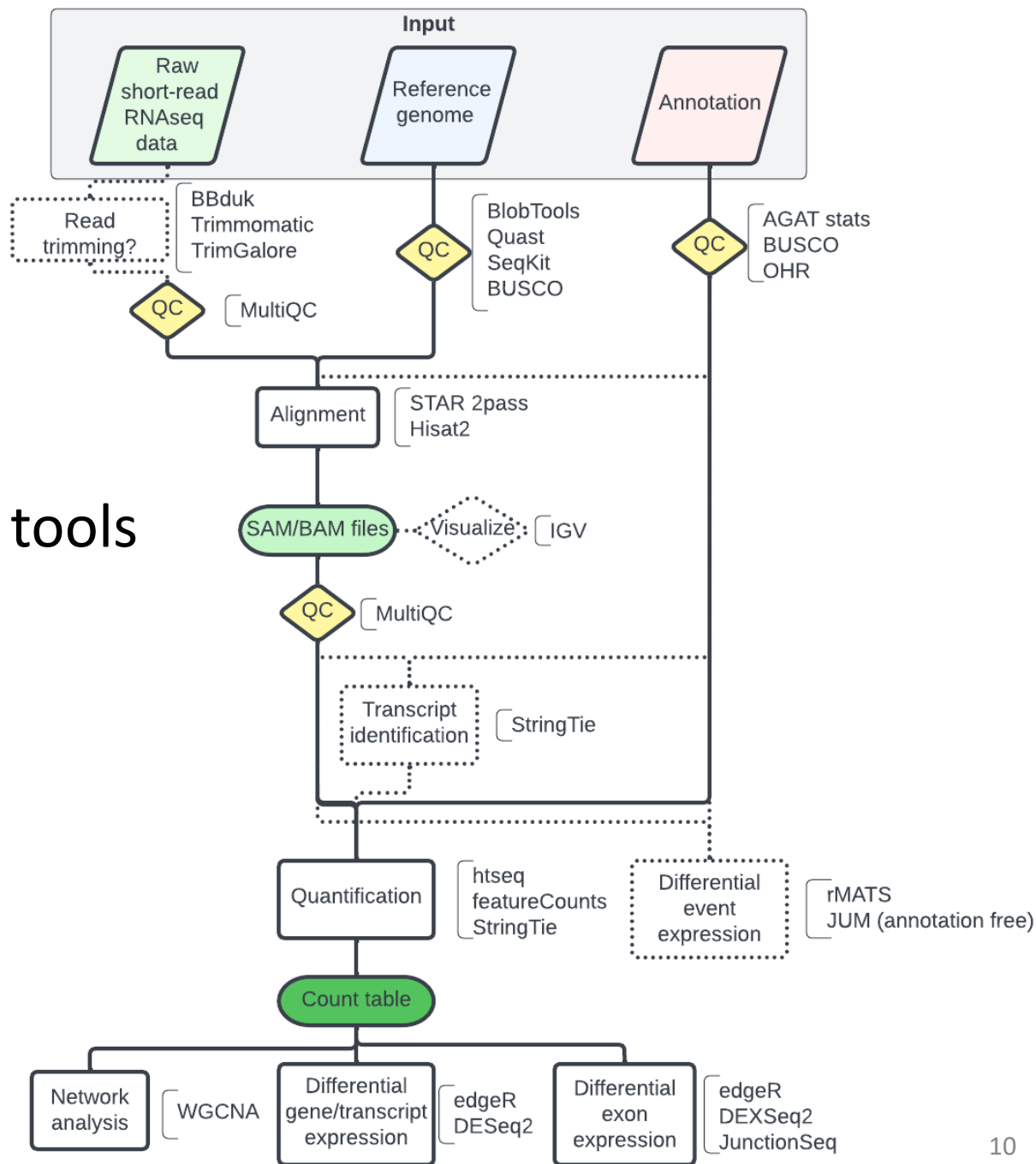
Price et al. 2022. Nature Ecology and Evolution

# (Ref-based) DGE workflow



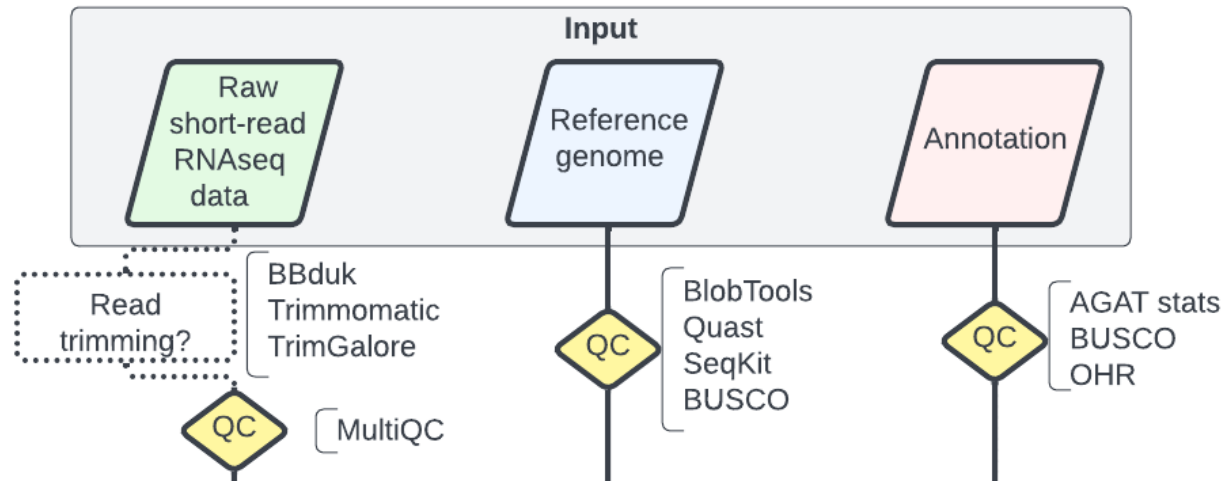






Combinations of tools  
can matter.

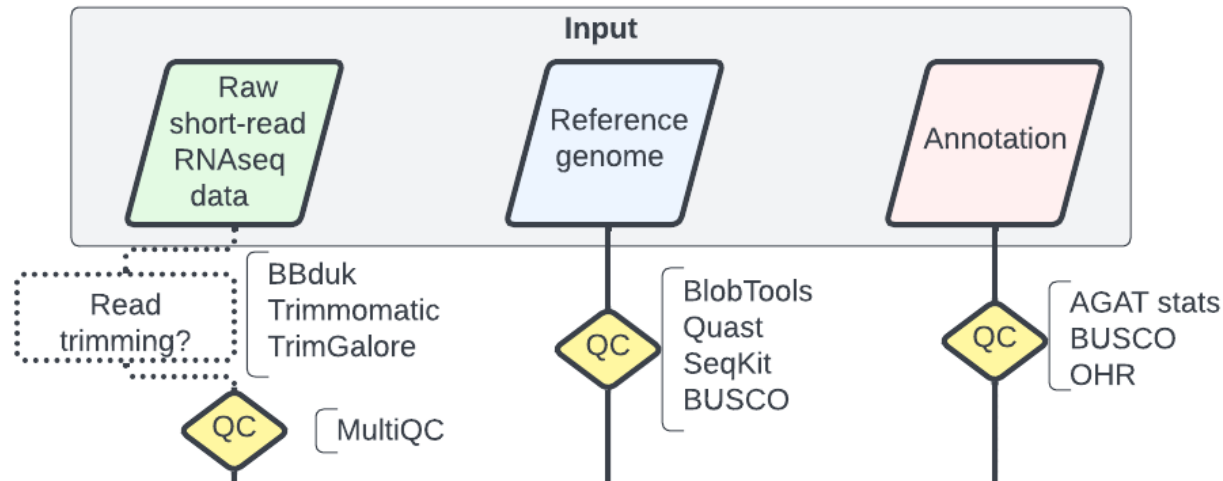
# Quality control



## Reads: To trim or not to trim?

- genome annotation, variant calling, transcriptome assembly : Trim!
- Anything else, maybe trim lightly?
  - adapters + low quality score (Q10-15)

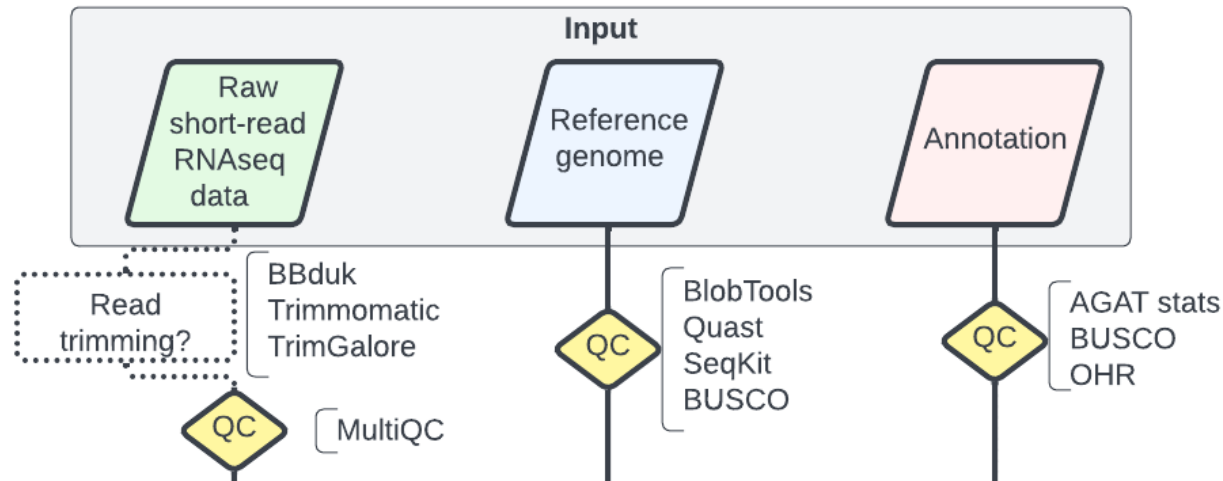
# Quality control



## Reference genome considerations:

- What maps where:
  - Recent duplications?
  - Highly repetitive content?
  - Missing content?

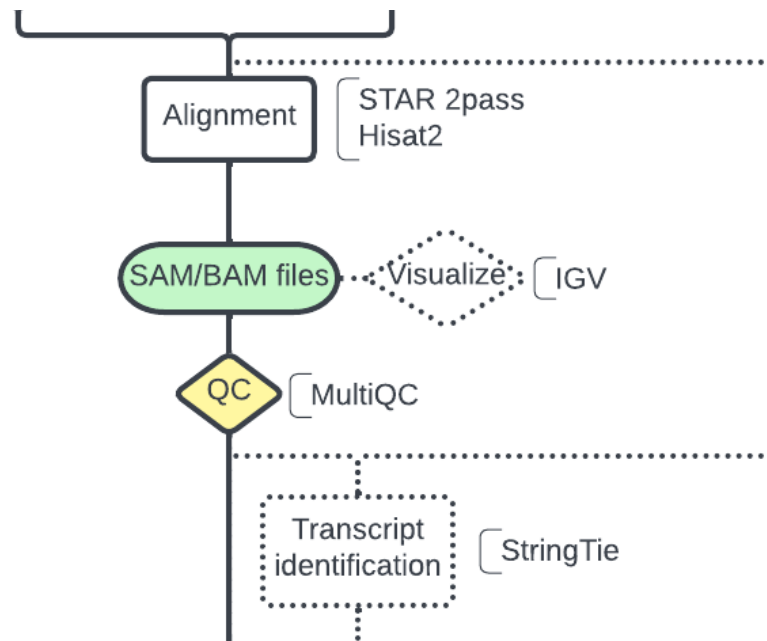
# Quality control



## Annotation considerations:

- What features have been annotated?
- Was RNAseq data used in the annotation?
  - *What* RNA? Life stage? Sex?
- In the lab, we use a protein-based BRAKER2 annotation

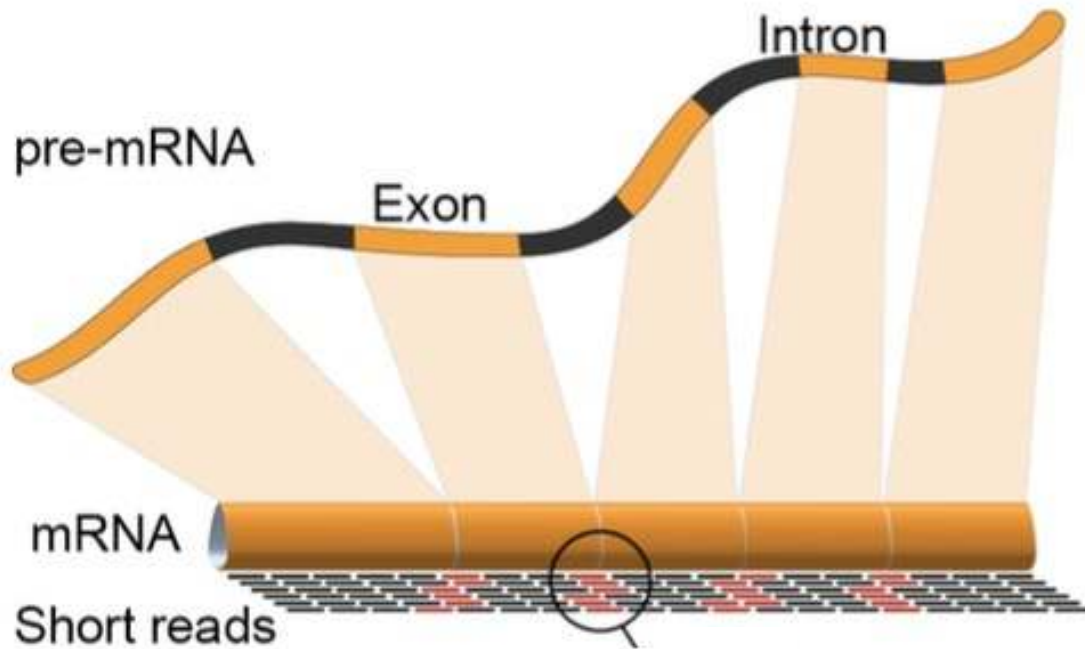
# Sequence alignment



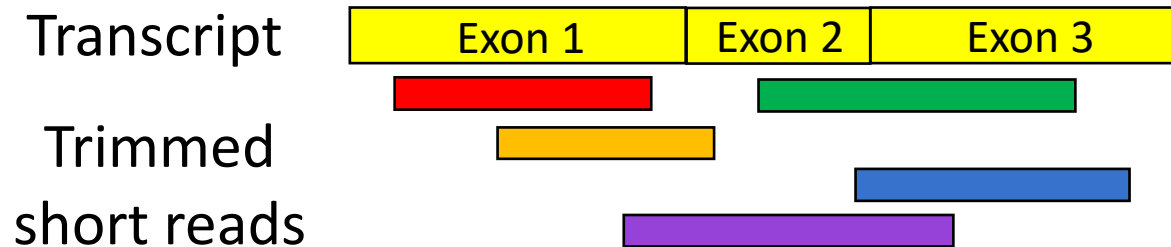
What are some challenges when aligning RNA-seq reads to the reference genome?

# Sequence alignment

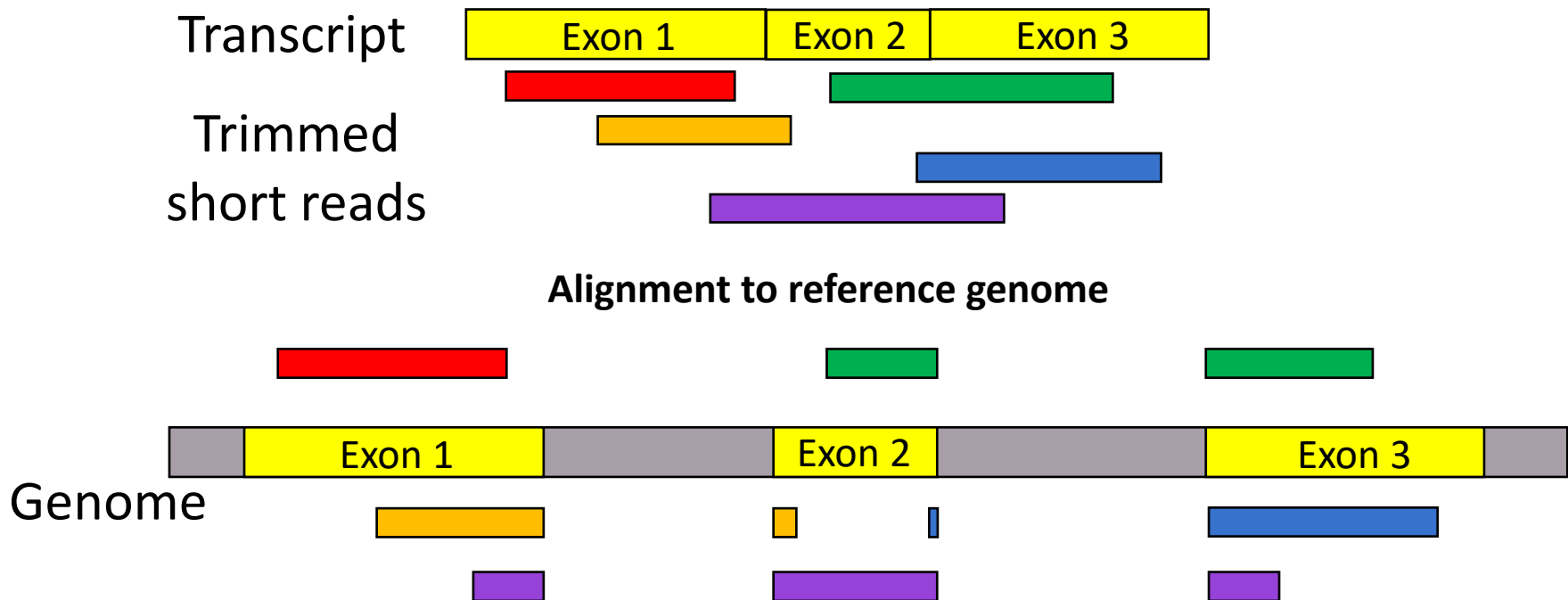
What are some challenges when aligning RNA-seq reads to the reference genome?



# Splice-aware sequence alignment



# Splice-aware sequence alignment

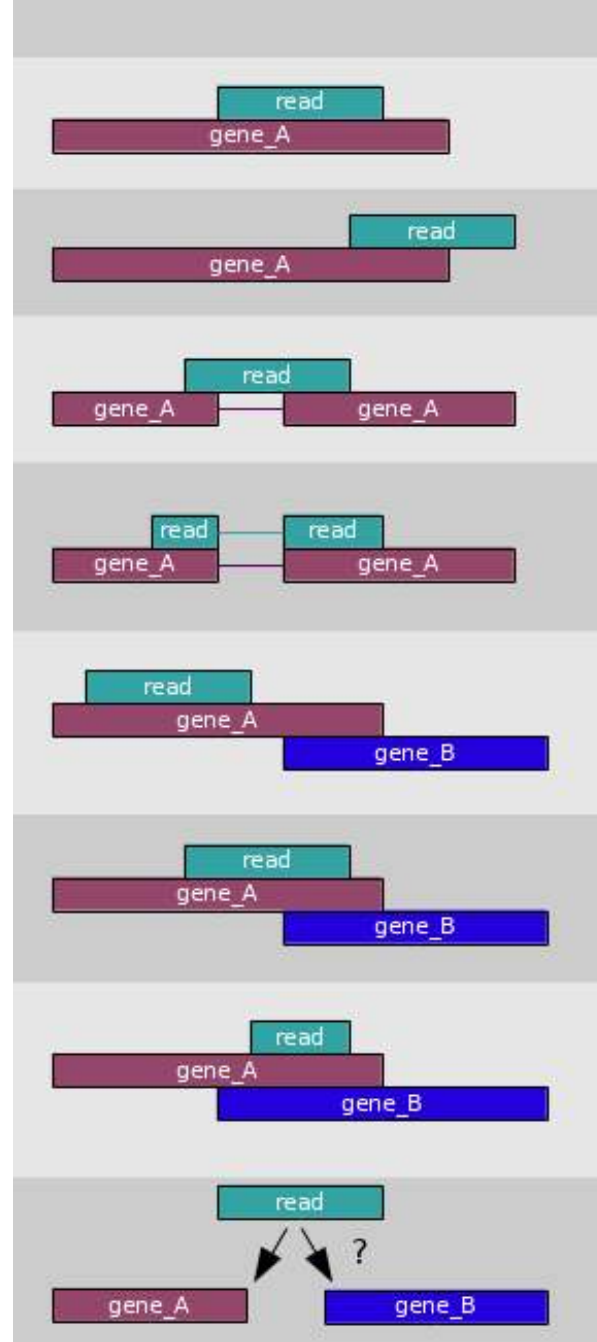


# Counting reads as a measure of expression

- Now we have our reads aligned to the genome, the next step is to count how many reads have been mapped to each features or metafeature.
- Two common counting tools are **featureCounts** and **htseq-count**.
- Total read count associated with a gene (*meta-feature*) = the sum of reads associated with each of the exons (*feature*) that "belong" to that gene.

```
genomics@ip-172-31-11-182: [~/workshop_materials/differential_expression/refs]$ head Pca_annotation.gtf
LG1    AUGUSTUS    transcript  22193    24413    .    -    .    transcript_id "Polcal_g1.t1"; gene_id "Polcal_g1";
LG1    AUGUSTUS    exon      22193    22320    .    -    .    transcript_id "Polcal_g1.t1"; gene_id "Polcal_g1";
LG1    AUGUSTUS    exon      23838    24048    .    -    .    transcript_id "Polcal_g1.t1"; gene_id "Polcal_g1";
LG1    AUGUSTUS    exon      24390    24413    .    -    .    transcript_id "Polcal_g1.t1"; gene_id "Polcal_g1";
LG1    AUGUSTUS    CDS       22193    22320    .    -    2    transcript_id "Polcal_g1.t1"; gene_id "Polcal_g1";
LG1    AUGUSTUS    CDS       23838    24048    .    -    0    transcript_id "Polcal_g1.t1"; gene_id "Polcal_g1";
LG1    AUGUSTUS    CDS       24390    24413    .    -    0    transcript_id "Polcal_g1.t1"; gene_id "Polcal_g1";
LG1    AUGUSTUS    transcript  79912    80136    .    -    .    transcript_id "Polcal_g2.t1"; gene_id "Polcal_g2";
LG1    AUGUSTUS    exon      79912    80136    .    -    .    transcript_id "Polcal_g2.t1"; gene_id "Polcal_g2";
LG1    AUGUSTUS    CDS       79912    80136    .    -    0    transcript_id "Polcal_g2.t1"; gene_id "Polcal_g2";
genomics@ip-172-31-11-182: [~/workshop_materials/differential_expression/refs]$
```

# What should count??



**Output of counting = A count matrix, with genes as rows and samples as columns**

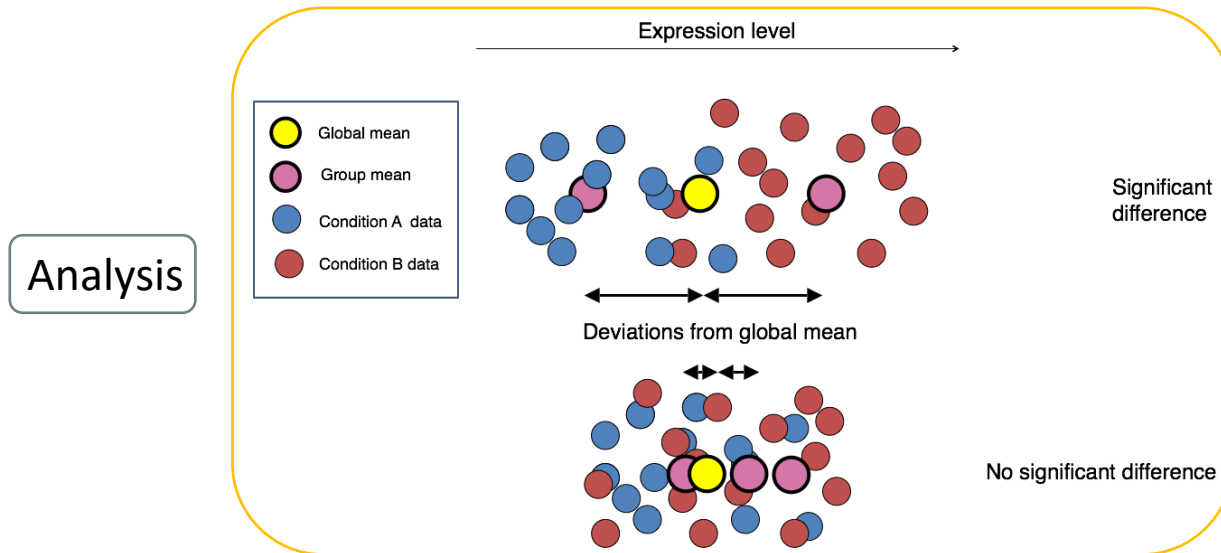
These are the “**raw**” counts and will be used in the downstream statistical program for differential gene expression.

Each column is a sample

Each row is a gene

| GENE ID     | KD.2 | KD.3 | OE.1 | OE.2 | OE.3 | IR.1 | IR.2 | IR.3 |
|-------------|------|------|------|------|------|------|------|------|
| 1/2-SBSRNA4 | 57   | 41   | 64   | 55   | 38   | 45   | 31   | 39   |
| A1BG        | 71   | 40   | 100  | 81   | 41   | 77   | 58   | 40   |
| A1BG-AS1    | 256  | 177  | 220  | 189  | 107  | 213  | 172  | 126  |
| A1CF        | 0    | 1    | 1    | 0    | 0    | 0    | 0    | 0    |
| A2LD1       | 146  | 81   | 138  | 125  | 52   | 91   | 80   | 50   |
| A2M         | 10   | 9    | 2    | 5    | 2    | 9    | 8    | 4    |
| A2ML1       | 3    | 2    | 6    | 5    | 2    | 2    | 1    | 0    |
| A2MP1       | 0    | 0    | 2    | 1    | 3    | 0    | 2    | 1    |
| A4GALT      | 56   | 37   | 107  | 118  | 65   | 49   | 52   | 37   |
| A4GNT       | 0    | 0    | 0    | 0    | 1    | 0    | 0    | 0    |
| AA06        | 0    | 0    | 0    | 0    | 0    | 0    | 0    | 0    |
| AAA1        | 0    | 0    | 1    | 0    | 0    | 0    | 0    | 0    |
| AAAS        | 2288 | 1363 | 1753 | 1727 | 835  | 1672 | 1389 | 1121 |
| AACS        | 1586 | 923  | 951  | 967  | 484  | 938  | 771  | 635  |
| AACSP1      | 1    | 1    | 3    | 0    | 1    | 1    | 1    | 3    |
| AADAC       | 0    | 0    | 0    | 0    | 0    | 0    | 0    | 0    |
| AADACL2     | 0    | 0    | 0    | 0    | 0    | 0    | 0    | 0    |
| AADACL3     | 0    | 0    | 0    | 0    | 0    | 0    | 0    | 0    |
| AADACL4     | 0    | 0    | 1    | 1    | 0    | 0    | 0    | 0    |
| AADAT       | 856  | 539  | 593  | 576  | 359  | 567  | 521  | 416  |
| AAGAB       | 4648 | 2550 | 2648 | 2356 | 1481 | 3265 | 2790 | 2118 |
| AAK1        | 2310 | 1384 | 1869 | 1602 | 980  | 1675 | 1614 | 1108 |
| AAMP        | 5198 | 3081 | 3179 | 3137 | 1721 | 4061 | 3304 | 2623 |
| AANAT       | 7    | 7    | 12   | 12   | 4    | 6    | 2    | 7    |
| AARS        | 5570 | 3323 | 4782 | 4580 | 2473 | 3953 | 3339 | 2666 |

# Differential expression analysis



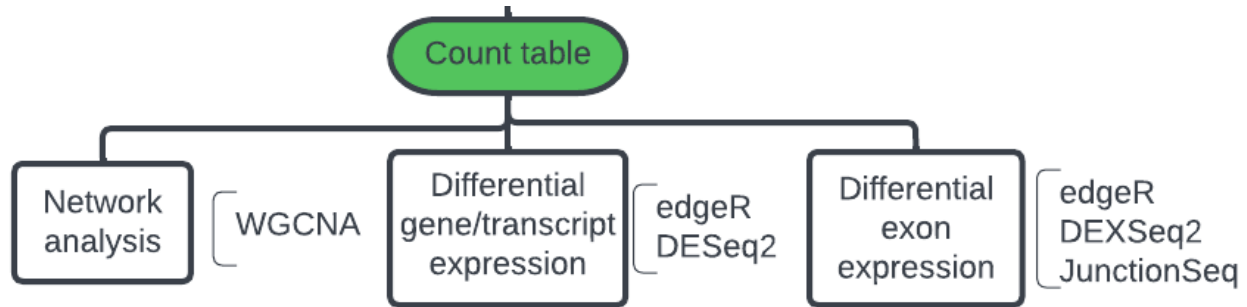
features (e.g. genes)

samples: want to see if differences across condition are significant

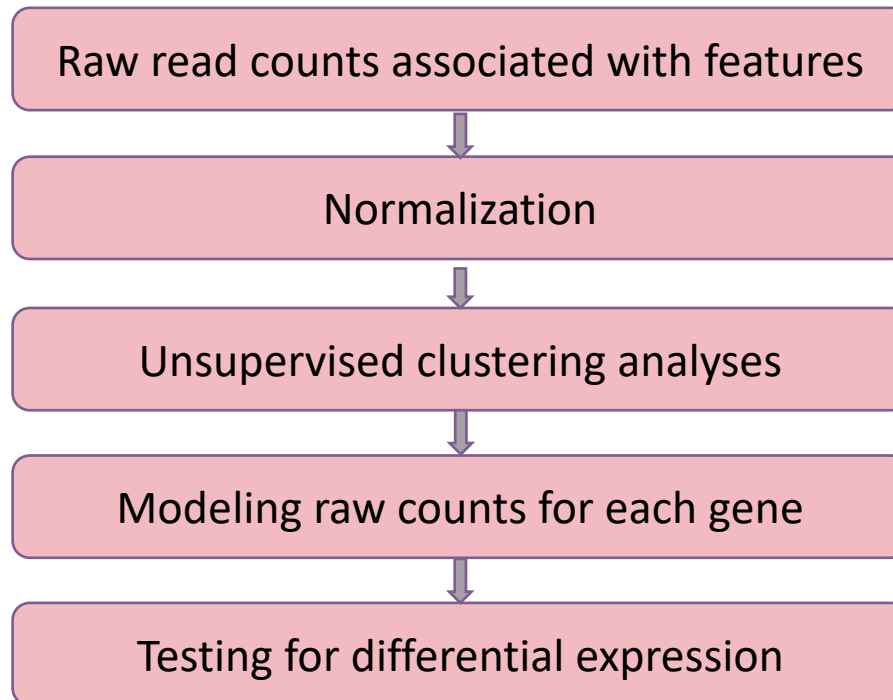
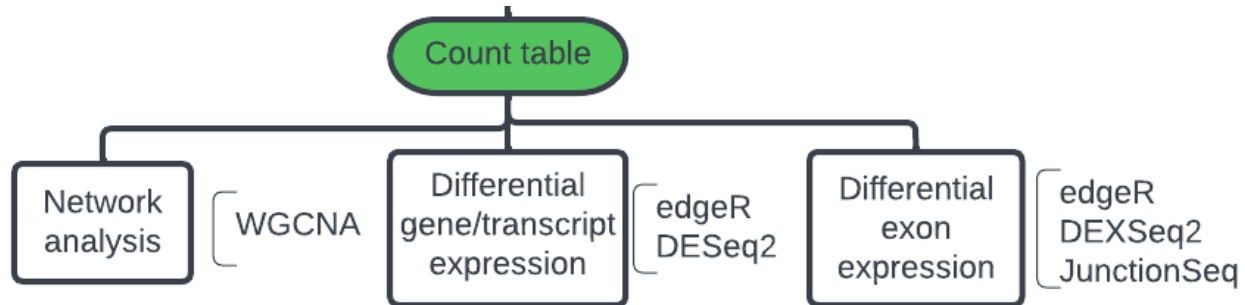
**Input**

| Gene_id   | S1 | S2 | S3 | S4 | S5 | S6 |
|-----------|----|----|----|----|----|----|
| Polcal_g1 | 17 | 10 | 5  | 23 | 10 | 6  |
| Polcal_g2 | 0  | 1  | 0  | 1  | 2  | 1  |
| Polcal_g3 | 7  | 0  | 2  | 7  | 4  | 0  |
| Polcal_g4 | 17 | 11 | 5  | 21 | 10 | 12 |

# Differential expression analysis



# Differential expression analysis



# DESeq2 package

METHOD | [Open Access](#) | [Published: 05 December 2014](#)

## **Moderated estimation of fold change and dispersion for RNA-seq data with DESeq2**

[Michael I Love](#), [Wolfgang Huber](#) & [Simon Anders](#) 

[Genome Biology](#) **15**, Article number: 550 (2014) | [Cite this article](#)

**450k** Accesses | **34853** Citations | **131** Altmetric | [Metrics](#)

# Normalization

- **Normalization is NOT** fitting a normal distribution or transforming data transformation.
- **Normalization aims to** identify the nature and magnitude of **systematic biases**, and take them into account in our model-based analysis of the data.

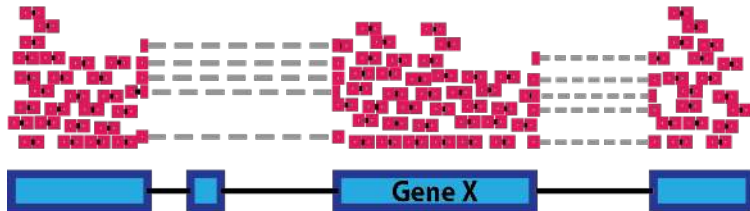
The main factors often considered during normalization are:

- Sequencing depth
- RNA composition
- Gene length (some methods)

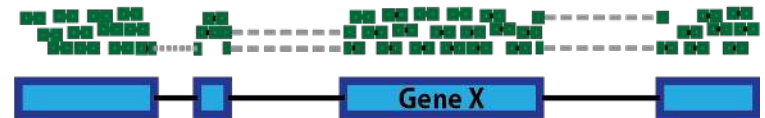
# Normalization

## Sequencing depth

Sample A Reads



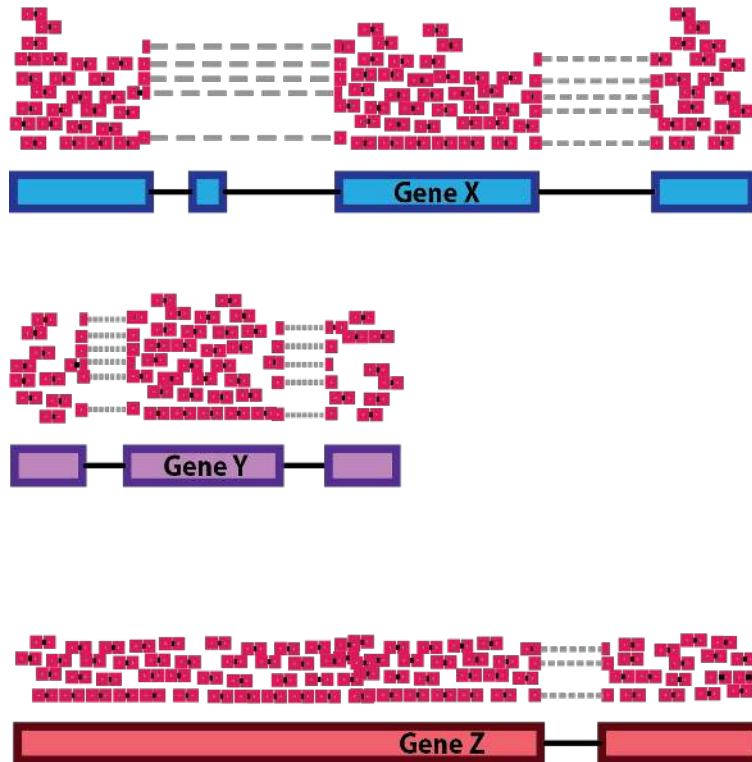
Sample B Reads



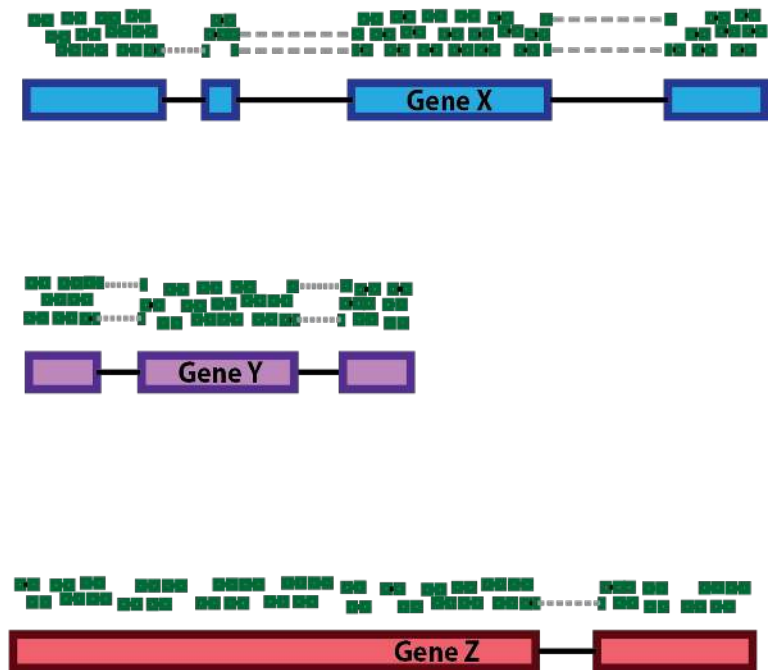
# Normalization

## Sequencing depth

Sample A Reads



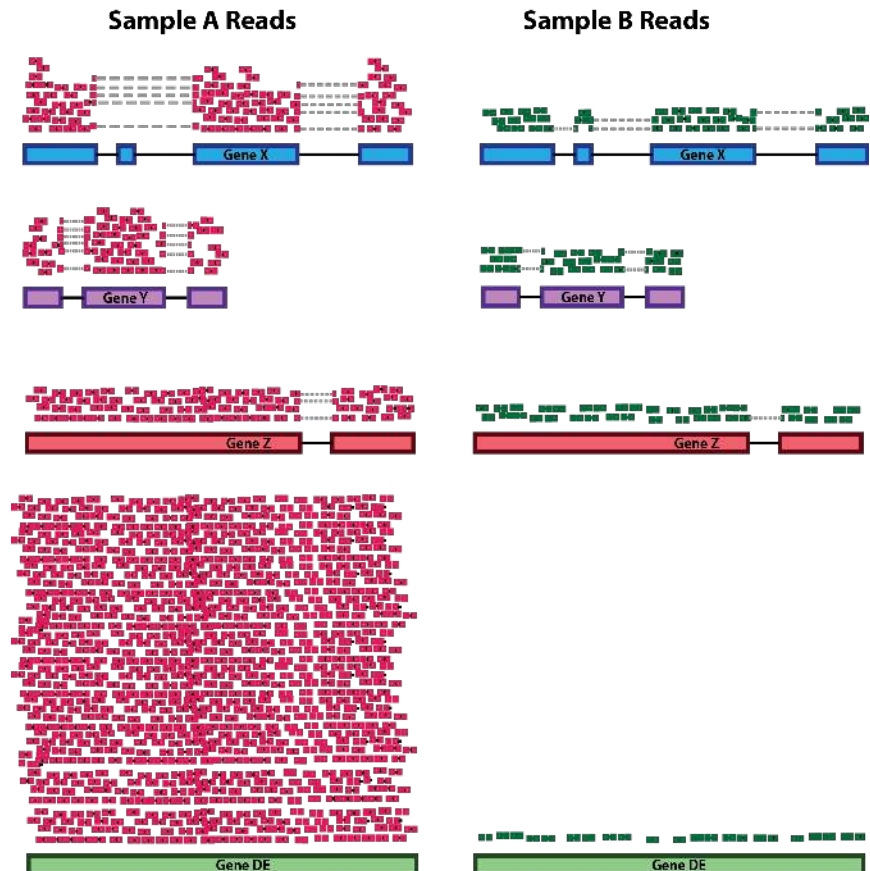
Sample B Reads



# Normalization

## RNA composition

- A few highly differentially expressed genes
- Can skew some normalization methods



# Median of ratios (MRN) normalization

- Used by DESeq2 (DGE analysis tool we will use today)

Let's see how the normalization works...

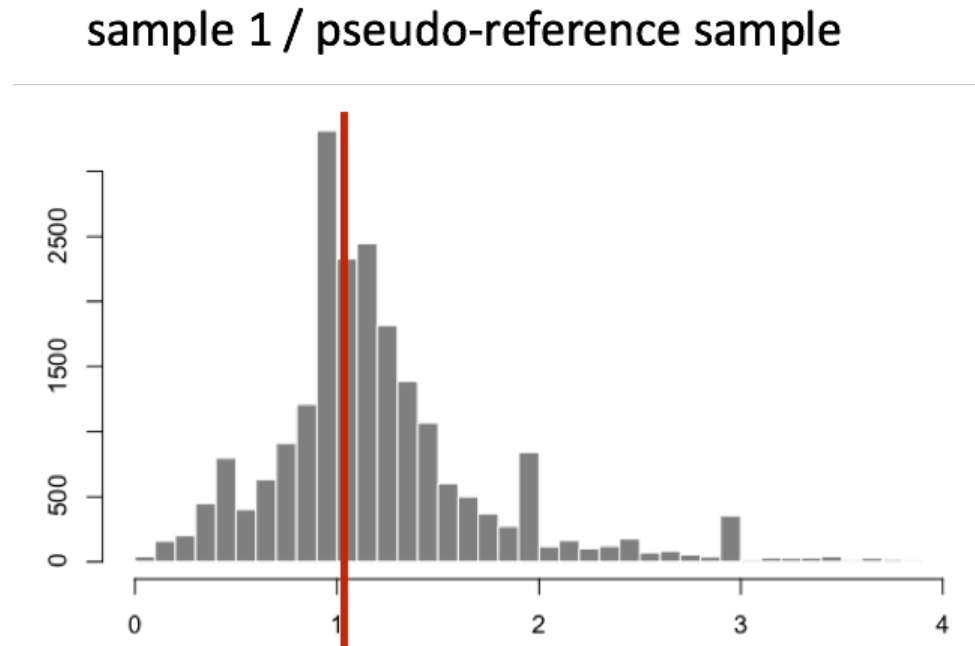
**Step 1. Create a pseudo-reference sample for each gene (row-wise geometric mean)**

| Gene  | sampleA | sampleB | Pseudo-reference sample           |
|-------|---------|---------|-----------------------------------|
| EF2A  | 1489    | 906     | $\sqrt{1489 \times 906} = 1161.5$ |
| ABCD1 | 22      | 13      | $\sqrt{22 \times 13} = 16.9$      |
| ...   | ...     | ...     | ...                               |

**Step 2. Calculates ratio of each sample to the reference**

| Gene  | sampleA | sampleB | Pseudo-reference sample | Ratio of sampleA/ref | Ratio of sampleB/ref |
|-------|---------|---------|-------------------------|----------------------|----------------------|
| EF2A  | 1489    | 906     | 1161.5                  | $1489/1161.5 = 1.28$ | $906/1161.5 = 0.78$  |
| ABCD1 | 22      | 13      | 16.9                    | $22/16.9 = 1.30$     | $13/16.9 = 0.77$     |
| MEFV  | 793     | 410     | 570.2                   | $793/570.2 = 1.39$   | $410/570.2 = 0.72$   |
| ...   | ...     | ...     | ...                     | ...                  | ...                  |

The figure below illustrates the median value for the distribution of all gene ratios for a single sample (frequency is on the y-axis).



The median of ratio methods makes the assumption that not ALL genes are differentially expressed; therefore, the normalization factors should account for sequencing depth and RNA composition of the sample (large outlier genes will not represent the median ratio values).

### Step 3. Calculate the normalization factor for each sample (size factor)

| Gene  | sampleA | sampleB | Pseudo-reference sample | Ratio of sampleA/ref | Ratio of sampleB/ref |
|-------|---------|---------|-------------------------|----------------------|----------------------|
| EF2A  | 1489    | 906     | 1161.5                  | $1489/1161.5 = 1.28$ | $906/1161.5 = 0.78$  |
| ABCD1 | 22      | 13      | 16.9                    | $22/16.9 = 1.30$     | $13/16.9 = 0.77$     |
| MEFV  | 793     | 410     | 570.2                   | $793/570.2 = 1.39$   | $410/570.2 = 0.72$   |
| ...   | ...     | ...     | ...                     | ...                  | ...                  |

`median(c(1.28, 1.3, 1.39, 1.35, 0.59))`  
`=1.3`

`median(c(1.28, 1.3, 1.39, 1.35, 0.59))`  
`=1.3`

#### Step 4: calculate the normalized count values using the normalization factor

Raw counts:

| Gene  | sampleA | sampleB |
|-------|---------|---------|
| EF2A  | 1489    | 906     |
| ABCD1 | 22      | 13      |
| ...   | ...     | ...     |

Normalized counts

| Gene  | sampleA              | sampleB              |
|-------|----------------------|----------------------|
| EF2A  | $1489/1.3 = 1145.39$ | $906/0.77 = 1176.62$ |
| ABCD1 | $22/1.3 = 16.92$     | $13/0.77 = 16.88$    |
| ...   | ...                  | ...                  |

Normalized counts are not whole numbers!

# Modeling raw counts for each gene

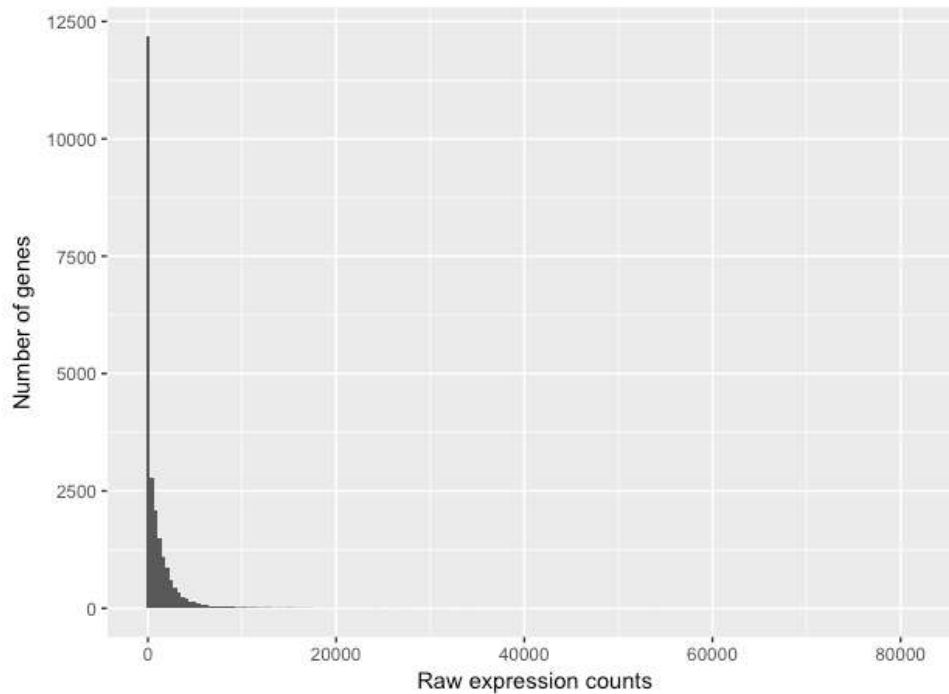
**Step 1. Normalization (aka estimation of size factors) → done!**

**Step 2. Estimate gene-wise **dispersion****

- To accurately model sequencing counts, we need to generate accurate estimates of **within-group variation** for each gene (aka dispersion)
  - need to choose the right distribution

# Properties of RNA-seq count data

The distribution of RNA-seq counts for a single sample looks as below:



**Low number of counts** associated with a large proportion of genes and a **long right tail** due to the lack of any upper limit for expression.

# Statistical modeling of count data

# Statistical modeling of count data

**Which probability distributions are suitable for modeling count data?**

Poisson distribution?

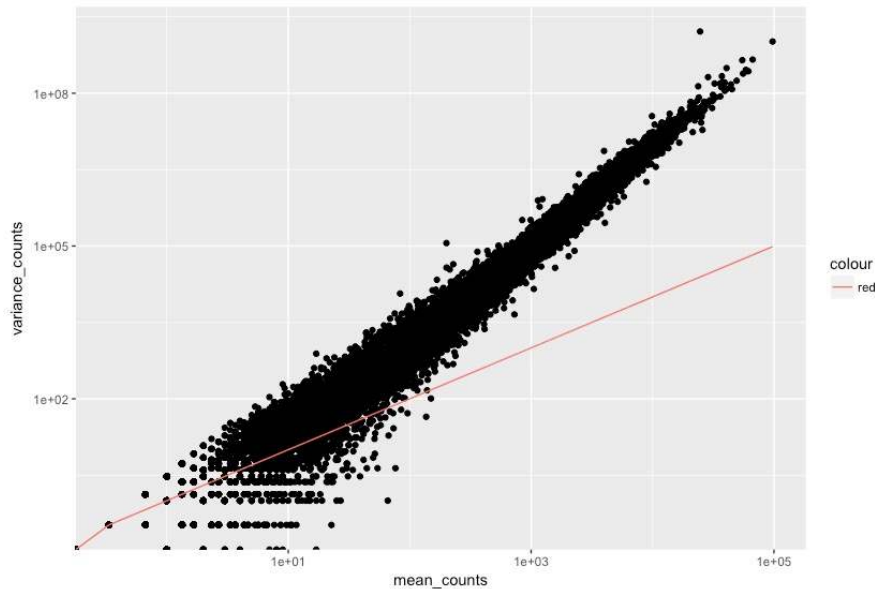
- Used when the number of cases is very large but the chance of a particular event is very low.
- **A property of Poission distribution is that the mean = variance.**

# Statistical modeling of count data

Which probability distributions are suitable for modeling count data?

Poisson distribution?

- Used when the number of cases is very large but the chance of a particular event is very low.
- **A property of Poisson distribution is that the mean = variance.**



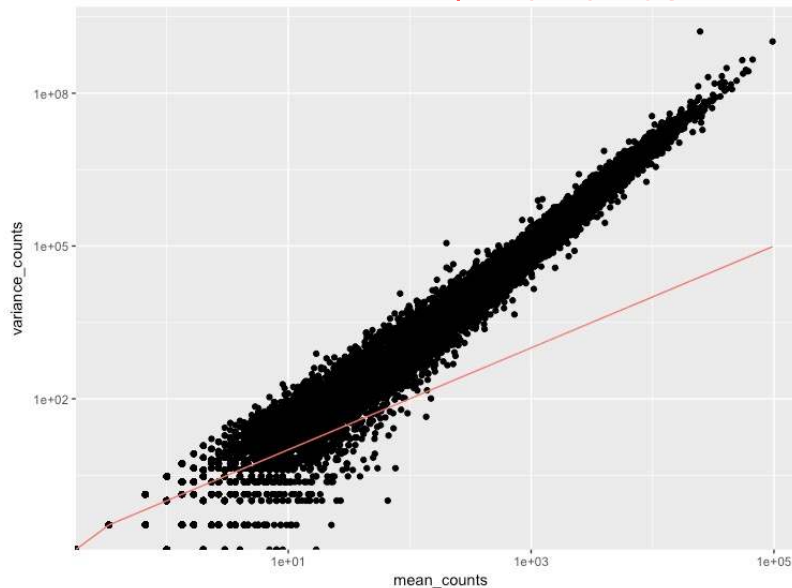
# Statistical modeling of count data

Which probability distributions are suitable for modeling count data?

Poisson distribution?

- Used when the number of cases is very large but the chance of a particular event is very low.
- **A property of Poisson distribution is that the mean = variance.**

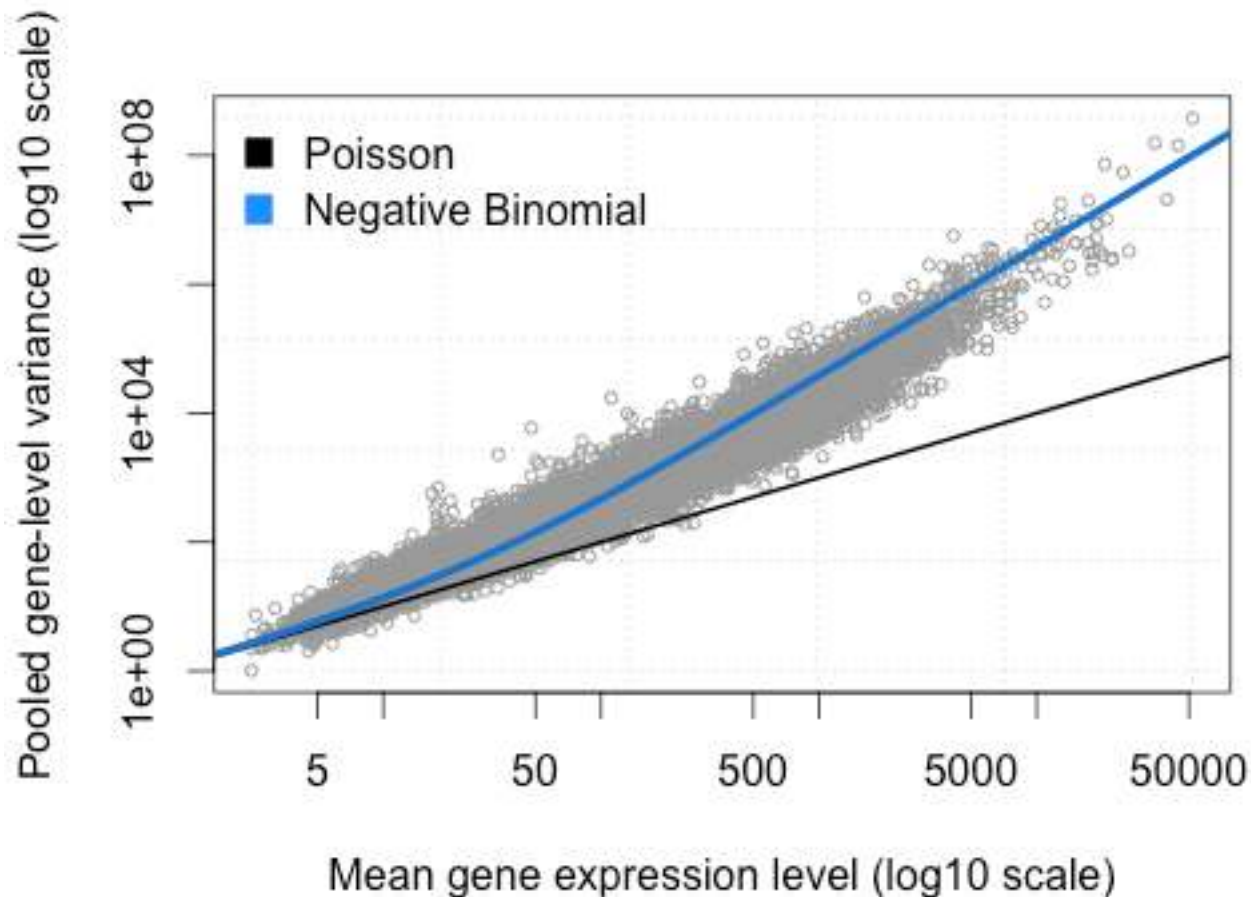
**mean  $\neq$  variance**



**Poisson distribution is not suitable to model count data across the biological samples.**

The distribution that fits best is the **Negative Binomial (NB)** distribution.

- two parameters, one for the mean and one for the variance
- flexibility to estimate the amount of dispersion for each gene across samples.

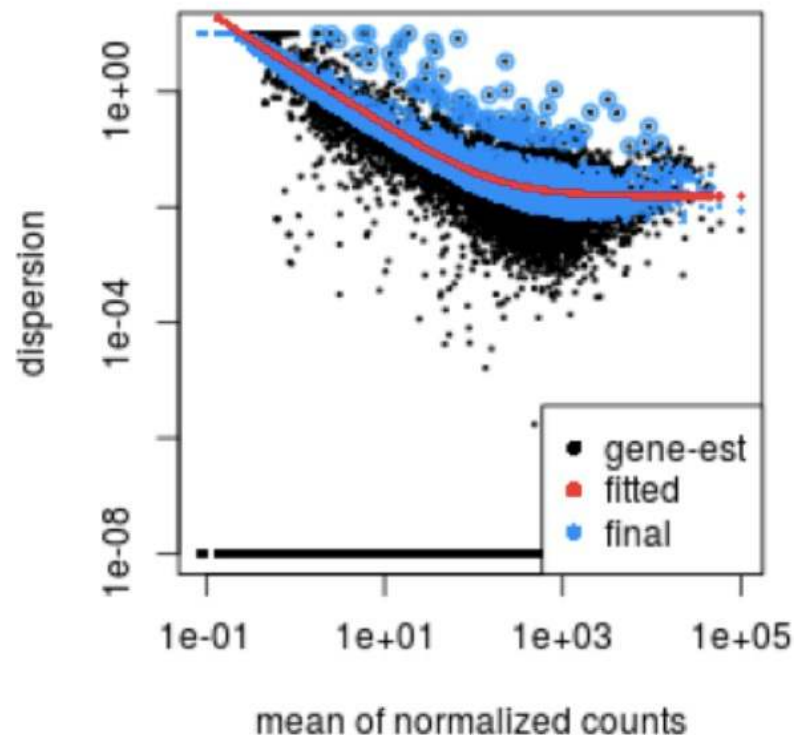


## How does the dispersion relate to our model?

- the **estimates of variation for each gene are often unreliable.**
- DESeq2 **shares information across genes** to generate more accurate estimates of variation : '**shrinkage**'.
  - assumes that genes with similar expression levels have similar dispersion.

### Step 3: Fit curve to gene-wise dispersion estimates

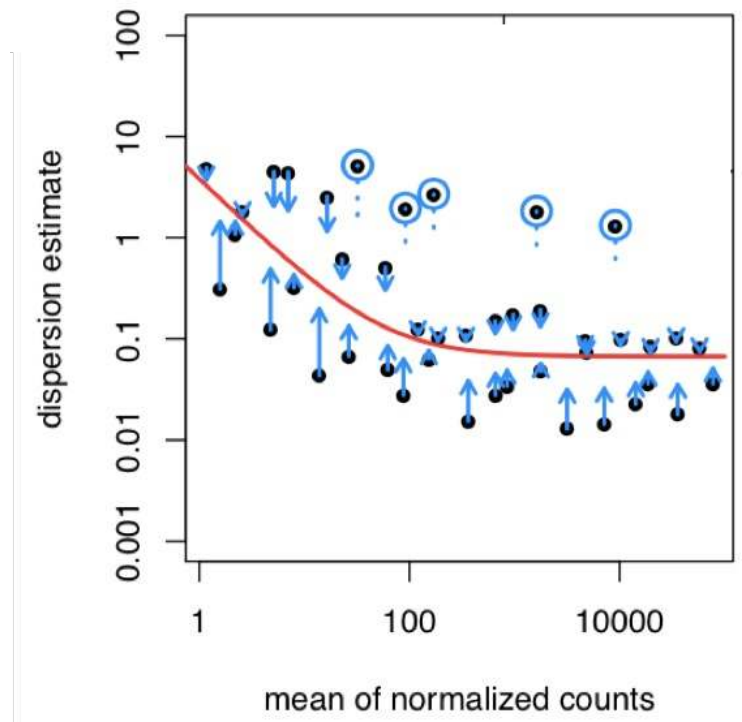
- Different genes will have different scales of biological variability
- However, we make the assumption that **DESeq2 assumes that genes with similar expression levels have similar dispersion.**
- **Fitted dispersion curve = expected dispersion for genes of a given level of expression (e.g., mean normalized count)**



## Step 4: Shrink dispersion estimates for each gene toward the values predicted by the curve

- Genes with low dispersion estimates are shrunk towards the curve
- Genes with high dispersion estimates do not follow model assumptions, and are their dispersion is not shrunk

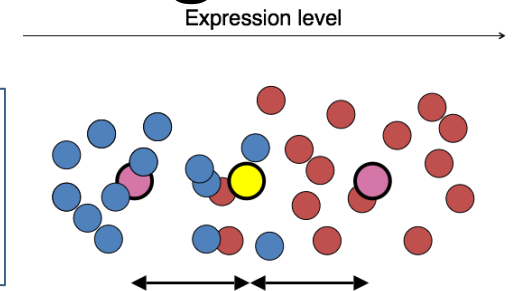
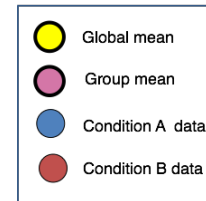
**This shrinkage method is particularly important to reduce false positives in the differential expression analysis.**



# Model fitting and hypothesis testing

**Blue:** base level group, control group

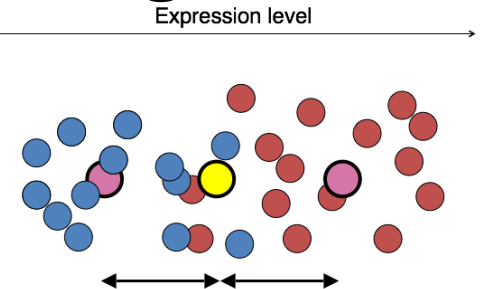
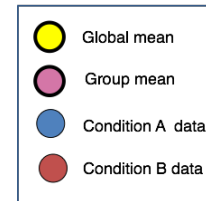
**Red:** treatment group



# Model fitting and hypothesis testing

**Blue:** base level group, control group

**Red:** treatment group



## Step 5. Generalized Linear Model fit for each gene

$$y = \beta_0 + x_1\beta_1$$

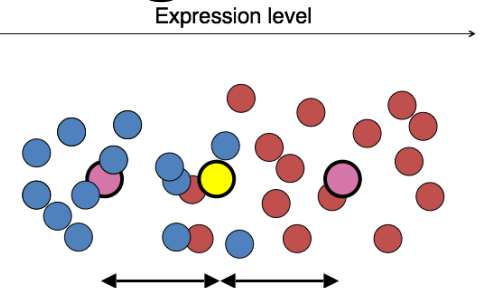
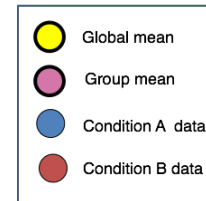
- $y$  = transformed **expression level**
- $\beta_0$  = **intercept** (the estimated expression for the base level group, expression in the **blue** group)
- $x_1$  = a binary indicator variable for (0 if part of the blue group, 1 if part of the **red** group)
- $\beta_1$  = coefficient for the treatment group (**red**)
  - represents the **difference** between **red** and **blue**

$$y = \beta_0 + \beta_1$$

# Model fitting and hypothesis testing

**Blue:** base level group, control group

**Red:** treatment group



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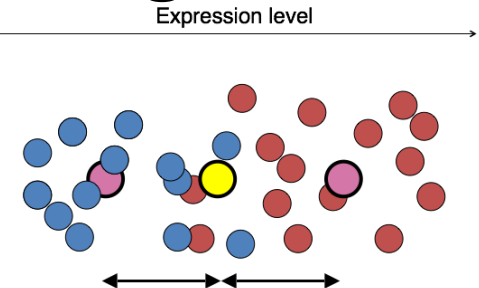
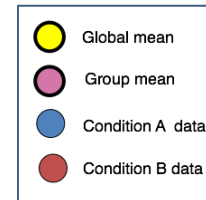


$$\beta_1 = y - \beta_0 = \log_2(\text{expression}_{\text{red}}) - \log_2(\text{expression}_{\text{blue}})$$

# Model fitting and hypothesis testing

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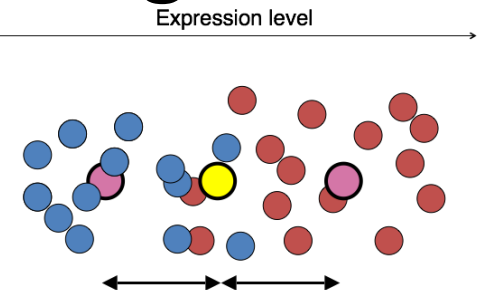
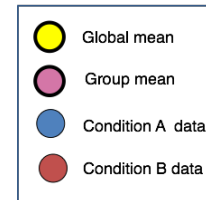


$$\begin{aligned}\beta_1 &= y - \beta_0 = \log_2(\text{expression}_{\text{red}}) - \log_2(\text{expression}_{\text{blue}}) \\ &= \frac{\log_2(\text{expression}_{\text{red}})}{\log_2(\text{expression}_{\text{blue}})}\end{aligned}$$

# Model fitting and hypothesis testing

**Blue:** base level group, control group

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## Step 5. Generalized Linear Model fit for each gene

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$$y = \beta_0 + \beta_1$$



$$\beta_1 = y - \beta_0 = \log_2(\text{expression}_{\text{red}}) - \log_2(\text{expression}_{\text{blue}})$$

$$\log_2 \left( \frac{\text{expression}_{\text{red}}}{\text{expression}_{\text{blue}}} \right)$$

$$\begin{aligned} \log_2 1 &= 0 \\ \log_2 2 &= 1 \\ \log_2 4 &= 2 \end{aligned}$$

$$= \log_2 \text{ Fold Change}$$

# Output of DESeq2

log2 fold change (MAP): samplotype MOV10\_overexpression vs control

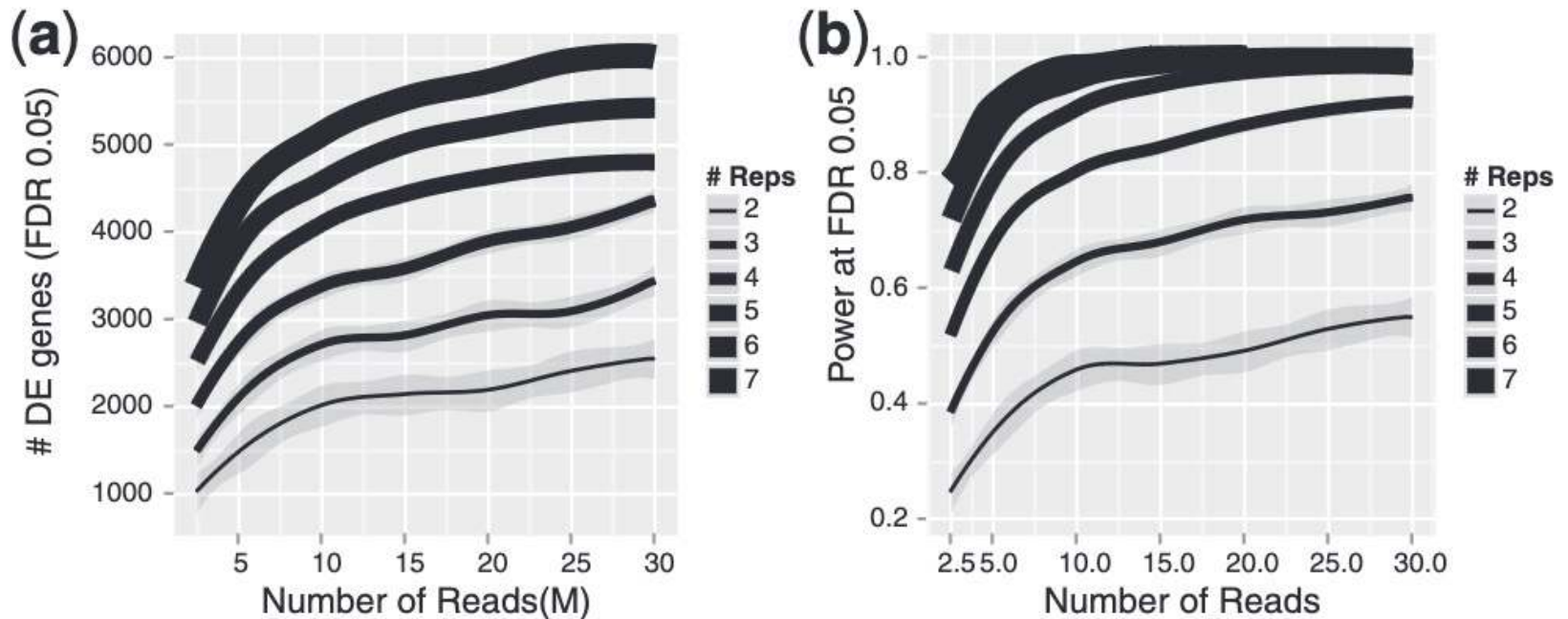
Wald test p-value: samplotype MOV10\_overexpression vs control

DataFrame with 6 rows and 6 columns

|             | baseMean    | log2FoldChange | lfcSE      | stat       | pvalue    | padj       |
|-------------|-------------|----------------|------------|------------|-----------|------------|
|             | <numeric>   | <numeric>      | <numeric>  | <numeric>  | <numeric> | <numeric>  |
| 1/2-SBSRNA4 | 45.6520399  | 0.26976764     | 0.18775752 | 1.4367874  | 0.1507784 | 0.25242910 |
| A1BG        | 61.0931017  | 0.20999700     | 0.17315013 | 1.2128030  | 0.2252051 | 0.34444163 |
| A1BG-AS1    | 175.6658069 | -0.05197768    | 0.12366259 | -0.4203185 | 0.6742528 | 0.77216278 |
| A1CF        | 0.2376919   | 0.02237286     | 0.04577046 | 0.4888056  | 0.6249793 | NA         |
| A2LD1       | 89.6179845  | 0.34598540     | 0.15901426 | 2.1758136  | 0.0295692 | 0.06725157 |
| A2M         | 5.8600841   | -0.27850841    | 0.18051805 | -1.5428286 | 0.1228724 | 0.21489067 |

1. baseMean: mean of normalized counts for all samples
2. log2FoldChange: log2 fold change
3. lfcSE: standard error
4. stat: Wald statistic
5. pvalue: Wald test p-value
6. padj: BH adjusted p-values

# When can we detect differential expression?



# What do we do with DE genes?

- Visualize expression levels, log fold changes, and significance
- Identify up- and down-regulated genes
- Compare sets of DE genes
- Test for functional enrichment of DE gene sets

# Today's activity

Focus on Differential Gene Expression Analysis:

- Evaluating our genomic resources
- Unsupervised clustering of samples based on expression
- Identifying differentially expressed (DE) genes
- Evaluating functional enrichment of DE gene sets

When you finish, you can run the steps for trimming, mapping and counting.

# Today's activity

## NOTES:

1. Skip counting the genes in the annotation (Rachel's mistake)
2. Using ggsave on guacamole: not compatible with .png, use .pdf.

7:00 - 7:30 : Differential expression background

7:30 – 8:30 : Free work time  
(take a break when you need/want it)

8:45: Check-in

9: – 9:40 : Free work time  
(take a break when you need/want it)

9:40 – 10 : Wrap-up and discussion

# Links to other DE/DS tools

| Tool                              | Use                                                                                                           | Link to best resource                                                                                                                                                                                                                                                                                              |
|-----------------------------------|---------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| WGCNA (R package)                 | Weighted gene coexpression analysis groups genes into modules/clusters by expression patterns across samples  | Horvath lab website:<br><a href="https://horvath.genetics.ucla.edu/html/CoexpressionNetwork/Rpackages/WGCNA/">https://horvath.genetics.ucla.edu/html/CoexpressionNetwork/Rpackages/WGCNA/</a>                                                                                                                      |
| DEXSeq (R package)                | Differential exon expression within the DESeq2 framework from exon count data                                 | Vignette:<br><a href="https://bioconductor.org/packages/release/bioc/vignettes/DEXSeq/inst/doc/DEXSeq.html">https://bioconductor.org/packages/release/bioc/vignettes/DEXSeq/inst/doc/DEXSeq.html</a>                                                                                                               |
| EdgeR (R package)                 | Differential expression analysis with differential exon expression functions from exon count data             | User guide:<br><a href="https://bioconductor.org/packages/release/bioc/vignettes/edgeR/inst/doc/edgeRUsersGuide.pdf">https://bioconductor.org/packages/release/bioc/vignettes/edgeR/inst/doc/edgeRUsersGuide.pdf</a>                                                                                               |
| LeafCutter (python & R scripts)   | Differential splicing analysis specifically focused on differential intron retention from junction count data | Github page:<br><a href="https://davidaknowles.github.io/leafcutter/">https://davidaknowles.github.io/leafcutter/</a>                                                                                                                                                                                              |
| IsoformSwitchAnalyzer (R package) | Differential isoform usage from transcript count data                                                         | Vignette:<br><a href="https://bioconductor.org/packages/release/bioc/vignettes/IsoformSwitchAnalyzer/inst/doc/IsoformSwitchAnalyzer.html">https://bioconductor.org/packages/release/bioc/vignettes/IsoformSwitchAnalyzer/inst/doc/IsoformSwitchAnalyzer.html</a>                                                   |
| EBSeq                             | Bayesian differential expression framework                                                                    | Vignette:<br><a href="https://bioconductor.org/packages/release/bioc/vignettes/EBSeq/inst/doc/EBSeq_Vignette.pdf">https://bioconductor.org/packages/release/bioc/vignettes/EBSeq/inst/doc/EBSeq_Vignette.pdf</a><br>Github page: <a href="https://github.com/lengning/EBSeq">https://github.com/lengning/EBSeq</a> |