

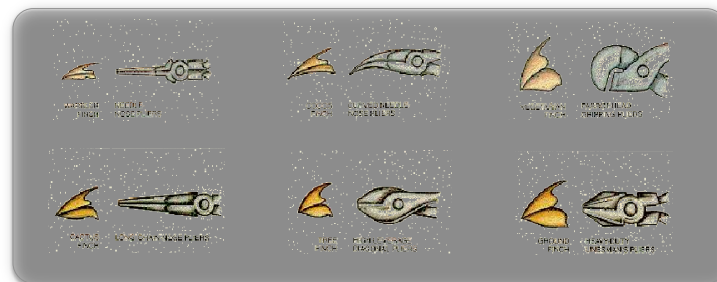
searching for functional divergence in genomes and metagenomes

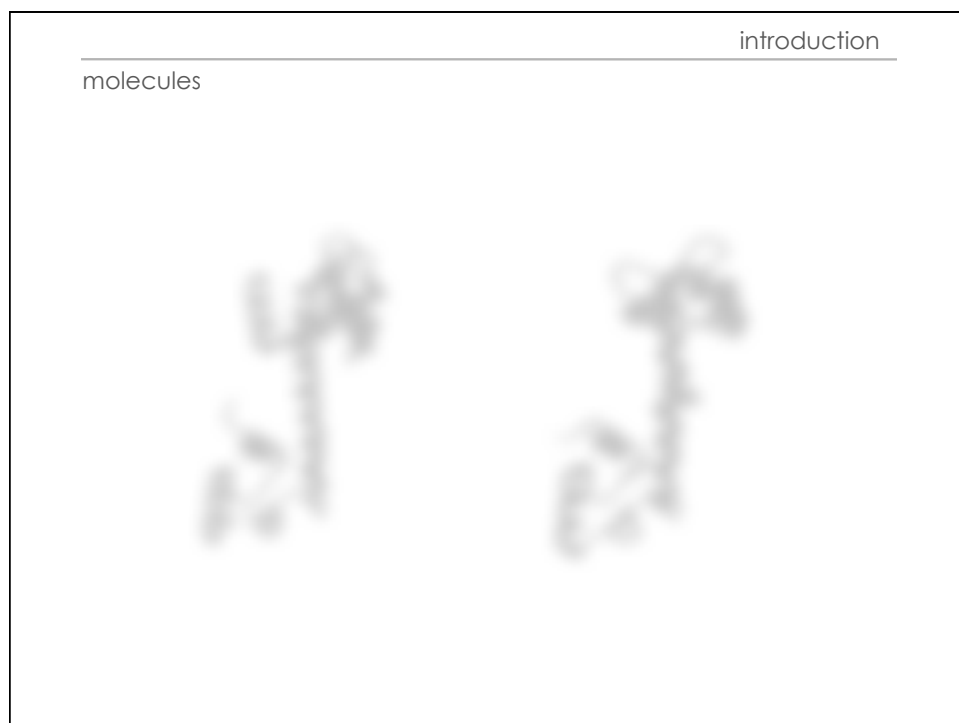
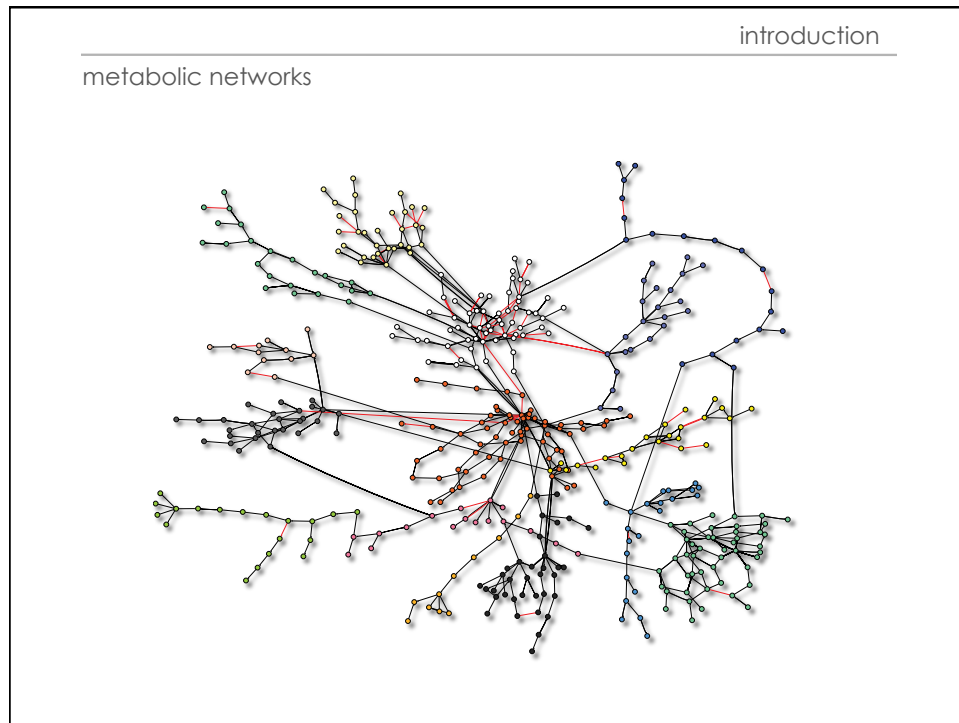
Joseph P. Bielawski
Department of Biology
Department of Mathematics & Statistics
Dalhousie University



introduction

morphology





introduction

gene sequences

human
cow
rabbit
rat
opossum

```

GTG CTG TCT CCT GCC GAC AAG ACC AAC GTC AAG GCC GCC TGG GGC AAG GTT GGC GCG CAC
... .. G.C ... .. T... ..T ... .. .. .. .. .. .. .. .. ..GC A..
... .. ..C ..T ... .. ..A... ..A.T ... ..AA ... ..A.C ... ..AGC ...
... ..C ... ..G.A ..AT ... ..A ... ..AA. TG. ... ..G ... ..A... ..T ..GC ..T
... ..C ..G GA. ..T ... ..T C... ..G ..A ... ..AT. ... ..T ... ..G ..A ..GC ...

GCT GGC GAG TAT GGT GCG GAG GCC CTG GAG AGG ATG TTC CTG TCC TFC CCC ACC ACC AAG
... ..A ..CT ... ..C ..A ... ..T ... .. .. .. .. ..AG. ... .. .. ..
..G. ... .. ..C ..C ... ..G... .. .. .. ..T... GG. ... .. .. ..
..G. ..T ..A ... ..C ..A... .. ..A C... .. .. ..GCT G... .. .. ..
..C ..T ..CC ..C ..CA ..T ..A ..T ..T ..CC ..A ..CC ... ..C ... .. ..T ... ..A

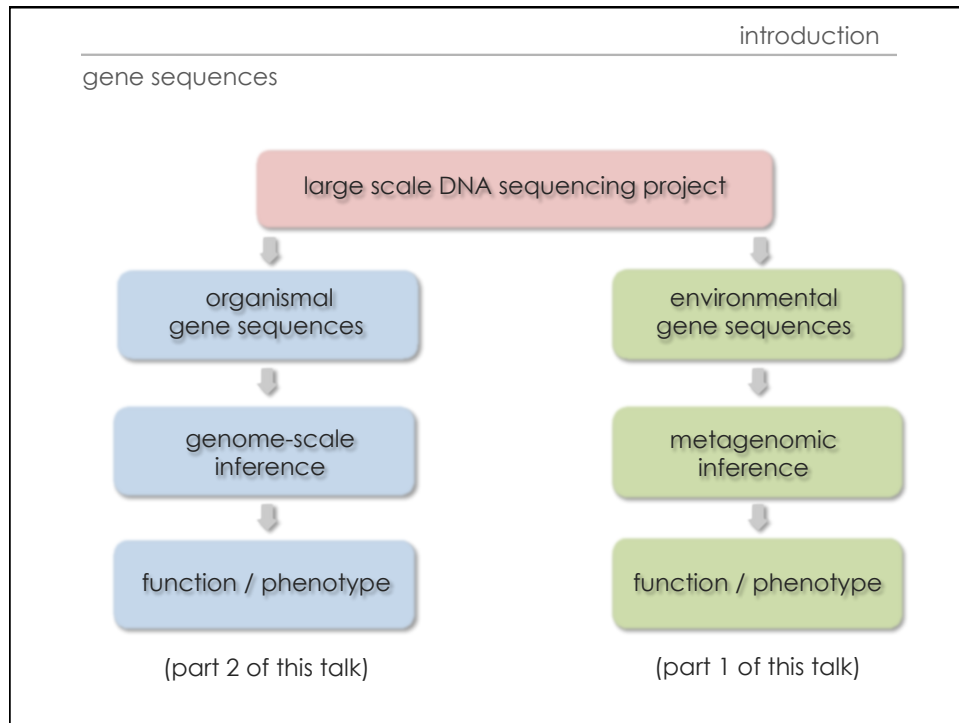
ACC TAC TTC CCG CAC TTC GAC CTG AGC CAC GGC TCT GCC CAG GTT AAG GGC CAC GGC AAG
... .. ..C ... .. .. .. .. ..G ... .. ..C ... .. .. ..G..
... .. ..C ... .. ..T.C ..C. ... .. .. ..AG ... ..A.C ..A ..C. ... ..
... .. ..T.T ... ..A.T ..T G.A ... ..C... .. .. ..C ... ..CT ... ..
..T ... ..C ... .. .. .. ..TC. ..C. ... ..C ... ..A.C C... ..T ..T ..T ...

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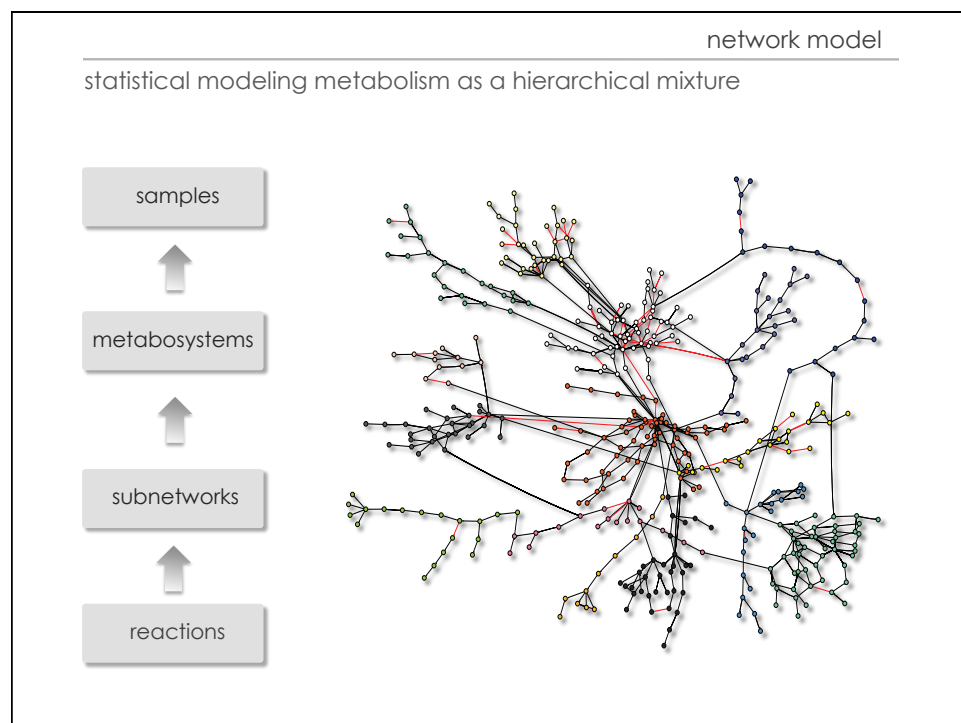
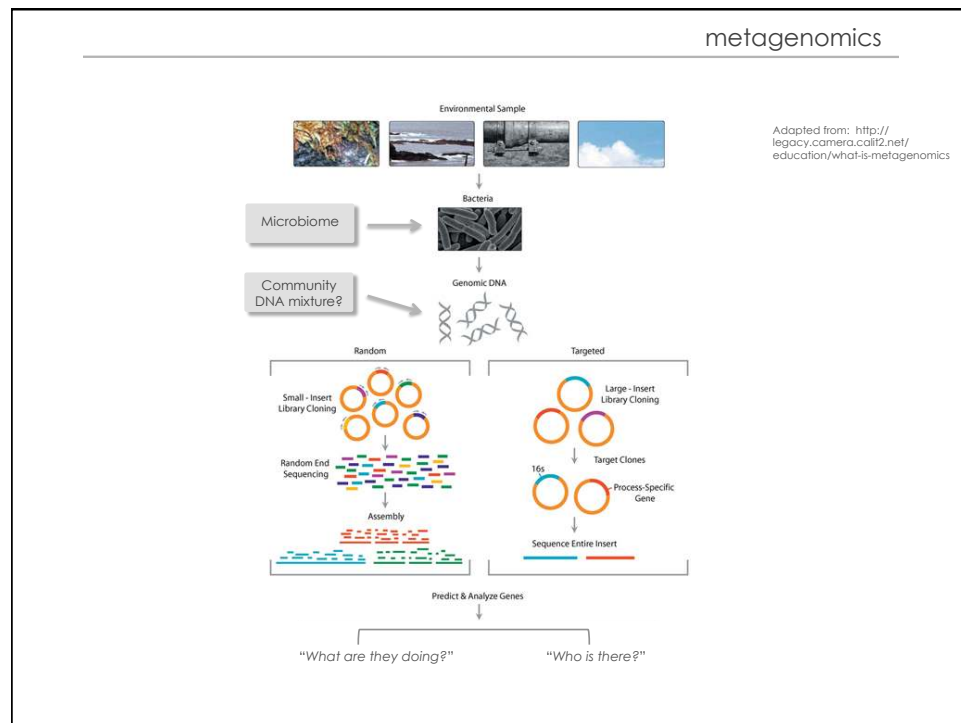
introduction

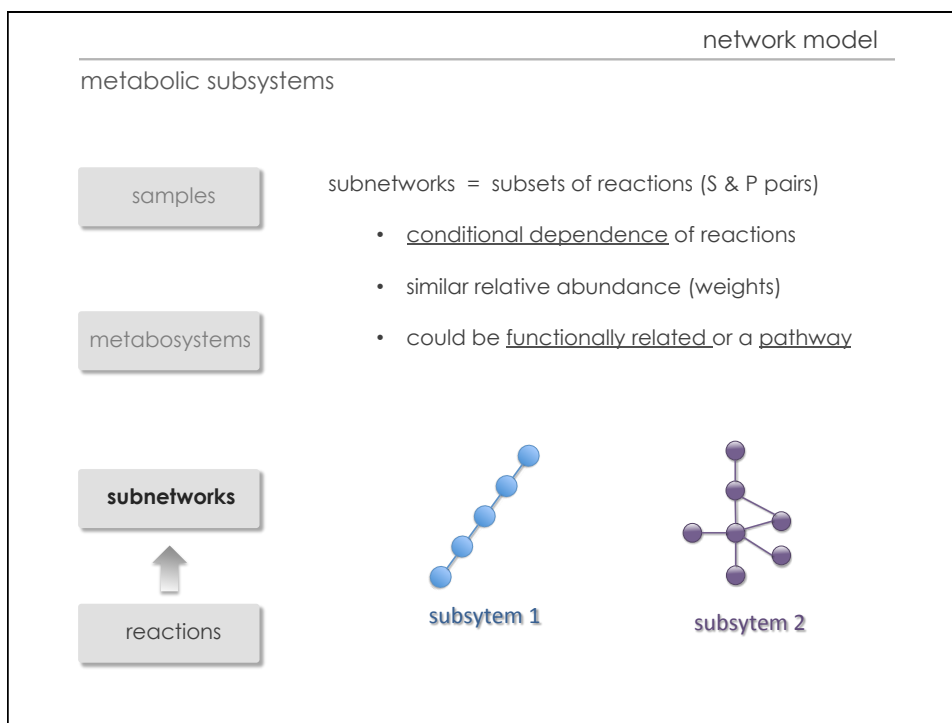
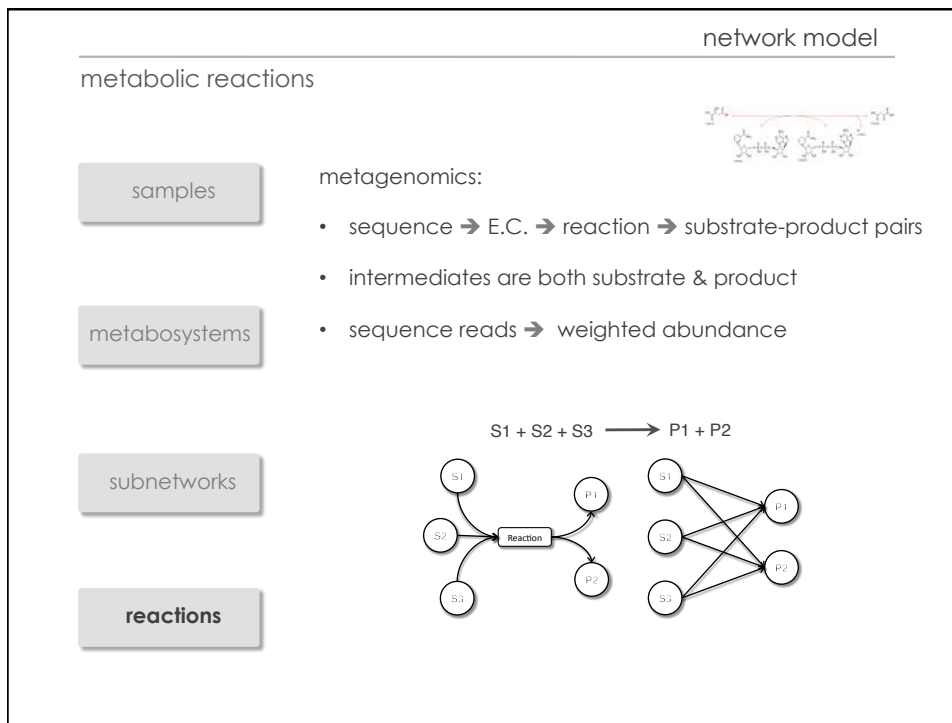
gene sequences

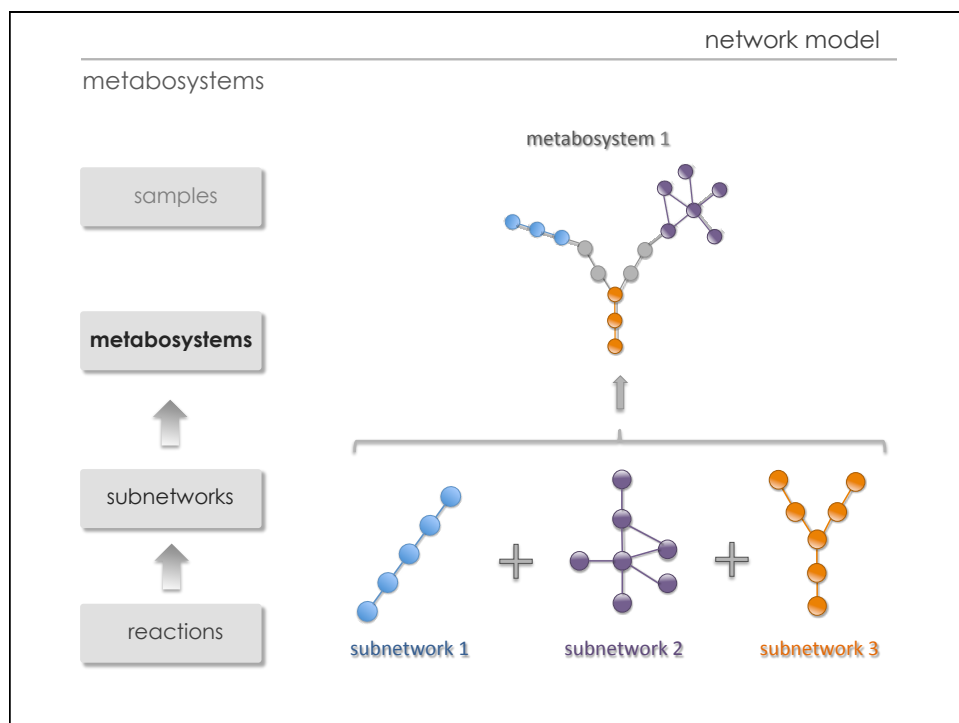
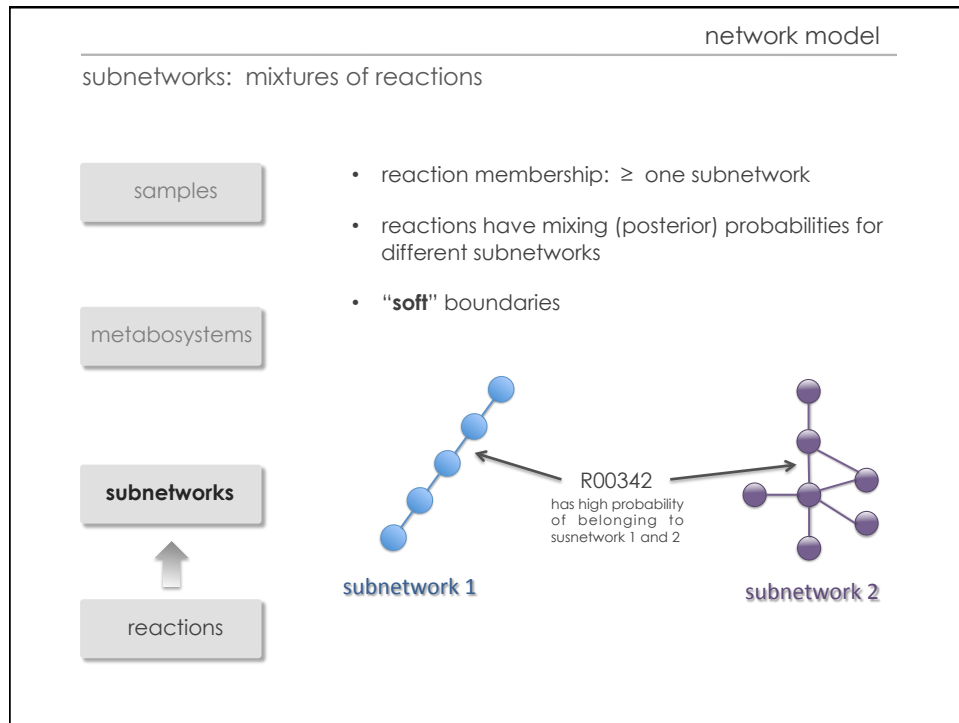
1. How do we efficiently extract information from large and complex datasets?
2. How to identify information (signals) most relevant to function?

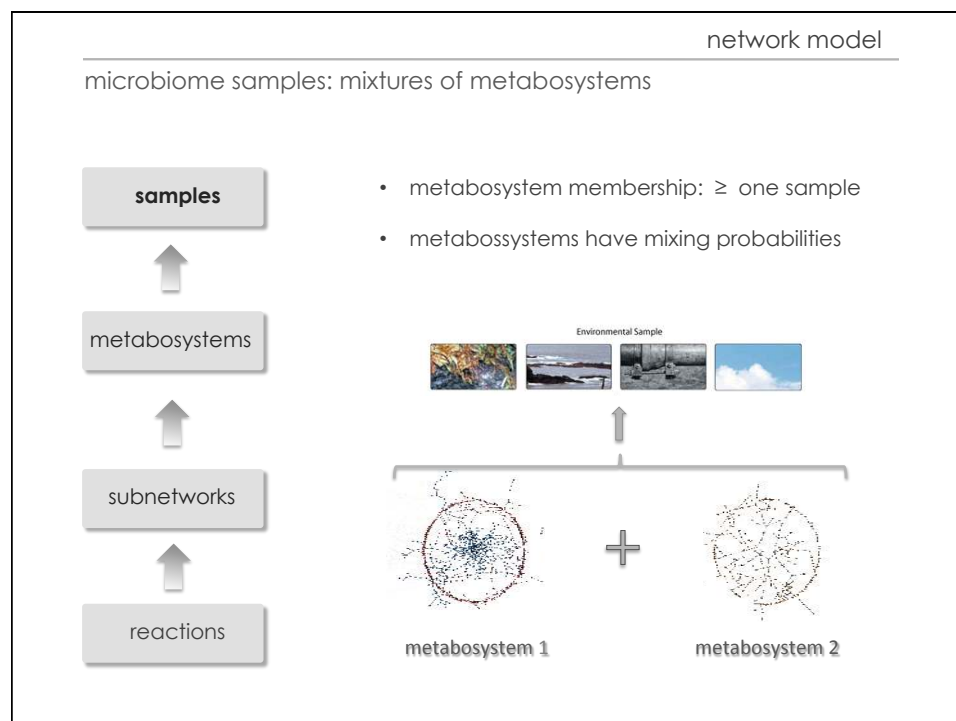
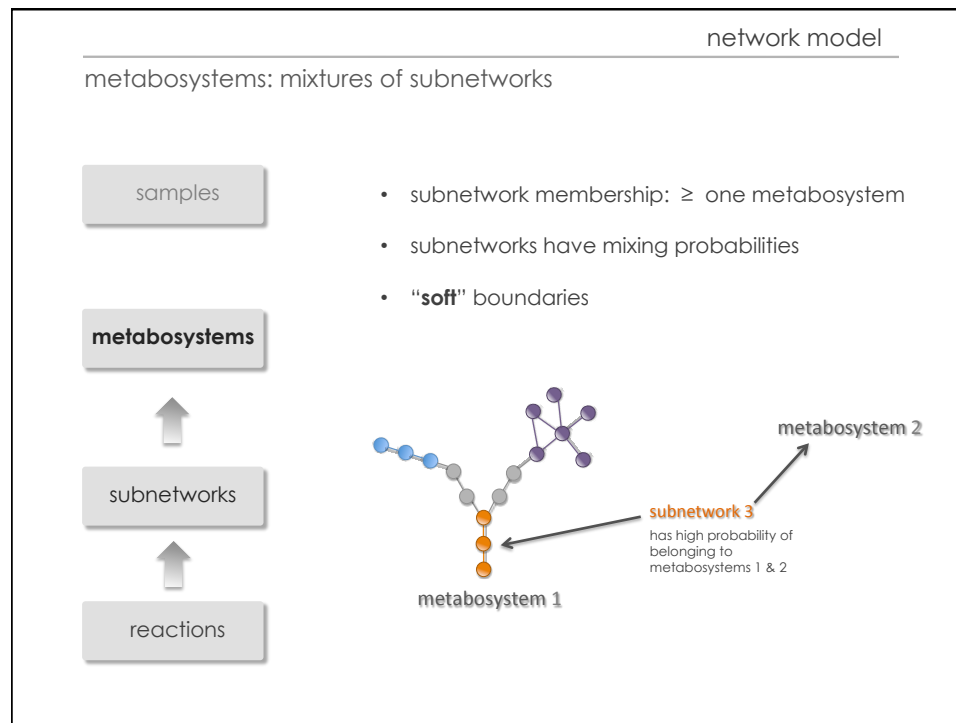


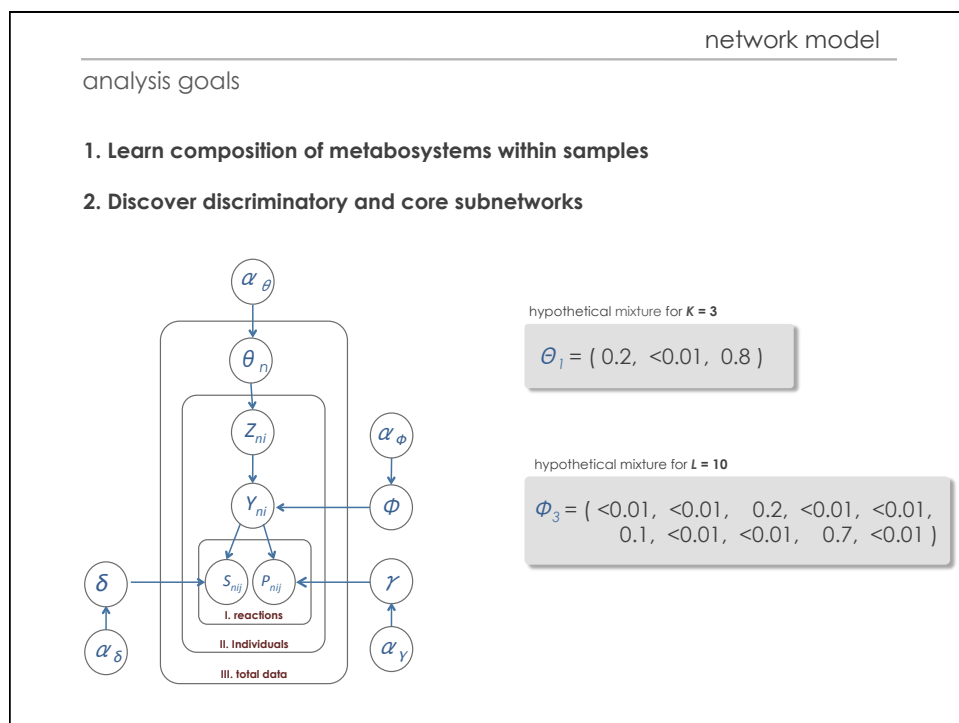
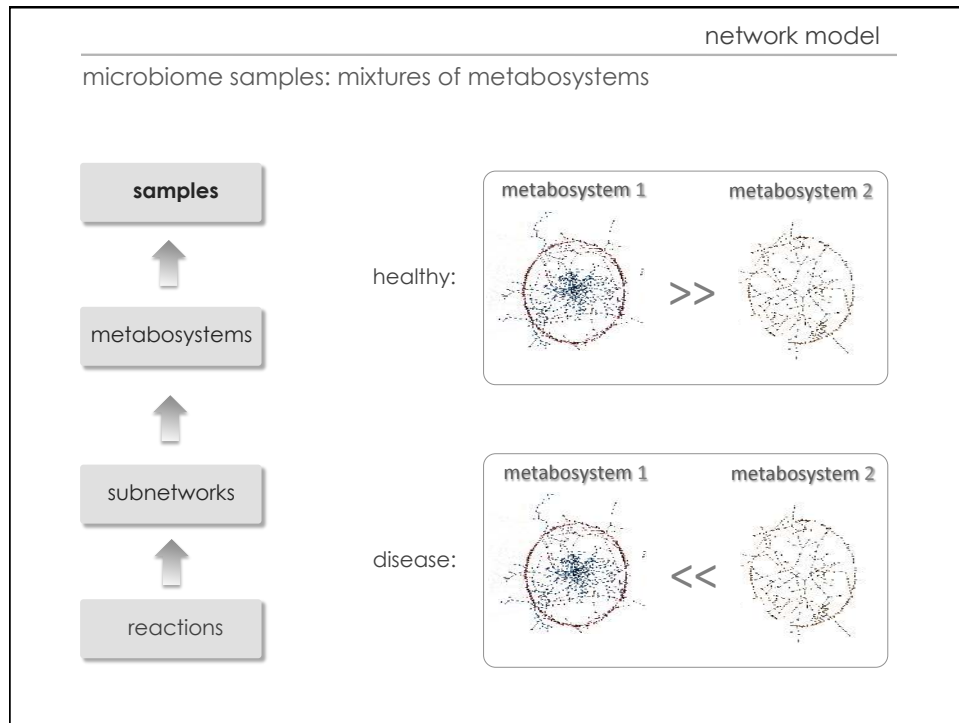
part 1: Searching for functional divergence
metagenomics

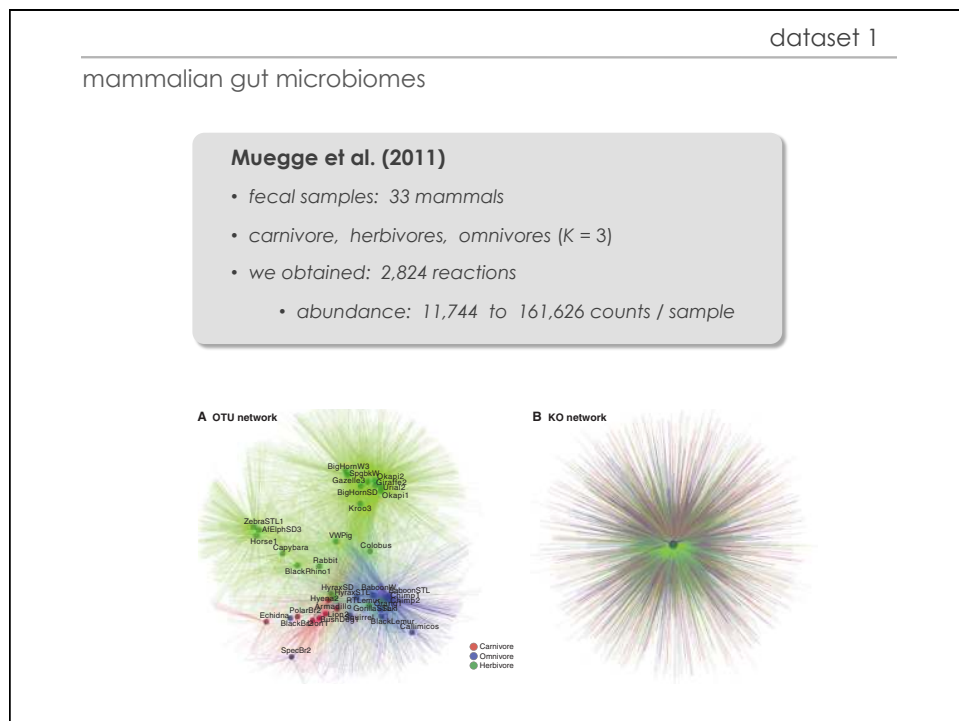
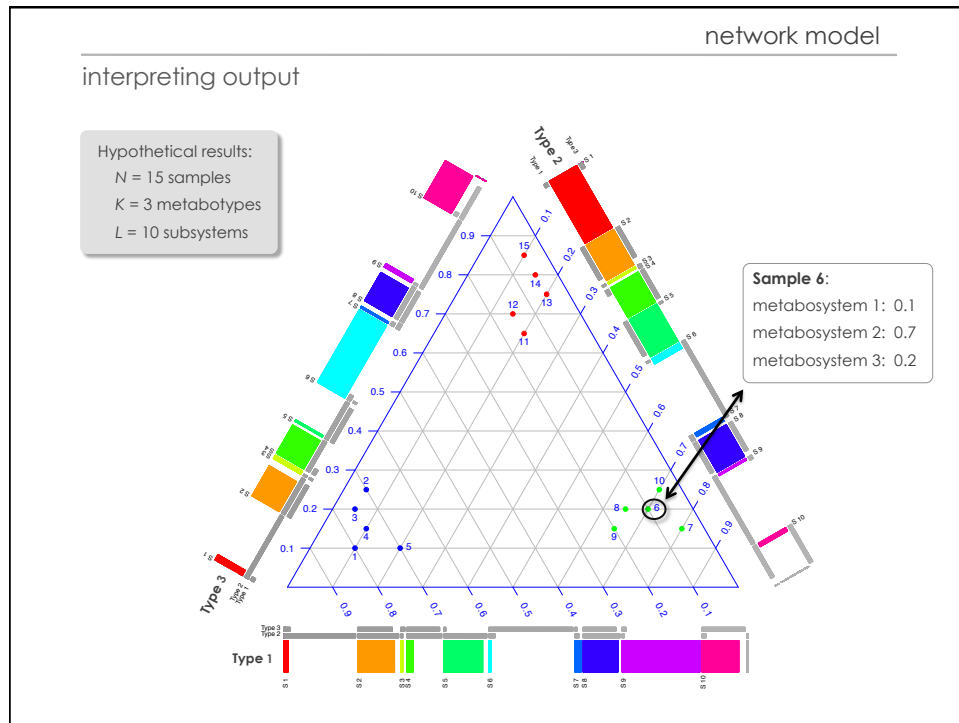


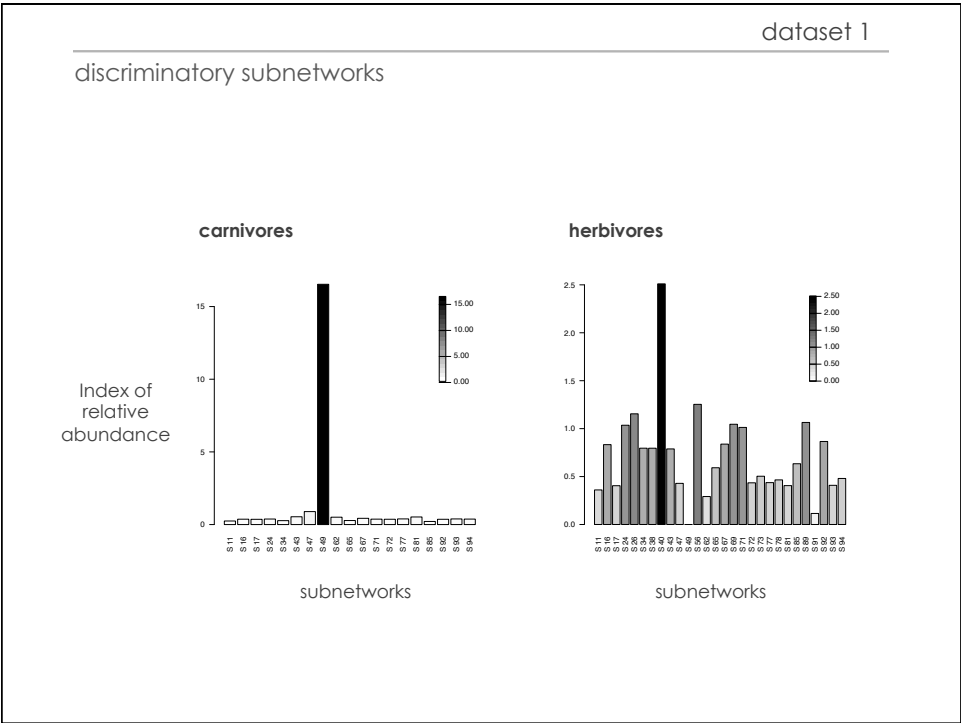
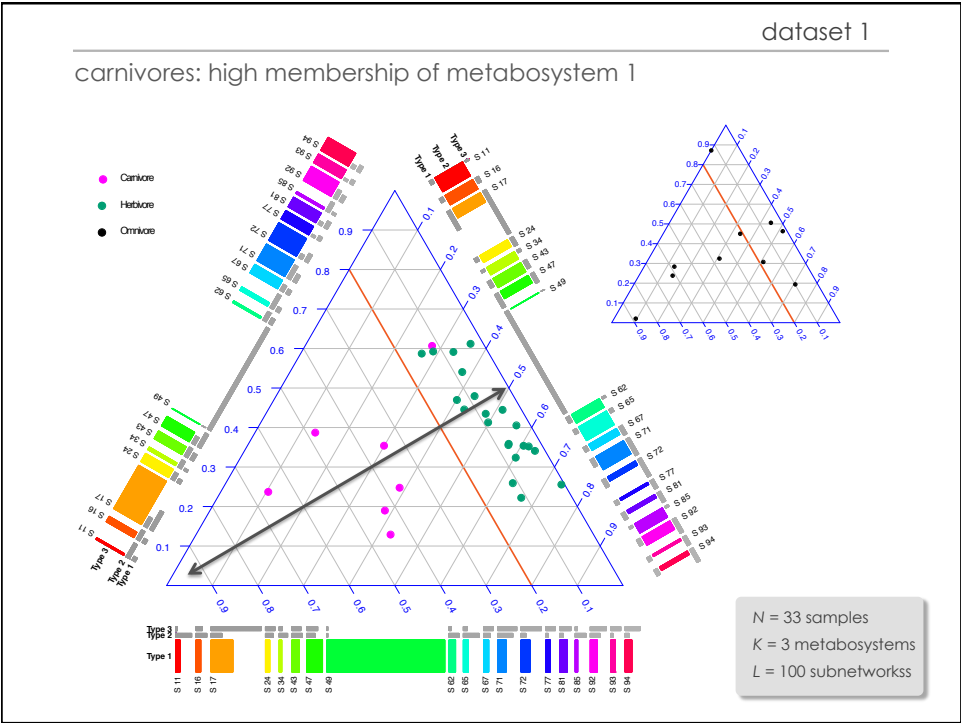






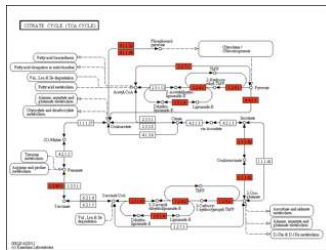
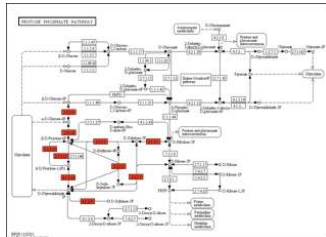
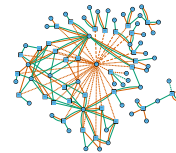




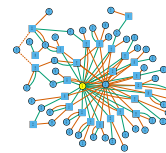


dataset 1

mammalian subnetworks

Core: correspond KEGG pathways**Discriminatory:** do not correspond to KEGG pathways

herbivore: S40



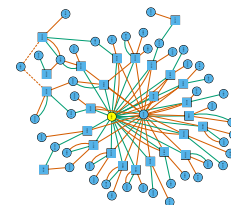
carnivore: S49

dataset 1

discriminatory for carnivores

subnetwork 49

- importation of certain extracellular saccharides
 - N-acetylmuramic acid
 - N-acetylglucosamine
 - fucose
 - glucose
 - mannose
- good for exploiting alternate carbohydrate sources
 - bacterial cell walls: N-acetylmuramic acid and N-acetylglucosamine
 - hosts secretions: fucosylated mucins

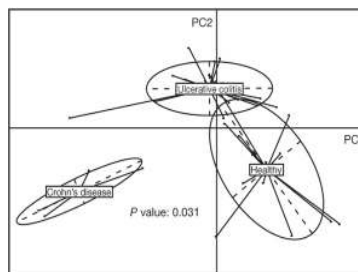


dataset 2

Human gut microbiomes

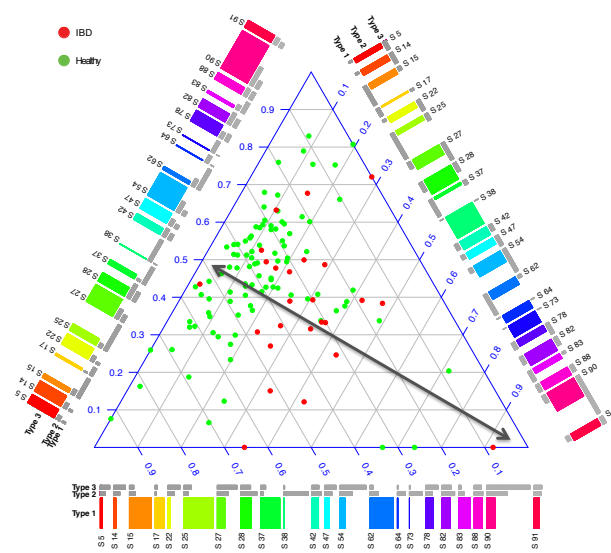
Qin et al. (2010)

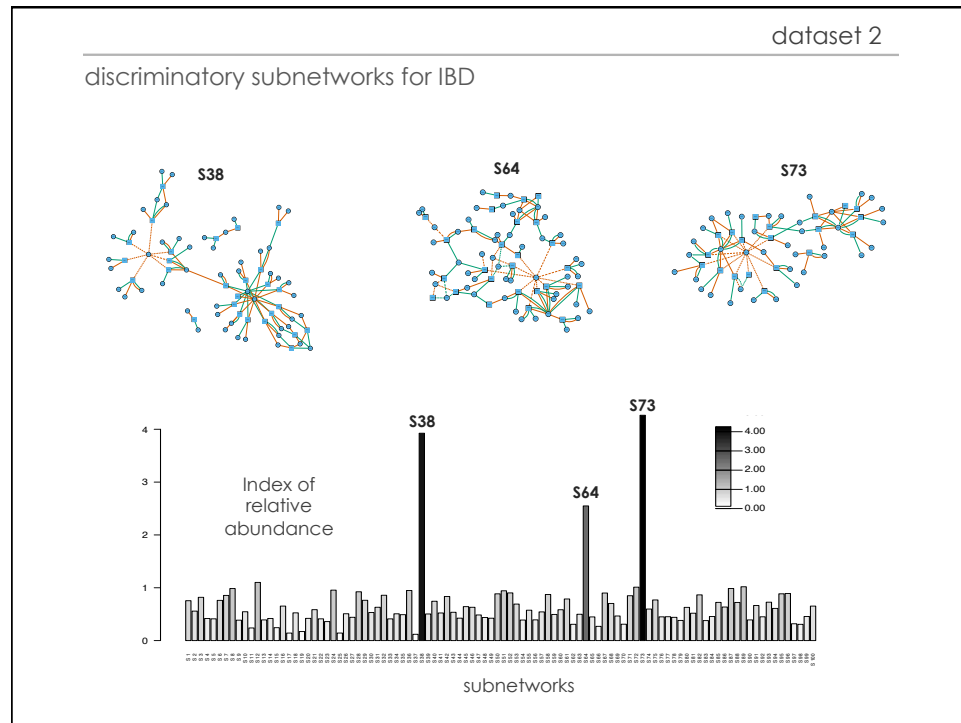
- 124 adult humans
 - 576.7 Gb of sequence data (4.5 Gb/sample)
- healthy, Crohn's, ulcerative colitis (K = 3)
- we obtained: 3,433 reactions
 - abundance: 5,968 to 1,270,409 counts / sample



dataset 2

Human gut microbiomes

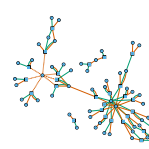




dataset 2

discriminatory for IBD

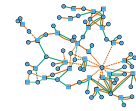
subnetwork 38



- Enriched for some PTS genes
 - suggests greater dependence on host-derived glycans for energy
 - mucin
 - shed-epithelial cells
 - suggests resistance to dietary changes
 - suggests close proximity to host cells
 - metabotype 2: greater impact on state of intestinal health
- no apparent connection to cause of gut inflammation of IBD
- other studies find enrichment of PTS genes in IBD patients

dataset 2

discriminatory for IBD



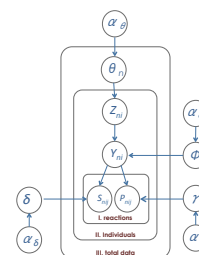
subnetwork 64

- enriched in ascorbate metabolism reactions
- metabolic profiling: IBD patients deficient in ascorbate
- ascorbate is an antioxidant
 - chronic IBD pathology related to excess reactive compounds
 - leads to oxidative stress within mucosa
 - IBD is associated with antioxidant levels and oxidative stress markers
 - absorption in gut depends on local gradient
 - metabotype 2 could interfere with human absorption

network model

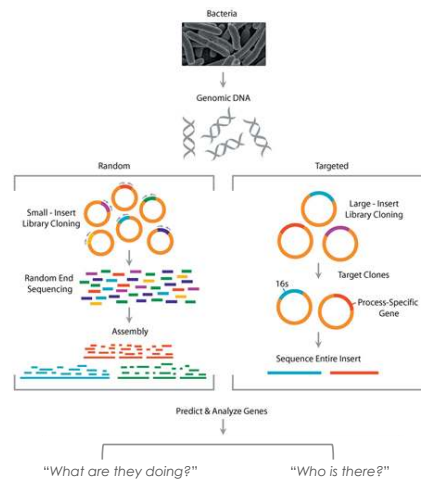
investigating community metabolic function

- any environment (soil, ocean, biofilm reactors, ...)
or scale (distance, time, ...)
- "soft" pathways, systems & metabosystems
- metatranscriptomes of un-cultivable microbes
- "supervision" should improve power
- number of reactions >> number of samples
- depends on data quality & processing



metagenomic inference

joint use of both sources of info ...



Adapted from: <http://legacy.camera.calit2.net/education/what-is-metagenomics>

let's take a break: ~20 mins?

part 2: searching for functional divergence in
genes and genomes

part 2: genes and genomes

overview

1. introduction (to ω ratio and codon models)
2. selected codon model
3. model based inference
4. gene-level example
5. genome-scale analyses

introduction

index of natural selection pressure: ω ratio

	U	C	A	G	
U	UUU Phe UUC Phe UUA Leu UUG Leu	UCU Ser UCC Ser UCA Ser UCG Ser	UAU Tyr UAC Tyr UAA Stop UAG Stop	UGU Cys UGC Cys UGA Stop UGG Trp	U C A G
C	CUU Leu CUC Leu CUA Leu CUG Leu	CCU Pro CCC Pro CCA Pro CCG Pro	CAU His CAC His CAA Gln CAG Gln	CGU Arg CGC Arg CGA Arg CGG Arg	U C A G
A	AUU Ile AUC Ile AUA Ile AUG Met	ACU Thr ACC Thr ACA Thr ACG Thr	AAU Asn AAC Asn AAA Lys AAG Lys	AGU Ser AGC Ser AGA Arg AGG Arg	U C A G
G	GUU Val GUC Val GUA Val GUG Val	GCU Ala GCC Ala GCA Ala GCG Ala	GAU Asp GAC Asp GAA Glu GAG Glu	GGU Gly GGC Gly GGA Gly GGG Gly	U C A G

<http://www.langara.bc.ca/biology/mario/Assets/Geneticcode.jpg>

Kimura (1968)

d_s : number of synonymous substitutions per synonymous site (K_s)

d_N : number of nonsynonymous substitutions per nonsynonymous site (K_A)

ω : the ratio d_N/d_s ; it measures selection at the protein level

introduction

index of natural selection pressure: ω ratio

rate ratio mode example

$\omega < 1$

purifying
(negative)
selection

histones

$\omega = 1$

Neutral
Evolution

pseudogenes

$\omega > 1$

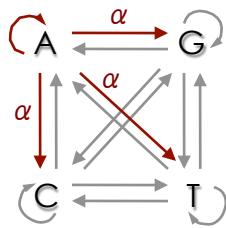
Diversifying
(positive)
selection

MHC,
Lysin

introduction

a model of sequence evolution: DNA

DNA state space



DNA transition matrix

to:

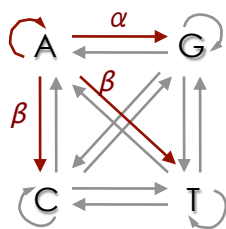
	A	C	G	T
from: A	-3α	α	α	α
C	α	-3α	α	α
G	α	α	-3α	α
T	α	α	α	-3α

* This is equivalent to most simple model for DNA (Jukes and Cantor, 1969).

introduction

a model of sequence evolution: DNA

DNA state space



DNA transition matrix

to:

	A	C	G	T
from: A	$*$	β	α	β
C	β	$*$	β	α
G	α	β	$*$	β
T	β	α	β	$*$

introduction

the CODON matrix is huge

universal code: 61 sense codons

	U	C	A	G	
U	UUU Phe UUC Phe UUA Leu UUG Leu	UCU Ser UCC Ser UCA Ser UCG Ser	UAU Tyr UAC Tyr UAA Stop UAG Stop	UGU Cys UGC Cys UGA Stop UGG Trp	U C A G
C	CUU Leu CUC Leu CUA Leu CUG Leu	CCU Pro CCC Pro CCA Pro CCG Pro	CAU His CAC His CAA Gln CAG Gln	CGU Arg CGC Arg CGA Arg CGG Arg	U C A G
A	AUU Ile AUC Ile AUA Ile AUG Met	ACU Thr ACC Thr ACA Thr ACG Thr	AAU Asn AAC Asn AAA Lys AAG Lys	AGU Ser AGC Ser AGA Arg AGG Arg	U C A G
G	GUU Val GUC Val GUA Val GUG Val	GCU Ala GCC Ala GCA Ala GCG Ala	GAU Asp GAC Asp GAA Glu GAG Glu	GGU Gly GGC Gly GGA Gly GGG Gly	U C A G

codon matrix:

$61 \times 61 = 3,721$
matrix elements

<http://www.langara.bc.ca/biology/mario/Assets/Geneticcode.jpg>

introduction

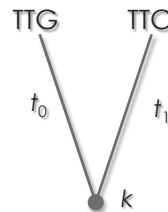
a model of sequence evolution: CODON

From codon below:	to codon below:						
	TTT (Phe)	TTC (Phe)	TTA (Leu)	TTG (Leu)	CTT (Leu)	CTC (Leu)	GGG (Gly)
TTT (Phe)	—	$\kappa\pi_{TTC}$	$\omega\pi_{TTA}$	$\omega\pi_{TTG}$	$\omega\kappa\pi_{TTT}$	0	...
TTC (Phe)	$\kappa\pi_{TTT}$	—	$\omega\pi_{TTA}$	$\omega\pi_{TTG}$	0	$\omega\kappa\pi_{CTC}$	...
TTA (Leu)	$\omega\pi_{TTT}$	$\omega\pi_{TTC}$	—	—	0	0	...
TTG (Leu)	$\omega\pi_{TTT}$	$\omega\pi_{TTC}$	$\kappa\pi_{TTA}$	—	0	0	...
CTT (Leu)	$\omega\kappa\pi_{TTT}$	0	0	0	—	$\kappa\pi_{CTC}$	...
CTC (Leu)	0	$\omega\kappa\pi_{TTC}$	0	0	$\kappa\pi_{TTT}$	—	...
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮
GGG (Gly)	0	0	0	0	0	0	—

* This is equivalent to the codon model of Goldman and Yang (1994). Parameter ω is the ratio d_N/d_S , κ is the transition/transversion rate ratio, and π_i is the equilibrium frequency of the target codon (i).

$$P(\mathbf{t}) = \{p_{ij}(\mathbf{t})\} = e^{Q\mathbf{t}}$$

compute the probability of codons



$$L_h(TTG, TTC) = \sum_k \pi_k p_{kTTG}(t_0) p_{kTTC}(t_1)$$

Note: analysis is typically done by using an unrooted tree

codon models

codon models

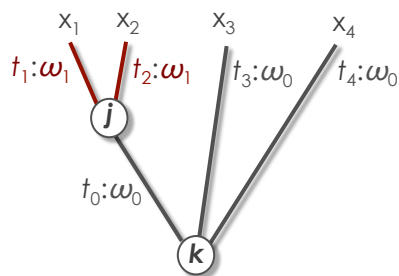
there are MANY different models

we will look at **three types of models**:

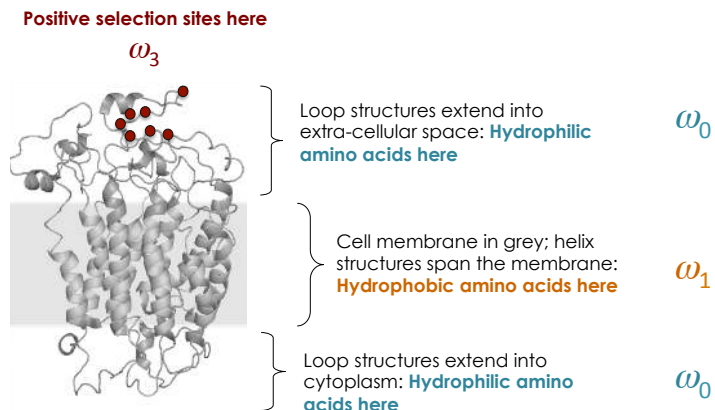
1. selection varies over time
2. selection varies among sites
3. selection varies among sites AND over time

codon models

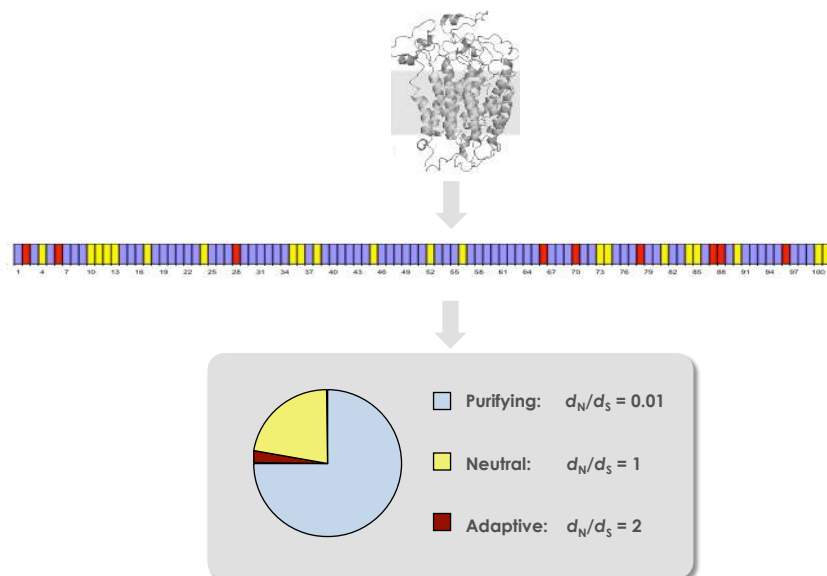
1. branch models: ω varies over time



codon models

2. site models: ω varies among sites

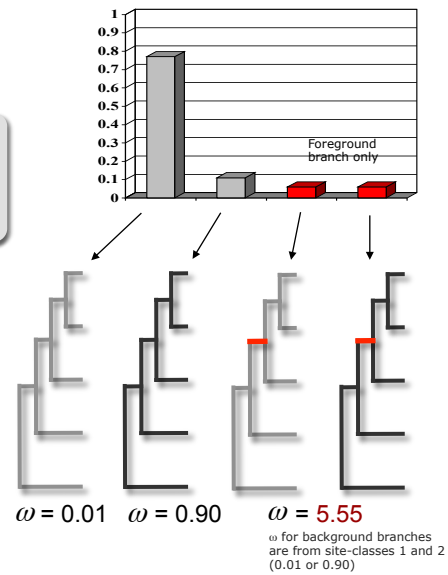
codon models

2. site models: ω varies among sites

codon models

3. branch-site model: ω varies among sites & branches

$$P(\mathbf{x}_h) = \sum_{i=0}^{K-1} p_i P(\mathbf{x}_h | \omega_i)$$



model based inference

analytical tasks

- Task 1.** parameter estimation (e.g., ω) 
- Task 2.** hypothesis testing
- Task 3.** make predictions (e.g., sites having $\omega > 1$)

Task 1

- we let the data tell us what the value of a parameter (e.g., ω) should be
- the optimal value for a parameter is the value that maximizes the probability of observing the data

Task 1

maximize likelihood and probability are inverted




Probabilities		Data	
		Data-1: 1H & 1T	Data-2: 2H
Hypotheses	$H_1: P(H) = 1/4$	0.375	0.0625
	$H_2: P(H) = 1/2$	0.5	0.25

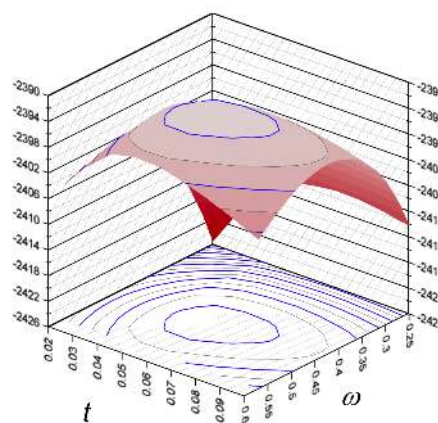
$$P(H|D) = \alpha P(D|H)$$

proportionality constant

Likelihoods		Data	
		Data-1: 1H & 1T	Data-2: 2H
Hypotheses	$H_1: P(H) = 1/4$	$\alpha_1 \times 0.375$	$\alpha_2 \times 0.0625$
	$H_2: P(H) = 1/2$	$\alpha_1 \times 0.5$	$\alpha_2 \times 0.25$

Task 1

maximum likelihood



Parameters: t and ω
Gene: acetylcholine α receptor



Task 2

How do we know that the estimate is significant?

Task 1. parameter estimation (e.g., ω) ✓

Task 2. hypothesis testing ← **LRT**

Task 3. prediction / site identification

Task 2

testing nested hypotheses by using the LRT

ℓ_0 is the maximum log likelihood under H_0 with parameters θ_0
and

ℓ_A is the maximum log likelihood under H_A with parameters θ_A

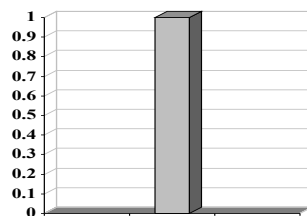
$$\text{Test statistic} = 2\Delta\ell = 2(\ell_0(\theta_0) - \ell_A(\theta_A))$$

Degrees of freedom = difference in the number of parameters between the two models

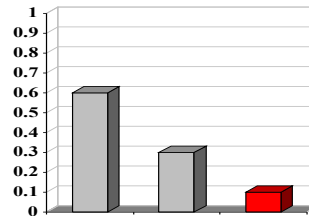
Task 2

LRT: Does selection pressure vary among sites?

H₀: uniform selective pressure among sites (M0)
H_A: variable selective pressure among sites (M3)
 Compare $2\Delta l = 2(l_1 - l_0)$ with a χ^2 distribution

H₀: Model 0

$\hat{\omega} = 0.65$

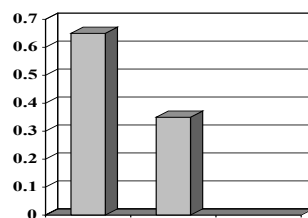
H_A: Model 3

$\hat{\omega} = 0.01$ $\hat{\omega} = 0.90$ $\hat{\omega} = 5.55$

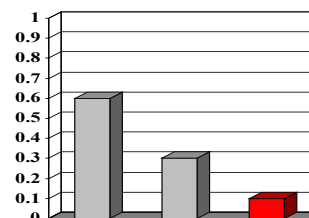
Task 2

LRT: Have some sites evolved under positive selection?

H₀: variable selective pressure but NO positive selection (M1)
H_A: variable selective pressure with positive selection (M2)
 Compare $2\Delta l = 2(l_1 - l_A)$ with a χ^2 distribution

H₀: Model 1a

$\hat{\omega} = 0.5$ ($\omega = 1$)

H_A: Model 2a

$\hat{\omega} = 0.5$ ($\omega = 1$) $\hat{\omega} = 3.25$

Task 3

How do we identify the selected sites?

Task 1. parameter estimation (e.g., ω) ✓

Task 2. hypothesis testing ✓

Task 3. prediction / site identification ← **Bayes' rule**

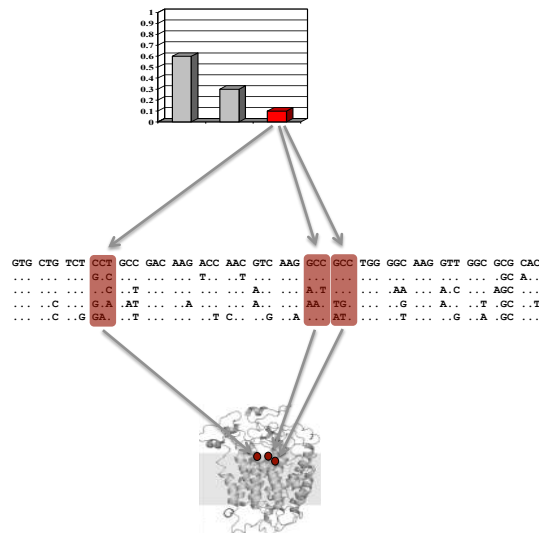
Task 3

Which sites have $\omega > 1$?

model:
5% have $\omega > 1$

Bayes' rule:
site 4, 12 & 13

structure:
sites are in contact



Task 3

Bayes' rule for identifying selected sites

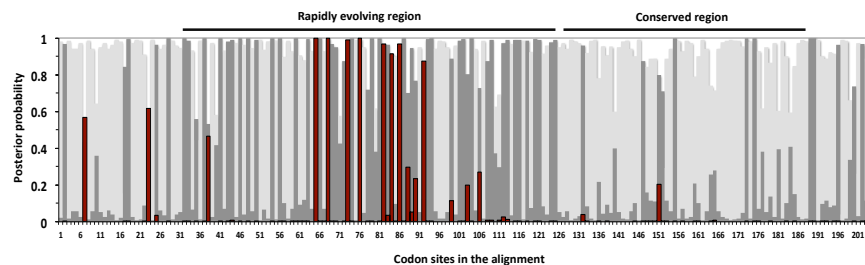
- site class 0: $\omega_0 = .03$, 85% of codon sites
- site class 1: $\omega_1 = .40$, 10% of codon sites
- ? → ■ **site class 2: $\omega_2 = 14$, 05% of codon sites**

Bayes' rule:

$$P(\omega_2 | \mathbf{x}_h) = \frac{p_2 P(x_h | \omega_2)}{P(x_h)}$$

Task 3

Bayes' rule for identifying selected sites



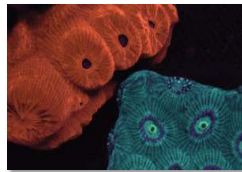
- Site class 0: $\omega_0 = .03$ (strong purifying selection)
- Site class 1: $\omega_1 = .40$ (weak purifying selection)
- **Site class 2: $\omega_2 = 5$ (positive selection)**

NOTE: The posterior probability should NOT be interpreted as a "P-value"; it can be interpreted as a measure of relative support

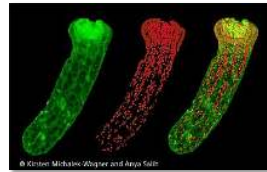
gene-level example

gene-level example

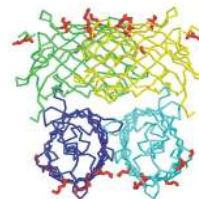
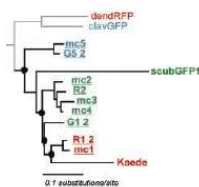
colour diversity of coral pigments



Red/blue colour morphs of the great star coral *Montastraea cavernosa*



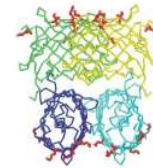
© Kirsten Mikusinski-Wagner and Ranya Yalci



- Is color diversity tuned by natural selection?
- Is there a relationship between colour and endosymbiotic algae?

gene-level example

green fluorescent proteins (GFPs) in corals

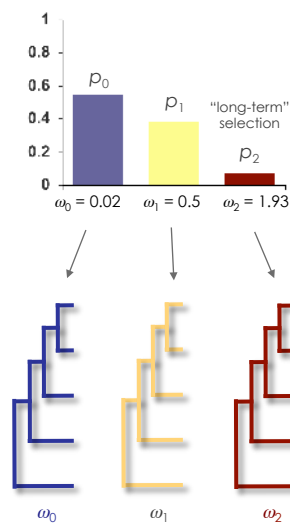


questions we have:

1. What is the intensity of selection on coral GFPs
2. Have there been episodes of positive selection during the evolution of colour diversity?
3. Are some sites in GFPs positively selected?
4. Which sites?
5. What happens to the colour when the amino acid is changes at these sites?

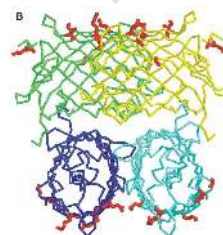
gene-level example

signal 1: long term (diversifying) selection

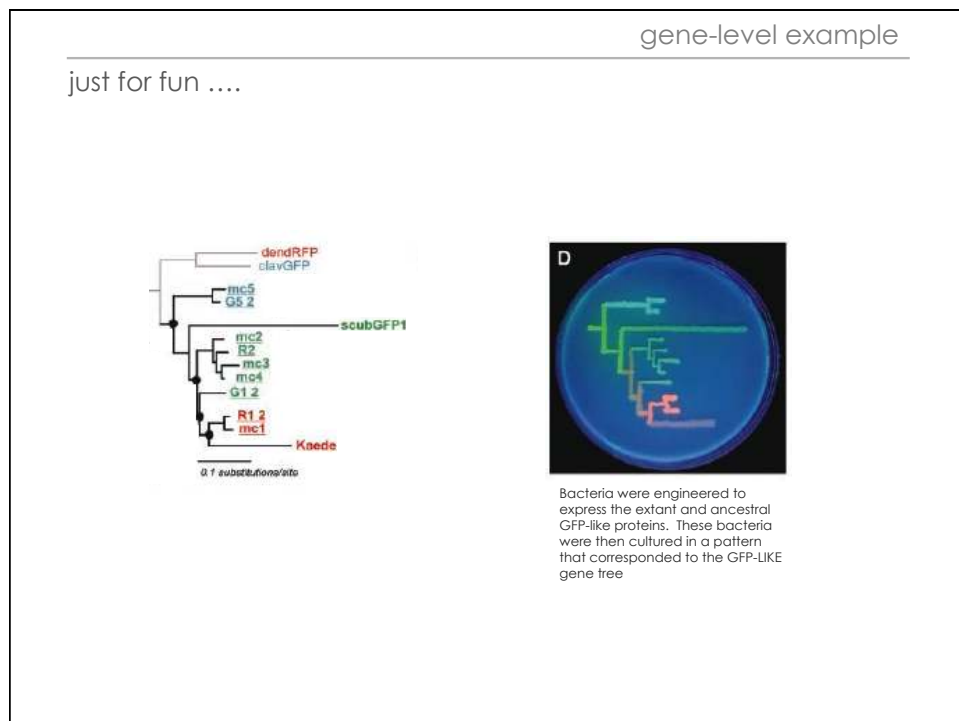
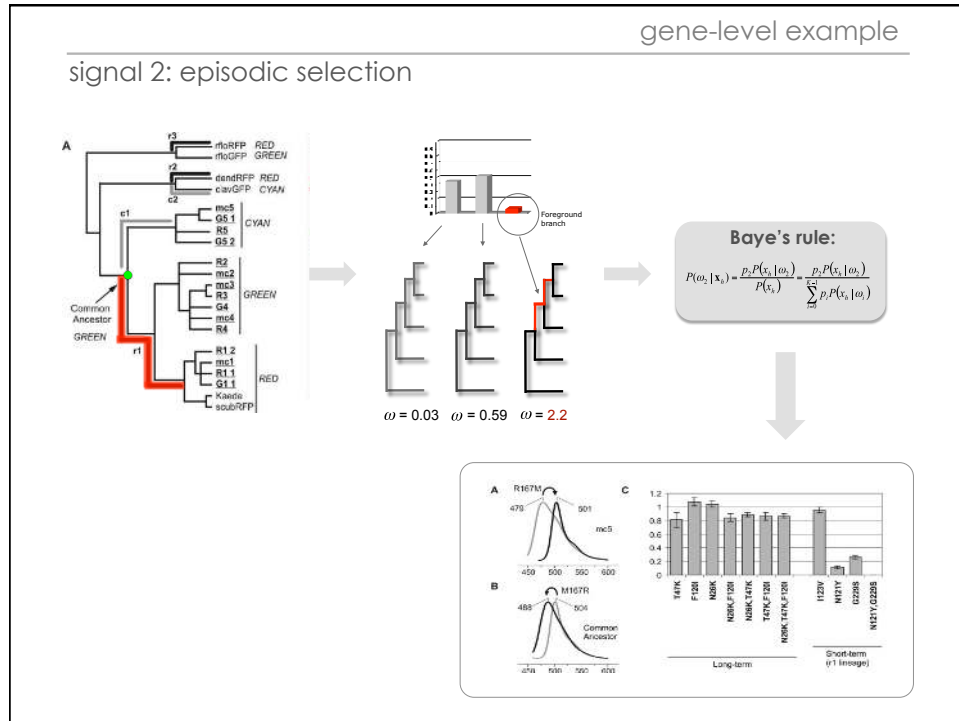


Bayes' rule:

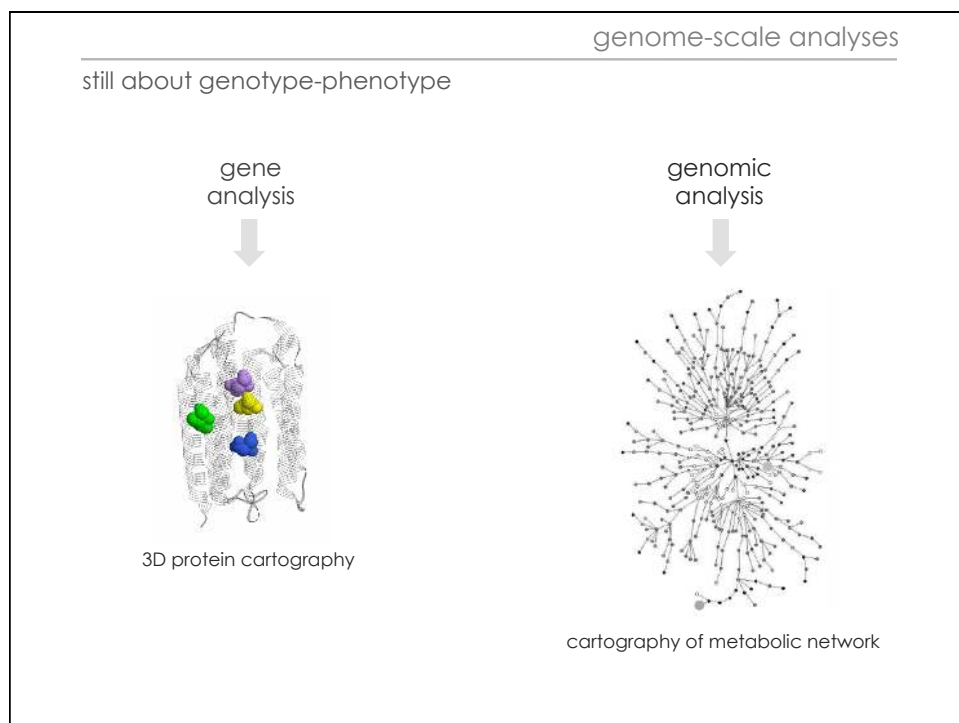
$$P(\omega_2 | \mathbf{x}_h) = \frac{p_2 P(\mathbf{x}_h | \omega_2)}{P(\mathbf{x}_h)} = \frac{p_2 P(\mathbf{x}_h | \omega_2)}{\sum_{i=0}^{K-1} p_i P(\mathbf{x}_h | \omega_i)}$$



sites in red correspond to the protein-binding region of **non-colored** homologs of these GFP proteins



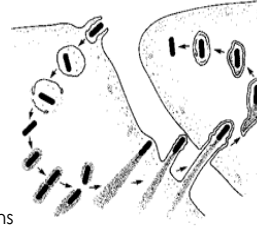
genome-scale analysis



genome-scale analyses

bacterial genus *Listeria*

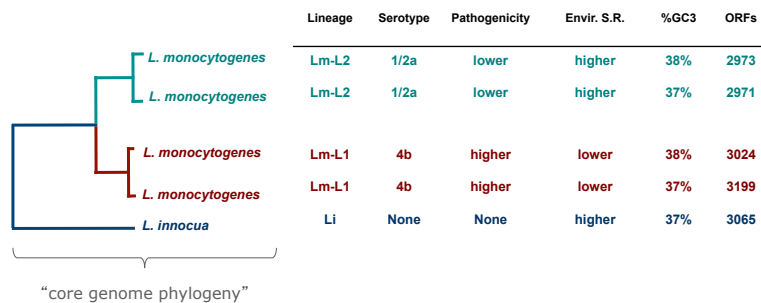
- gram positive
- no capsule
- non-spore forming
- low G+C%
- facultative anaerobes
- rod shaped
- opportunistic pathogens



- genus contains pathogenic and non-pathogenic species
- lineages of *L. monocytogenes* differ in (i) population structure, (ii) ability to respond to stress, and (iii) pathogenicity
- *L. monocytogenes* is serious food-borne pathogen; hence, several genomes

genome-scale analyses

core genome analysis

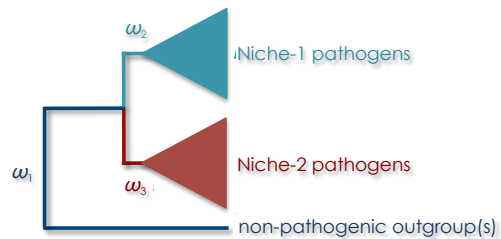


- 1905 "core" genes
- concatenated genes
- 82% of single core genes

- mosaic genome:
- > 18% recombination (HR)
- loci w/ "extended gene pools"

genome-scale analyses

branch models: divergent selection pressure



null (1 parameter):

$$H_0: \omega_1 = \omega_2 = \omega_3$$

2 parameter alternatives:

$$H_1: \omega_1 \neq \omega_2 = \omega_3$$

$$H_2: \omega_1 = \omega_2 \neq \omega_3$$

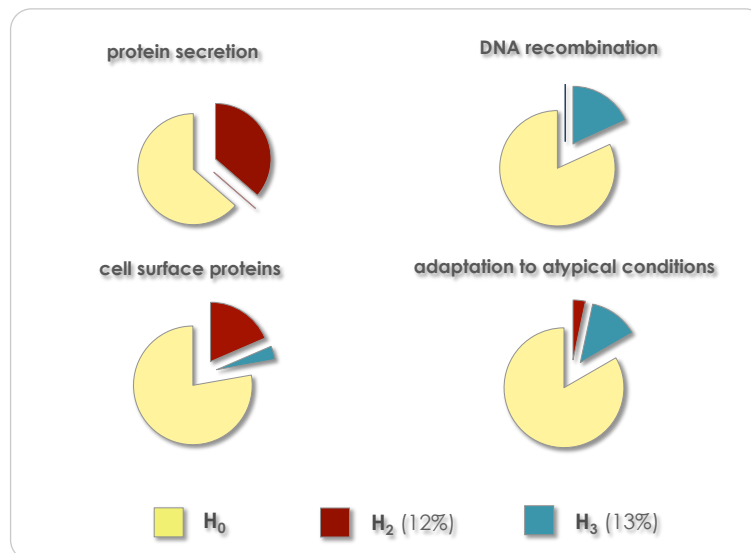
$$H_3: \omega_1 = \omega_3 \neq \omega_2$$

3 parameter alternative:

$$H_4: \omega_1 \neq \omega_2 \neq \omega_3$$

genome-scale analyses

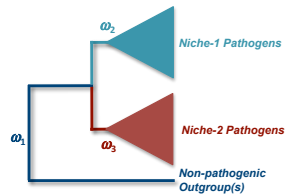
patterns of divergent selection



genome-scale analyses

patterns of divergent selection

A: Gene-level data analysis



Null model (1 parameter):

$$H_0 : \omega_1 = \omega_2 = \omega_3$$

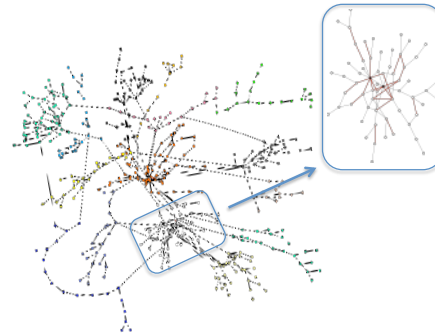
Alternatives (2 parameters):

$$H_1 : \omega_1 \neq \omega_2 = \omega_3$$

$$H_2 : \omega_1 = \omega_2 \neq \omega_3$$

$$H_3 : \omega_1 = \omega_3 \neq \omega_2$$

B: Phenotype-level data analysis



3 modules, and 3 KEGG pathways, were significantly associated with a particular pattern of selection pressure (H_1 , H_2 , or H_3).

genome-scale analyses

divergent selection & gene expression

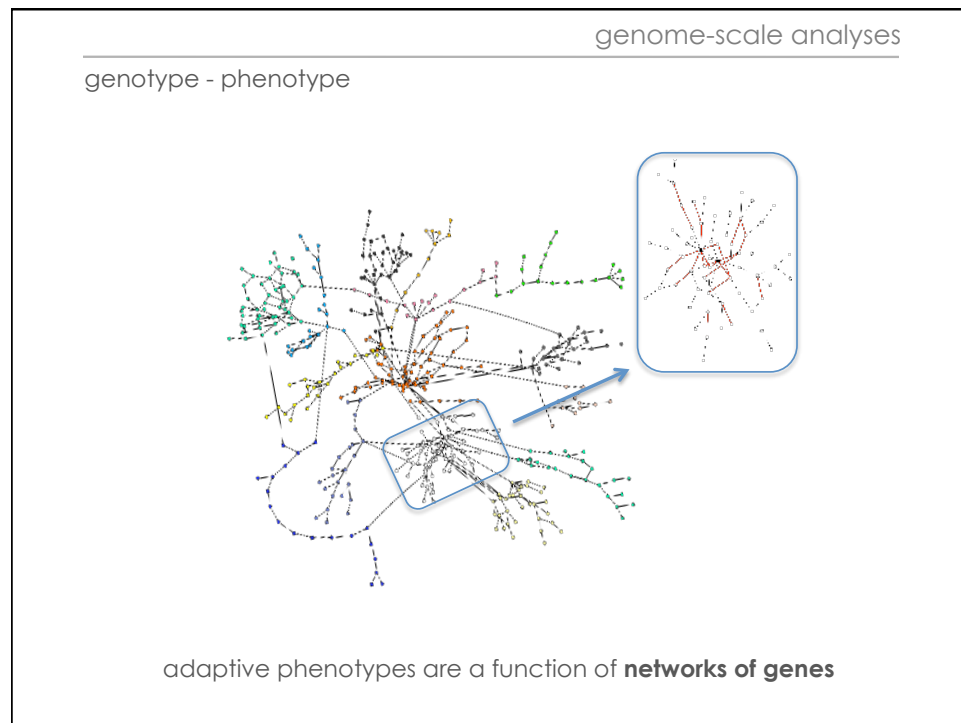
Odds of divergent selection when gene expression is altered during invasive disease

genes	odds of divergent selection		altered vs. unaltered expression	
	altered expression	unaltered expression	odds ratio	P-value
growth & survival*	0.506	0.293	1.72	0.017
other	0.320	0.392	0.82	0.1098

* genes in ListiList categories considered critical to intracellular growth & survival

For genes critical to intracellular growth:

The odds of divergent selection pressure was significantly higher if a gene had altered expression during intracellular growth.



"We are drowning in information and starving for knowledge."

— Rutherford D. Roger