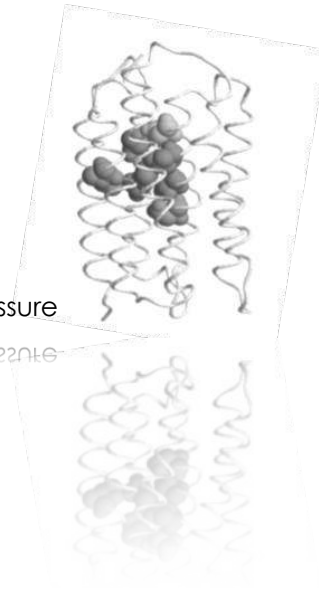


part 3: analysis of natural selection pressure

part 3: analysis of natural selection pressure



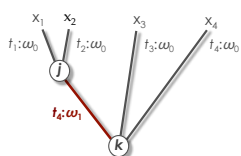
markov models are good

phenomenological codon models do have many benefits:

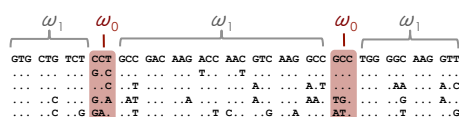
- principled framework for statistical inference
- avoiding *ad hoc* corrections of "counting" methods
- computation of transition probabilities \*
- explicit use of phylogeny
- model  $\omega$  variation among sites
- model  $\omega$  variation among branches
- many other kinds of models for  $\omega$

\* Computation of transition probabilities accomplishes, in just one step, (1) a proper correction for multiple substitutions, (2) weighting for alternative pathways between codons and (3) is the basis for estimating the values of the model parameters from the data in hand.

## two basic types of models

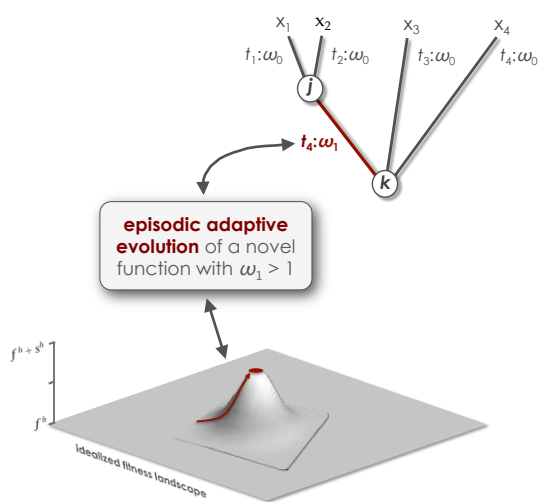


**branch models**  
( $\omega$  varies among  
branches)

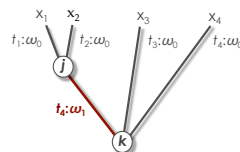


**site models**  
( $\omega$  varies among sites)

## interpretation of a branch model



## branch models\*



| variation ( $\omega$ ) among branches: | approach              |
|----------------------------------------|-----------------------|
| Yang, 1998                             | fixed effects         |
| Bielawski and Yang, 2003               | fixed effects         |
| Seo et al. 2004                        | auto-correlated rates |
| Kosakovsky Pond and Frost, 2005        | genetic algorithm     |
| Dutheil et al. 2012                    | clustering algorithm  |

\* these methods can be useful when selection pressure is strongly **episodic**

## site models\*

```

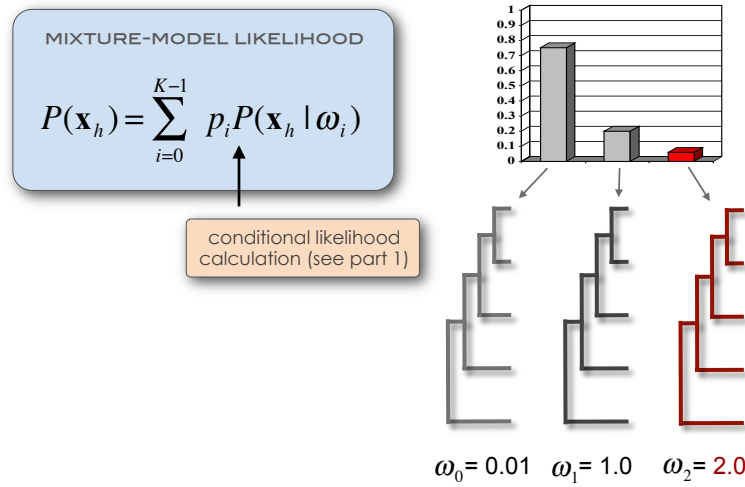
GTG CTG TCT CCT GCC GAC AAG ACC AAC GTC AAG GCC GCC TGG GGC AAG GTT GGC GCG CAC
G..C ..C ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T
..C ..C ..C ..C ..C ..C ..C ..C ..C ..C ..C ..C ..C ..C ..C ..C ..C ..C ..C ..C ..C ..C
G..A ..AT ..A ..A ..A ..A ..A ..A ..A ..A ..A ..A ..A ..A ..A ..A ..A ..A ..A ..A ..A ..A
..C ..C ..G ..GA ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T ..T

```

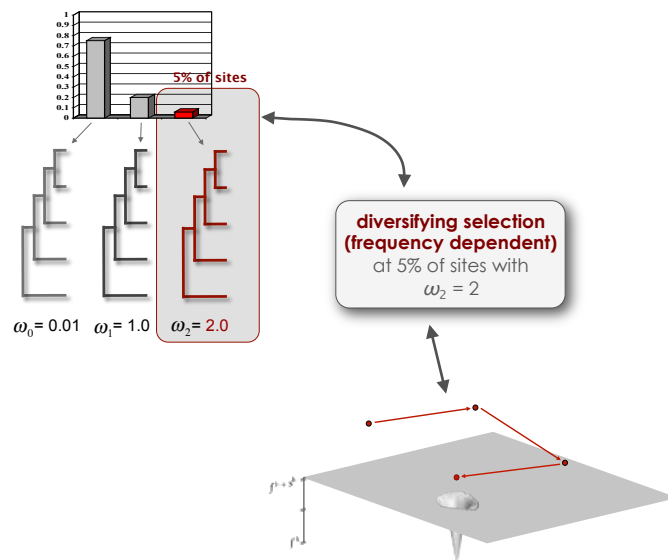
| variation ( $\omega$ ) among sites:                 | approach            |
|-----------------------------------------------------|---------------------|
| Yang and Swanson, 2002                              | fixed effects (ML)  |
| Bao, Gu and Bielawski, 2006                         | fixed effects (ML)  |
| Massingham and Goldman, 2005                        | site wise (LRT)     |
| Kosakovsky Pond and Frost, 2005                     | site wise (LRT)     |
| Nielsen and Yang, 1998                              | mixture model (ML)  |
| Kosakovsky Pond, Frost and Muse, 2005               | mixture model (ML)  |
| Huelsenbeck and Dyer, 2004; Huelsenbeck et al. 2006 | mixture (Bayesian)  |
| Rubenstein et al. 2011                              | mixture model (ML)  |
| Bao, Gu, Dunn and Bielawski 2008 & 2011             | mixture (LiBaC/MBC) |
| Murell et al. 2013                                  | mixture (Bayesian)  |

- useful when at some sites evolve under **diversifying selection** pressure over long periods of time
- this is not a comprehensive list

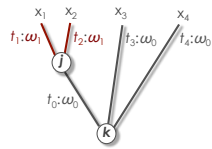
## site models: discrete model (M3)



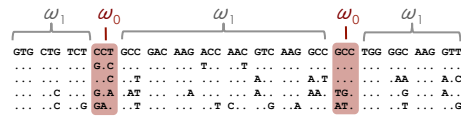
## interpretation of a sites-model



## models for variation among branches & sites



**branch models**  
( $\omega$  varies among  
branches)



**site models**  
( $\omega$  varies among sites)



## models for variation among branches & sites

| variation ( $\omega$ ) among branches & sites: | approach           |
|------------------------------------------------|--------------------|
| Yang and Nielsen, 2002                         | fixed+mixture (ML) |
| Forsberg and Christiansen, 2003                | fixed+mixture (ML) |
| Bielawski and Yang, 2004                       | fixed+mixture (ML) |
| Giundon et al., 2004                           | switching (ML)     |
| Zhang et al. 2005                              | fixed+mixture (ML) |
| Kosakovsky Pond et al. 2011, 2012              | full mixture (ML)  |

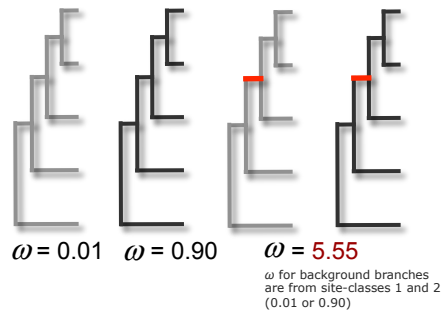
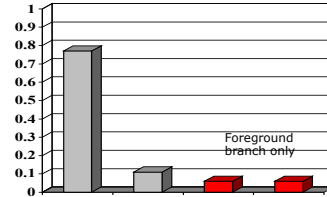
\* these methods can be useful when selection **pressures change over time at just a fraction of sites**

\* it can be a challenge to apply these methods properly (**more about this later**)

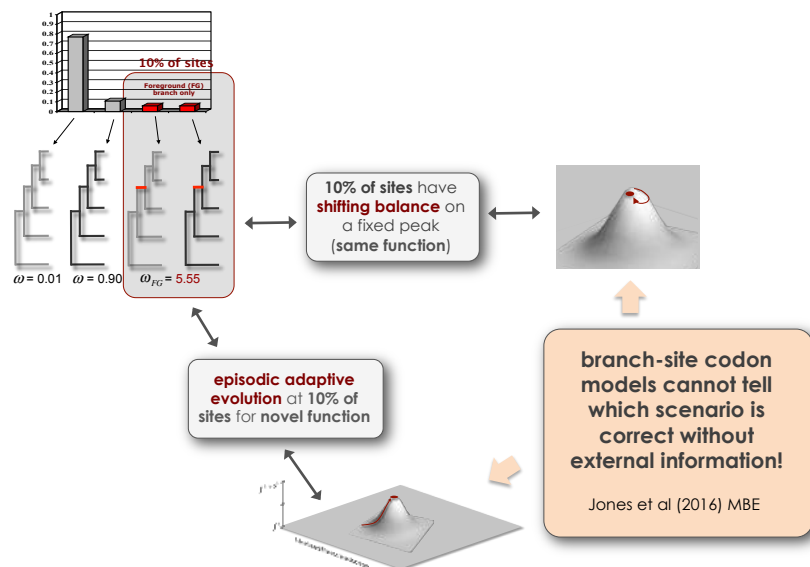
## branch-site "Model B"

MIXTURE-MODEL LIKELIHOOD

$$P(\mathbf{x}_h) = \sum_{i=0}^{K-1} p_i P(\mathbf{x}_h | \omega_i)$$



## two scenarios can yield branch-sites with dN/dS &gt; 1



## model-based inference

model-based inference

"OMEGA MODELS"

$$Q_{ij} = \begin{cases} 0 & \text{if } i \text{ and } j \text{ differ by } > 1 \\ \pi_j & \text{for synonymous tv.} \\ \kappa\pi_j & \text{for synonymous ts.} \\ \omega\pi_j & \text{for non-synonymous tv.} \\ \omega\kappa\pi_j & \text{for non-synonymous ts.} \end{cases}$$

Goldman and Yang (1994)  
Muse and Gaut (1994)

## model based inference

---

### 3 analytical tasks

**task 1.** parameter estimation (e.g.,  $\omega$ ) 

**task 2.** hypothesis testing

**task 3.** make predictions (e.g., sites having  $\omega > 1$  )

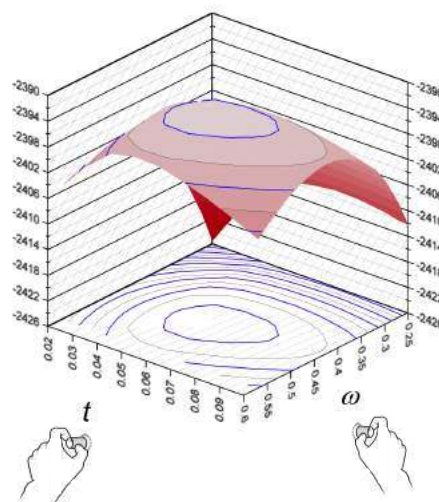
# task 1: parameter estimation

$t, \kappa, \omega$  = unknown constants estimated by ML

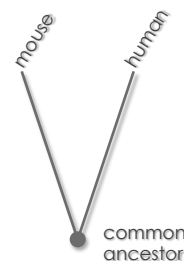
$\pi$ 's = empirical [GY: F3×4 or F61 in Lab]

use a numerical hill-climbing algorithm to maximize the likelihood function

## task 1: parameter estimation



**Parameters:**  $t$  and  $\omega$   
**Gene:** acetylcholine  $\alpha$  receptor



$\ln L = -2399$



## task 2: statistical significance

task 1. parameter estimation (e.g.,  $\omega$ ) ✓

task 2. hypothesis testing ← **LRT**

task 3. prediction / site identification

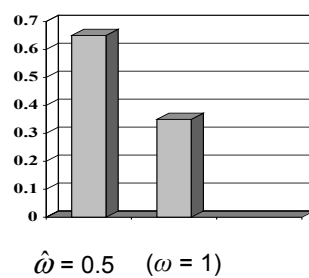
## task 2: likelihood ratio test for positive selection

$H_0$ : variable selective pressure but NO positive selection (M1)

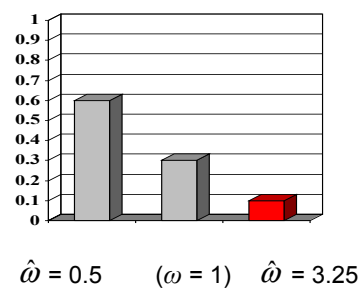
$H_1$ : variable selective pressure with positive selection (M2)

Compare  $2\Delta l = 2(l_1 - l_0)$  with a  $\chi^2$  distribution

Model 1a

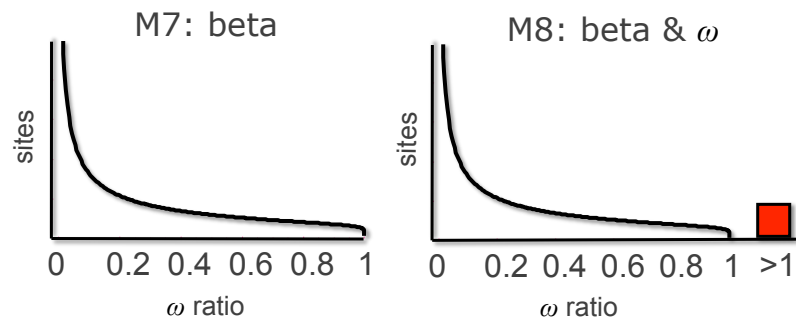


Model 2a



## task 2: likelihood ratio test for positive selection

$H_0$ : Beta distributed variable selective pressure (M7)  
 $H_1$ : Beta plus positive selection (M8)  
 Compare  $2\Delta l = 2(l_1 - l_0)$  with a  $\chi^2$  distribution



## task 3: identify the selected sites

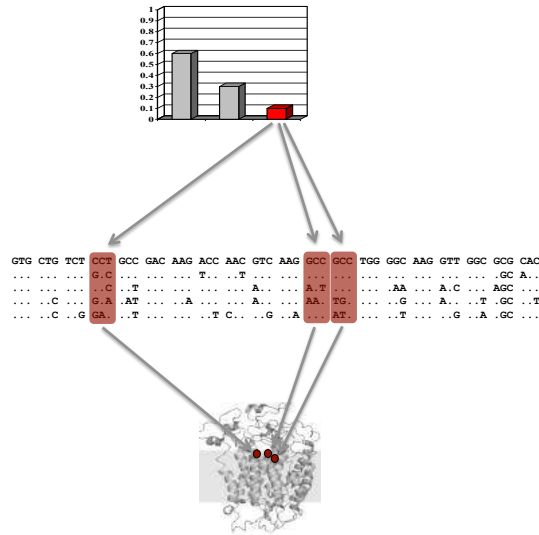
- task 1. parameter estimation (e.g.,  $\omega$ ) ✓
- task 2. hypothesis testing ✓
- task 3. prediction / site identification ← **Bayes' rule**

task 3: which sites have  $dN/dS > 1$

**model:**  
9% have  $\omega > 1$

**Bayes' rule:**  
site 4, 12 & 13

**structure:**  
sites are in contact



Bayes' rule: yet another (silly) example

**Suppose that a population consists of 60% males and 40% females, and a disease occurs at the rate 1% in males and 0.1% in females.**

$Q_1$ : What is the probability that any individual carries the disease?

$$A_1: 0.6 \times 0.01 + 0.4 \times 0.001 = 0.0064$$

$$P(D) = P(M)P(D|M) + P(F)P(D|F)$$

See Yang and Bielawski (2000) TREE 15:496-503 for a detailed presentation of this example

Bayes' rule: yet another (silly) example

Q<sub>2</sub>: Given that an individual carries the disease, what is the probability that it is a male?

$$A_2: 0.6 \times 0.01 / 0.0064 = 0.94$$

$$P(M|D) = \frac{P(M)P(D|M)}{P(D)}$$

See Yang and Bielawski (2000) TREE 15:496-503 for a detailed presentation of this example

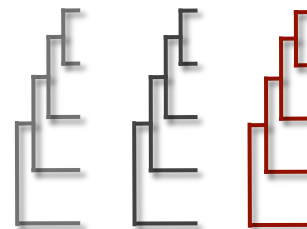
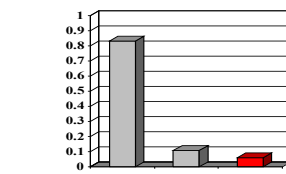
review the mixture likelihood

$$P(\mathbf{x}_h) = \sum_{i=0}^{K-1} p(\omega_i) P(\mathbf{x}_h | \omega_i)$$

↑  
Total  
probability

↑  
Prior

↑  
Likelihood



$$\begin{array}{lll} \omega_0 = 0.03 & \omega_1 = 0.40 & \omega_2 = 14.1 \\ p_0 = 0.85 & p_1 = 0.10 & p_2 = 0.05 \end{array}$$

### Bayes' rule for identifying selected sites

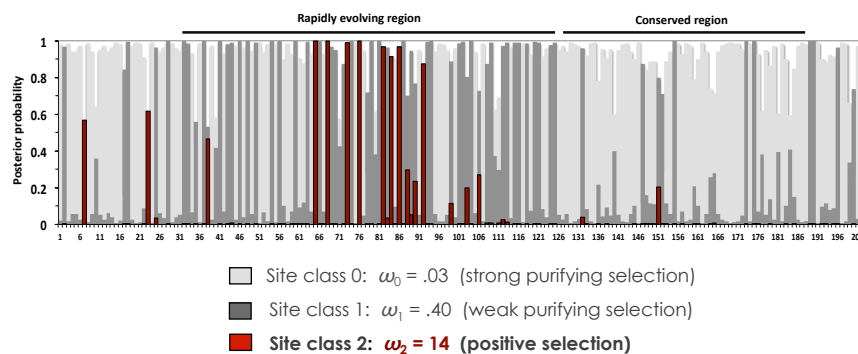
- Site class 0:  $\omega_0 = .03$ , 85% of codon sites  
 ■ Site class 1:  $\omega_1 = .40$ , 10% of codon sites  
 ? → ■ Site class 2:  $\omega_2 = 14$ , 05% of codon sites

Prior probability of hypothesis ( $\omega_2$ )      Likelihood of hypothesis ( $\omega_2$ )

$$P(\omega_2 | x_h) = \frac{P(\omega_2)P(x_h | \omega_2)}{\sum_{i=0}^{K-1} P(\omega_i)P(x_h | \omega_i)}$$

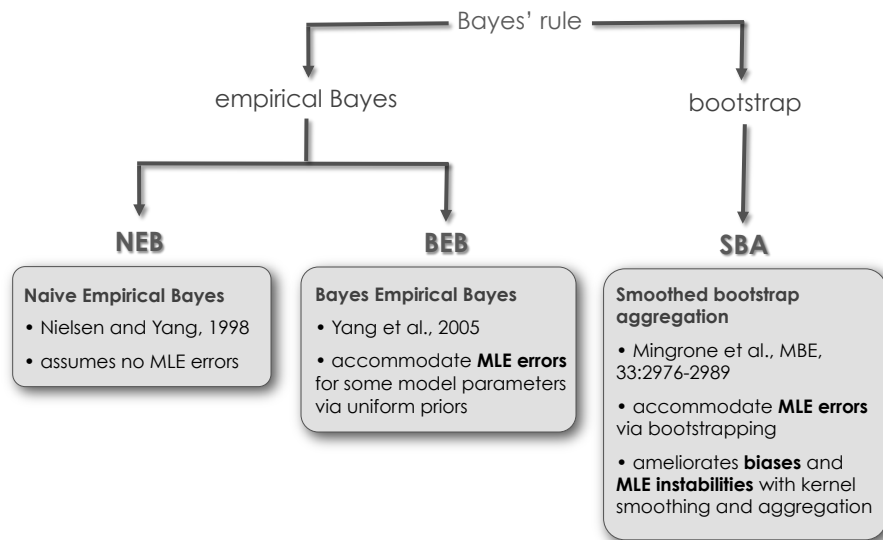
Posterior probability of hypothesis ( $\omega_2$ )      Marginal probability (Total probability) of the data

### task 3: Bayes rule for which sites have dN/dS > 1



**NOTE:** The posterior probability should NOT be interpreted as a "P-value"; it can be interpreted as a measure of relative support, although there is rarely any attempt at "calibration".

task 3: Bayes rule for which sites have  $dN/dS > 1$

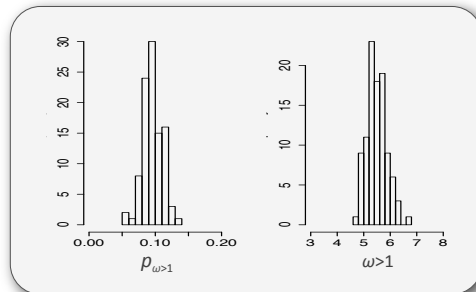


critical question:

*Have the requirements for maximum likelihood inference been met?*

(rarely addressed in real data analyses)

regularity conditions have been met

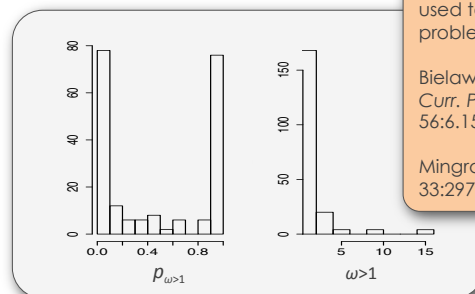


#### Normal MLE uncertainty (M2a)

- large sample size with regularity conditions
- MLEs approximately unbiased and minimum variance

$$\hat{\theta} \sim N\left(\theta, I(\hat{\theta})^{-1}\right)$$

regularity conditions have **NOT** been met



**bootstrapping** can be used to diagnose this problem:

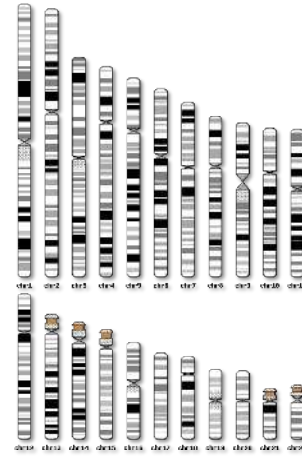
Bielawski et al. (2016)  
*Curr. Protoc. Bioinf.*  
56:6.15.

Mingrone et al., *MBE*,  
33:2976-2989

#### MLE instabilities (M2a)

- small sample sizes and  $\theta$  on boundary
- continuous  $\theta$  has been discretized (e.g., M2a)
- non-Gaussian, over-dispersed, divergence among datasets

multi-gene evolutionary survey  
(*& experimental validation*)  
(*& experimental validation*)  
multi-gene evolutionary survey



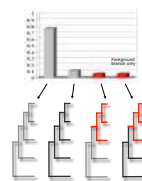
*evolutionary survey*

"Identification and assessment of *NR2C1* (*TR2*) as a modulator of pluripotentiality during hominid evolution"

Baker et al. (2016) *Genetics*, 203:905-922



Sample, process, and align 48 nuclear receptors



(1) evolutionary survey  
(2) rank candidates



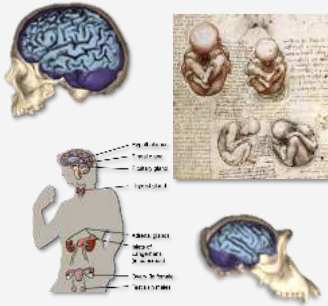
Experimental assessment of evolutionary change in pluripotentiality



*evolutionary survey*

nuclear receptor (NR) family

reproduction,  
development, and  
endocrine signaling



hormones & behavior



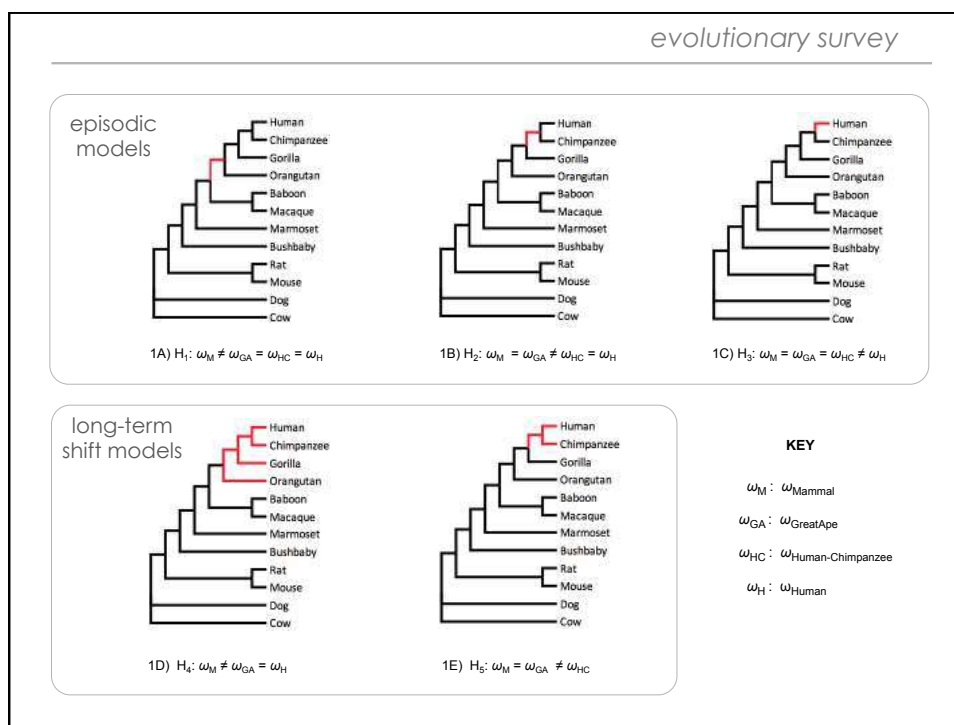
Intracellular transcription factors regulate gene expression

*evolutionary survey*

analysis of 48 primate NRs

**Phase 1:**

1. processing and Q.C.
2. structurally-aware modelling of codon evolution
3. test each gene for 5 different evolutionary scenarios
4. use "FDR control" to identify families of genes associated with different evolutionary scenarios



*evolutionary survey*

phase 1: analysis of 48 NRs

| evolutionary scenario  | LRT: $p < 0.05$ | FDR: $q < 0.05$ |
|------------------------|-----------------|-----------------|
| <b>episodic models</b> |                 |                 |
| $H_1$ : great apes     | 1 gene          | 0 genes         |
| $H_2$ : human-chimp    | 0 genes         | 0 genes         |
| $H_3$ : humans         | 4 genes         | 1 genes         |
| <b>long-term shift</b> |                 |                 |
| $H_4$ : great apes     | 10 genes        | 5 genes         |
| $H_5$ : human-chimp    | 8 genes         | 5 genes         |

number of unique candidate genes: 9

analysis of 9 NRs

**phase 2: reliability and robustness assessment**

1. alignment (independent evaluations)
2. recombination
3. MG94 style codon model
4. alternative tree topologies
5. robustness to variation in baseline DNA/RNA rates
6. bootstrapping

**nuclear receptor *NR1D1***: positive selection along human lineage  
at 1% of sites

1. alignment assessment ✓
2. no evidence of recombination ✓
3. alternate framework (MG94): *LRTs and MLEs robust*

brief detour

## how to model codon frequencies?

---

|                             |                                                                |
|-----------------------------|----------------------------------------------------------------|
|                             | substitution rates are proportional to empirical frequency of: |
| Goldman and Yang 1994 (GY): | target codon                                                   |
| Muse and Gaut 1994 (MG):    | target nucleotide                                              |

See Rodrigue et al. (2008) for a comparison of GY and MG style codon models that suggests the MG style, combined with parameters for codon preferences, might be the most desirable core-model for future development.

The MutSel process (part 1) is inherently a process whereby the transition probability depends on the target nucleotide (MG).

## how to model codon frequencies?

---

example: A → C

AAA → CAA

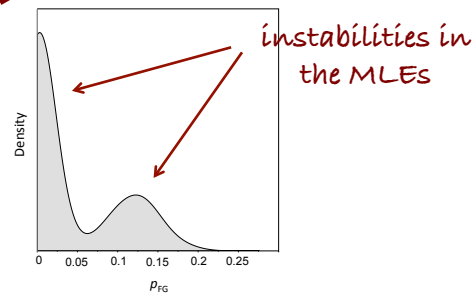
AAA → ACA

AAA → AAC

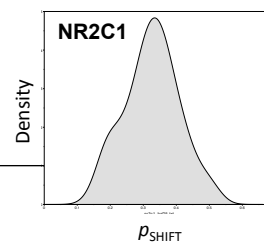
|    | Δ at codon position |                 |                 |
|----|---------------------|-----------------|-----------------|
|    | 1 <sup>st</sup>     | 2 <sup>nd</sup> | 3 <sup>rd</sup> |
| GY | $\pi_{CAA}$         | $\pi_{ACA}$     | $\pi_{AAC}$     |
| MG | $\pi_c^1$           | $\pi_c^2$       | $\pi_c^3$       |

**nuclear receptor *NR1D1***: positive selection along human lineage at 1% of sites

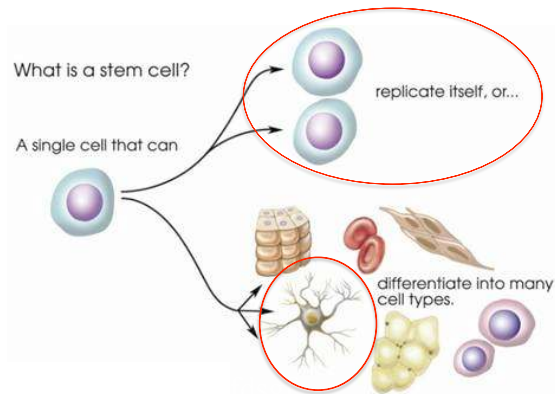
1. alignment assessment ✓
2. no evidence of recombination ✓
3. alternate framework (MG94): LRTs and MLEs robust ✓
4. alternate tree topology: LRTs and MLEs robust ✓
5. variation in baseline DNA:RNA rate of evolution: ✓
6. bootstrap distribution on L



| gene         | status                       | note              |
|--------------|------------------------------|-------------------|
| ESSRA        | <b>excluded</b>              | MLE instabilities |
| ESSRB        | <b>excluded</b>              | MLE instabilities |
| NR1D1        | <b>excluded</b>              | MLE instabilities |
| NR2E3        | <b>excluded</b>              | recombination     |
| RARG         | <b>excluded</b>              | MLE instabilities |
| ESSRB        | ranked 4 <sup>th</sup>       |                   |
| PGR          | ranked 3 <sup>rd</sup>       |                   |
| RORA         | ranked 2 <sup>nd</sup>       |                   |
| <b>NR2C1</b> | <b>ranked 1<sup>st</sup></b> |                   |



## What is the function of *NR2C1*?



- Prefrontal cortex
- Embryonic stem cell maintenance
- Neuronal differentiation

image: C. Tworney

I. Introduction II. Comparative genomics III. Gene expression IV. Ancestral gene reconstruction V. Future directions VI. Conclusions

## *Oct4* & *Nanog*

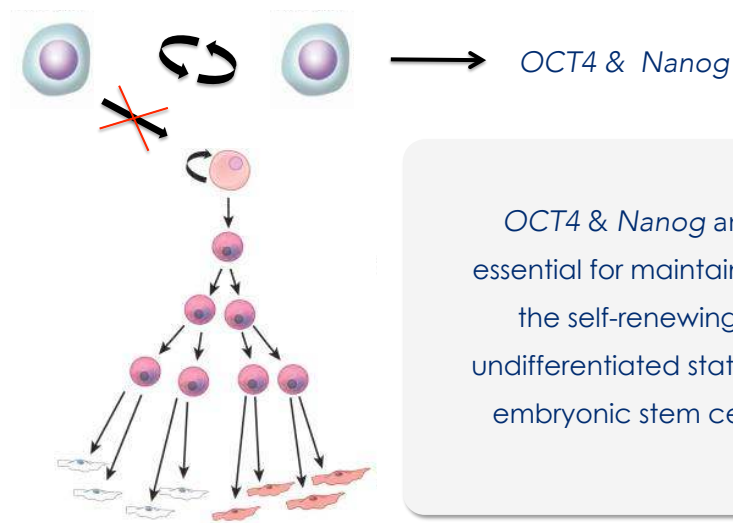


image: White 2015

I. Introduction II. Comparative genomics III. Gene expression IV. Ancestral gene reconstruction V. Future directions VI. Conclusions

## Oct4 & Nanog

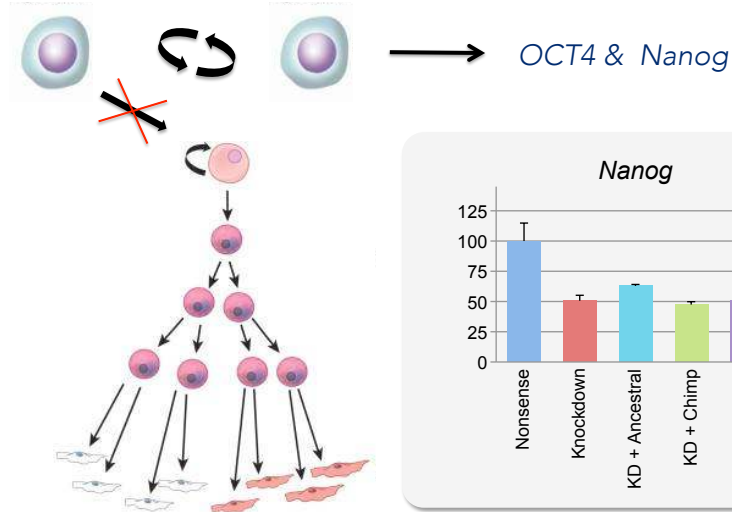


image: White 2015

I. Introduction II. Comparative genomics III. Gene expression IV. Ancestral gene reconstruction V. Future directions VI. Conclusions

## Oct4 & Nanog

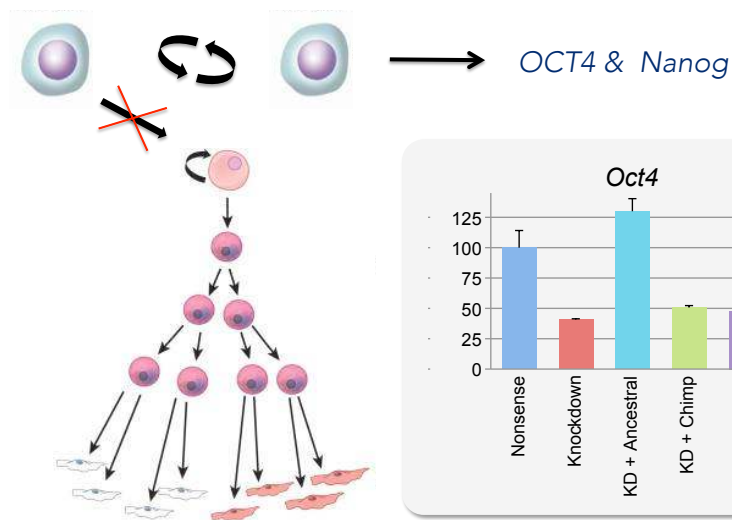


image: White 2015

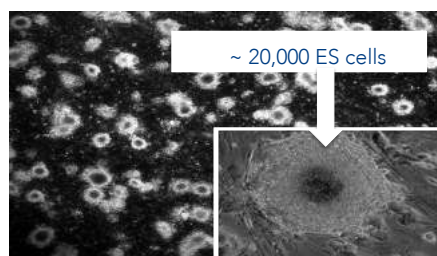
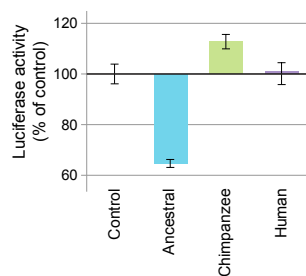
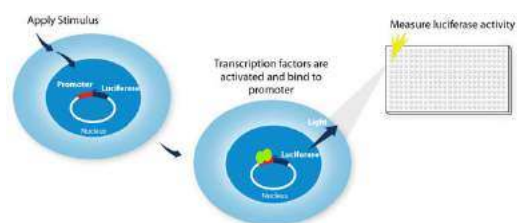
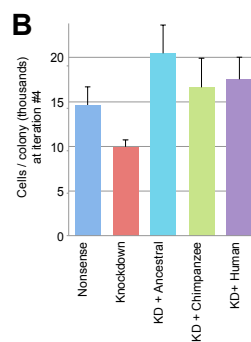
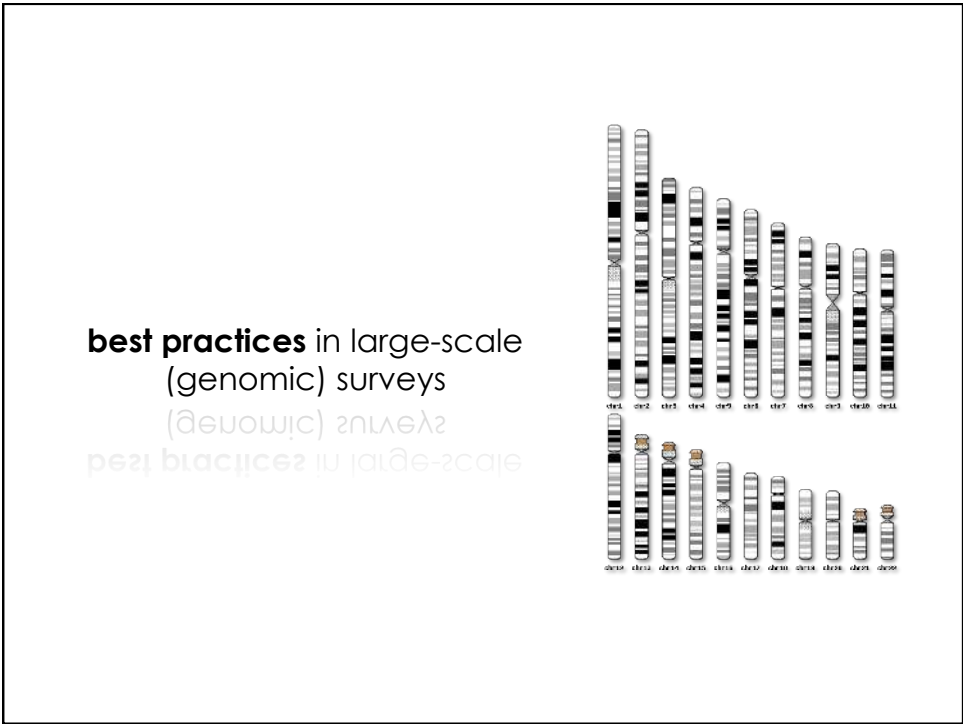
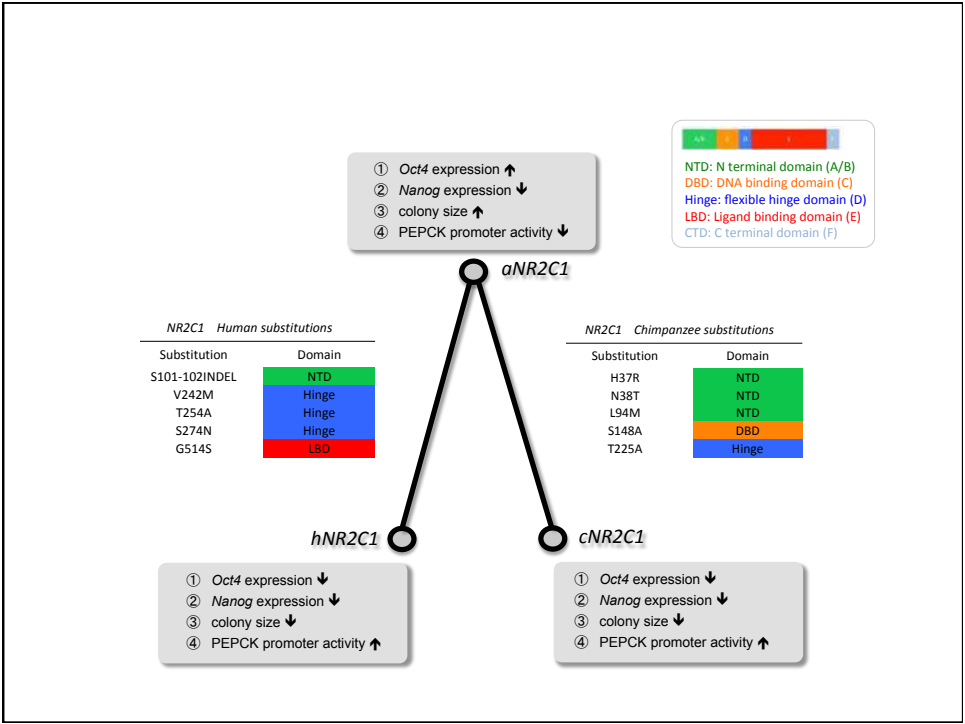


Photo: Tom Maynard







---

*best practices for "genome scans"***Phase 1: Large scale survey**

1. Do as much quality control and cross validation in the pipeline as possible. Remove as many poor candidates as possible.
2. alignment validation
3. plan your analysis carefully; cover a variety of evolutionary questions; execute that plan
4. control the false discovery rate; identify "families" of genes which are significantly associated with specific evolutionary scenarios

---

*best practices for "genome scans"***Phase 2: Robustness analysis**

1. independent alignment validation (possible re-analysis)
2. test for recombination
3. re-run the analytical plan using a different formulation of the codon model (e.g., MG vs, GY).
4. re-run the analytical plan using alternative tree topologies.
5. bootstrap to assess MLE distributions for instabilities.
6. smoothed aggregated bootstrap for site-wise inference

---

*best practices for "genome scans"*

for further discussion of best practices see ...

- Baker et al. (2016) *Genetics*, 203:905-922
- Bielawski et al. (2016) *Curr. Protoc. Bioinf.*, 56: Unit 6.15
- Mingrone et al. (2016) *MBE*, 33:2976-2989

**THE END.**